

## 1-1 Entering Matrix

The best way for you to get started with MATLAB is to learn how to handle matrices. You only have to follow a few basic conventions:

- Separate the elements of a row with blanks or commas.
- Use a semicolon ( ; ) to indicate the end of each row.
- Surround the entire list of elements with square brackets, [ ].

For Example

```
>> A = [16 3 2 13; 5 10 11 8; 9 6 7 12; 4 15 14 1]
```

MATLAB displays the matrix you just entered.

```
A =  
    16     3     2    13  
     5    10    11     8  
     9     6     7    12  
     4    15    14     1
```

Once you have entered the matrix, it is automatically remembered in the MATLAB workspace. You can refer to it simply as **A**. Also you can enter and change the values of matrix elements by using **workspace** window.

## 1-2 Subscripts

The element in row **i** and column **j** of **A** is denoted by **A(i, j)**. For example, **A(4, 2)** is the number in the fourth row and second column. For the above matrix, **A(4, 2)** is **15**. So to compute the sum of the elements in the fourth column of **A**, type

```
>> A(1,4) + A(2,4) + A(3,4) + A(4,4)  
ans =  
    34
```

You can do the above summation, in simple way by using **sum** command.

If you try to use the value of an element outside of the matrix, it is an error.

```
>> t = A(4,5)
??? Index exceeds matrix dimensions.
```

On the other hand, if you store a value in an element outside of the matrix, the size increases to accommodate the newcomer. The initial values of other new elements are zeros.

```
>> X = A;
>> X(4,5) = 17

X =
16   3   2  13   0
 5  10  11   8   0
 9   6   7  12   0
 4  15  14   1  17
```

### 1-3 Colon Operator

The colon " : " is one of the most important MATLAB operators. It occurs in several different forms. The expression

```
>> 1:10
```

is a row vector containing the integers from 1 to 10

```
1 2 3 4 5 6 7 8 9 10
```

To obtain nonunit spacing, specify an increment. For example,

```
>> 100:-7:50
100 93 86 79 72 65 58 51
```

Subscript expressions involving colons refer to portions of a matrix.

```
>>A(1:k, j)
```

is the first k elements of the jth column of A.

The colon by itself refers to *all* the elements in a row or column of a matrix and the keyword **end** refers to the *last* row or column. So

```
>> A(4, :)           or       >> A(4, 1:end)   give the same action
ans =
4     15     14     1

>> A(2, end)
ans =
8
```

### 1-4 Basic Matrix Functions

Command	Description
<pre><b>sum(x)</b> &gt;&gt; x=[1 2 3       4 5 6]; &gt;&gt; sum(x) ans =       5      7      9  &gt;&gt; sum(x, 2) ans=       6      15  &gt;&gt;sum(sum(x) ) ans =      21</pre>	<p>The sum of the elements of x. For matrices, sum(x) is a row vector with the sum over each column.</p> <p>sum(x,dim) sums along the dimension dim.</p> <p>In order to find the sum of elements that are stored in matrix with <i>n</i> dimensions, you must use <b>sum</b> command <i>n</i> times in cascade form, this is also applicable for <b>max</b>, <b>min</b>, <b>prod</b>, <b>mean</b>, <b>median</b> commands.</p>

Command	Description
<pre> <b>mean (x)</b> x=[1 2 3; 4 5 6]; &gt;&gt; mean(x) ans =     2.5    3.5    4.5  &gt;&gt; mean(x,2) ans =      2      5  &gt;&gt;mean(mean(x)) ans =     3.5000 </pre>	<p>The average of the elements of x. For matrices, mean(x) is a row vector with the average over each column.</p> <p>mean (x,dim) averages along the dimension dim.</p>
<pre> <b>zeros (N)</b> <b>zeros (N,M)</b> &gt;&gt; zeros(2,3) ans =      0     0     0      0     0     0 </pre>	<p>Produce N by N matrix of zeros.</p> <p>Produce N by M matrix of zeros.</p>
<pre> <b>ones (N)</b> <b>ones (N,M)</b> &gt;&gt; ones(2,3) ans =      1     1     1      1     1     1 </pre>	<p>Produce N by N matrix of ones.</p> <p>Produce N by M matrix of ones.</p>

Command	Description
<pre><b>size(x)</b> &gt;&gt; x=[1 2 3       4 5 6]; &gt;&gt; size(x) ans =       2      3</pre>	return the size (dimensions) of matrix x.
<pre><b>length(v)</b> &gt;&gt; v=[1 2 3]; &gt;&gt; length(v) ans =       3</pre>	return the length (number of elements) of vector v.
<pre><b>numel(x)</b>  &gt;&gt; v = [55 63 34]; &gt;&gt; numel(v) ans =       3  &gt;&gt; x=[1 2       4 5       7 8 ]; &gt;&gt; numel(x) ans =       6</pre>	returns the number of elements in array x.

Command	Description
<pre>single quote ( ' )  &gt;&gt; x=[1 2 3       4 5 6       7 8 9];  &gt;&gt; x'  ans =      1     4     7      2     5     8      3     6     9  &gt;&gt; v=[1 2 3];  &gt;&gt; v'  ans =      1      2      3</pre>	<p>Matrix transpose. It flips a matrix about its main diagonal and it turns a row vector into a column vector.</p>
<pre><b>max (x)</b>  &gt;&gt; x=[1 2 3       4 5 6];  &gt;&gt; max (x)  ans =      4     5     6  &gt;&gt; max(max(x))  ans =      6</pre>	<p>Find the largest element in a matrix or a vector.</p>

Command	Description
<pre> <b>min (x)</b> &gt;&gt; x=[1 2 3       4 5 6]; &gt;&gt; min (x) ans =       1      2      3 &gt;&gt; min(min(x)) ans =       1 </pre>	<p>Find the smallest element in a matrix or a vector.</p>
<pre> <b>magic (N)</b> &gt;&gt; magic(3) ans =       8      1      6       3      5      7       4      9      2 </pre>	<p>produce N Magic square. This command produces valid magic squares for all N&gt;0 except N=2.</p>
<pre> <b>inv (x)</b> &gt;&gt; x=[1 4;       5 8]; &gt;&gt; inv(x) ans =     -0.6667    0.3333      0.4167   -0.0833 </pre>	<p>produce the inverse of matrix x.</p>

Command	Description
<pre> <b>diag(x)</b> &gt;&gt; x=[1  2  3       4  5  6       7  8  9];  &gt;&gt; diag(x)  ans =      1      5      9  &gt;&gt; v=[1 2 3]; &gt;&gt; diag(v)  ans =      1     0     0      0     2     0      0     0     3 </pre>	<p>Return the diagonal of matrix x. if x is a vector then this command produce a diagonal matrix with diagonal x.</p>
<pre> <b>prod(x)</b> &gt;&gt; x=[1 2 3       4 5 6];  &gt;&gt; prod(x)  ans =  4    10    18  &gt;&gt; prod(prod(x))  ans =     720 </pre>	<p>Product of the elements of x. For matrices, Prod(x) is a row vector with the product over each column.</p>



Command	Description
<pre> <b>median(x)</b> x=[4 6 8     10 9 1     8 2 5]; &gt;&gt; median(x) ans =      8     6     5 &gt;&gt; median(x,2) ans =      6      9      5 &gt;&gt; median(median(x)) ans =      6 </pre>	<p>The median value of the elements of x. For matrices, median(x) is a row vector with the median value for each column.</p> <p>median(x,dim) takes the median along the dimension dim of x.</p>
<pre> <b>sort(x,DIM,MODE)</b> &gt;&gt; x = [3 7 5         0 4 2]; &gt;&gt; sort(x,1) ans =      0     4     2      3     7     5 &gt;&gt; sort(x,2) ans =      3     5     7      0     2     4 &gt;&gt; sort(x,2,'descend') ans =      7     5     3      4     2     0 </pre>	<p>Sort in ascending or descending order.</p> <p>- For vectors, sort(x) sorts the elements of x in ascending order.</p> <p>For matrices, sort(x) sorts each column of x in ascending order.</p> <p>DIM= 1            by default  MODE= 'ascend'   by default</p>

Command	Description
<pre> <b>det(x)</b>  &gt;&gt; x=[5 1 8       4 7 3       2 5 6];  &gt;&gt; det(x)  ans =      165 </pre>	<p>Det is the determinant of the square matrix x.</p>
<pre> <b>tril(x)</b>  &gt;&gt; x=[5 1 8       4 7 3       2 5 6];  &gt;&gt; tril(x)  ans =       5     0     0      4     7     0      2     5     6 </pre>	<p>Extract lower triangular part of matrix x.</p>
<pre> <b>triu(x)</b>  &gt;&gt; x=[5 1 8       4 7 3       2 5 6];  &gt;&gt; triu(x)  ans =       5     1     8      0     7     3      0     0     6 </pre>	<p>Extract upper triangular part of matrix x.</p>

**Note**

When we are taken away from the world of linear algebra, matrices become two-dimensional numeric arrays. Arithmetic operations on arrays are done element-by-element. This means that addition and subtraction are the same for arrays and matrices, but **that multiplicative operations are different**. MATLAB uses a **dot ( . ), or decimal point, as part of the notation for multiplicative array operations**.

**Example:** Find the factorial of 5

```
>> x=2:5;
>> prod(x)
```

**Example:** if  $x = [1,5,7,9,13,20,6,7,8]$ , then

- replace the first five elements of vector  $x$  with its maximum value.
- reshape this vector into a 3 x 3 matrix.

solution

```
a)
>> x(1:5)=max(x)

b)
>> y(1,:) = x(1:3);
>> y(2,:) = x(4:6);
>> y(3,:) = x(7:9);
>> y
```

**Example:** Generate the following row vector  $b=[1, 2, 3, 4, 5, \dots, 9,10]$ , then transpose it to column vector.

solution

```
>> b=1:10
b =
     1     2     3     4     5     6     7     8     9    10
>> b=b';
```

**Exercises**

1- If  $x = \begin{bmatrix} 1 & 4 \\ 8 & 3 \end{bmatrix}$ , find :

- a) the inverse matrix of  $x$  .
- b) the diagonal of  $x$ .
- c) the sum of each column and the sum of whole matrix  $x$ .
- d) the transpose of  $x$ .

2- If  $x = \begin{bmatrix} 2 & 8 & 5 \\ 9 & 7 & 1 \end{bmatrix}$ ,  $b = [2 \ 4 \ 5]$  find:

- a) find the maximum and minimum of  $x$ .
- b) find median value over each row of  $x$ .
- c) add the vector  $b$  as a third row to  $x$ .

3- If  $x = \begin{bmatrix} 2 & 6 & 12 \\ 15 & 6 & 3 \\ 10 & 11 & 1 \end{bmatrix}$ , then

- a) replace the first row elements of matrix  $x$  with its average value.
- b) reshape this matrix into row vector.

4- Generate a 4 x 4 Identity matrix.

5- Generate the following row vector  $b = [5, 10, 15, 20 \dots \dots \dots 95, 100]$ , then find the number of elements in this vector.

