



# Solar Thermal Technology - Daily Water Heating Energy Load



# Refrigeration and Air conditioning Techniques Engineering Department



**Subject : Renewable Energy**  
**Grade: 4<sup>th</sup> Class**

**Lecture :7**  
**Estimate Daily Water Heating Load**

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**2019-2020**



# Simple Evaluation Procedure \_-Solar Water Heater



- Estimate Daily Water Heating Load
- Determine Solar Resource
- Calculate Solar System Size
- Calculate Annual Energy Savings
- Calculate Annual Cost Savings
- Estimate System Cost
- Calculate Savings-to-Investment Ratio and Simple Payback Period



# Daily Water Heating Energy Load



$$L = MC (T_{\text{hot}} - T_{\text{cold}})$$

L = Daily Hot Water Energy Load  
(kWh/day)

M = mass of water per day (kg/day),  
3.785 kg/gallon

C = specific heat of water =  
0.001167 kWh/kg°C

$T_{\text{hot}}$  = hot water delivery temperature  
(°C), often 50 °C = 120 °F

$T_{\text{cold}}$  = cold water temperature (°C),  
often 18 °C = 65 °F

## Typical Hot Water Usage:

Dormitory ( مبنى للطلبة او القسم الداخلي )  
13 gal/day/person

Motel 15 gal/day/unit

Hospital 18 gal/day/bed

Office 1  
gal/day/person

Food Service 2.4 gal/meal

Residence 40  
gal/day/person

School 1.8  
gal/day/student



# Solar Water Heating System Size and Savings



## Solar System Size

$$A_c = L / (\eta_{\text{solar}} I_{\text{max}})$$

$A_c$  = collector area (m<sup>2</sup>)

$L$  = Daily Load (kWh/day)

$\eta_{\text{solar}}$  = efficiency of solar system (typically 0.40)

$I_{\text{max}}$  = maximum daily solar radiation (kWh/m<sup>2</sup>/day)

## Annual Energy Savings

$$E_s = A_c I_{\text{ave}} \eta_{\text{solar}} 365 / \eta_{\text{boiler}}$$

$I_{\text{ave}}$  = average solar radiation (kWh/m<sup>2</sup>/day)

$\eta_{\text{boiler}}$  = auxiliary heater efficiency

gas	0.43 to 0.86
electric	0.77 to 0.97
propane	0.42 to 0.86
oil	0.51 to 0.66



# Solar Water Heating System Cost and Savings



## Solar System Cost

$$C = C_{\text{solar}} A_c$$

C = Installed Cost of Solar System (\$)

$C_{\text{solar}}$  = per-unit-area cost of installed solar system (\$/m<sup>2</sup>), typically

\$300/ m<sup>2</sup> for large system

\$1000/m<sup>2</sup> for small systems

\$650/ m<sup>2</sup> might be average

## Annual Cost Savings

$$S = E_s C_e$$

S = annual cost savings (\$/year)

$C_e$  = cost of auxiliary energy

typically:

Electricity     \$0.084/kWh

Natural Gas    \$0.020/kWh

Propane        \$0.040/kWh

Oil               \$0.025/kWh





# Solar Water Heating System Cost and Savings



## Solar Water Heating System Cost Effectiveness

### Savings-to-Investment Ratio

$$SIR = S * pwf / C$$

***project is cost effective if SIR > 1.***

pwf = present worth factor for future savings stream, = 24 years for 40 year lifetime and 3% real discount rate (specified by NIST).

EISA 2007 specifies the 40 year analysis period (lifetime)

### Simple Payback Period

$$SPB = C / S$$



# Example: 4 person residence in Denver against electricity



- |  $M = 4 \text{ person} * 40 \text{ gal/person/day} * 3.785 \text{ kg/gal} = \mathbf{606 \text{ kg/day}}$
- |  $L = MC(T_{\text{hot}} - T_{\text{cold}}) = 606 \text{ kg/day} * 0.001167 \text{ kWh/kgC} * (50\text{C} - 18\text{C}) = \mathbf{22.6 \text{ kWh/day}}$
- | For Denver,  $I_{\text{max}} = 6.1$  and  $I_{\text{ave}} = 5.5 \text{ kWh/m}^2/\text{day}$
- |  $A_c = L / (\eta_{\text{solar}} I_{\text{max}}) = 22.6 \text{ kWh/day} / (0.4 * 6.1 \text{ kWh/m}^2/\text{day}) = \mathbf{9.3 \text{ m}^2}$
- |  $E_s = A_c I_{\text{ave}} \eta_{\text{solar}} 365 / \eta_{\text{boiler}} = 9.3 \text{ m}^2 * 5.5 \text{ kWh/m}^2.\text{day} * 0.4 * 365 \text{ days/year} / 0.97 = \mathbf{7,665 \text{ kWh/year}}$
- |  $C = c_{\text{solar}} A_c = \$650/\text{m}^2 * 9.3 \text{ m}^2 = \mathbf{\$6,045}$
- |  $S = E_s C_e = 7,665 \text{ kWh/year} * \$0.084/\text{kWh} = \mathbf{\$644/\text{year}}$
- |  $\text{SIR} = S * \text{pwf} / C = \$644/\text{year} * 15.5 \text{ years} / \$6,045 = \mathbf{1.65}$
- | **SO IT IS COST EFFECTIVE!**





# Hot water demand



The most important parameter that needs to be considered in the design of a water heating system is the hot water demand over a certain period of time (hourly, daily, or monthly). The energy demand,  $L$ , required for the generation of sanitary hot water can be obtained if the volumetric consumption,  $V$ , is known for the required time period. Also required are the temperatures of the cold water supplied by public mains,  $T_m$ , and the water distribution,  $T_w$ . Then

$$L = V \rho c_p (T_w - T_m)$$

for the monthly water demand, the following equation can be used:

$$V = N_{days} N_{persons} V_{person}$$

where

$N_{days}$ : number of days in a month.

$N_{persons}$ : number of persons served by the water heating system.

$V_{person}$ : Volume of hot water required per person.



# Hot water demand



Example : Estimate the hot water energy demand for a family of four, with medium normal consumption, cold water mains supply of  $18^{\circ}\text{C}$ , and water distribution temperature of  $45^{\circ}\text{C}$ .

## Solution:

According to Table 3.4, the consumption per day per person is 40 L. Therefore, the daily demand,  $V$ , is 160 L/d or 0.16  $\text{m}^3/\text{d}$ .

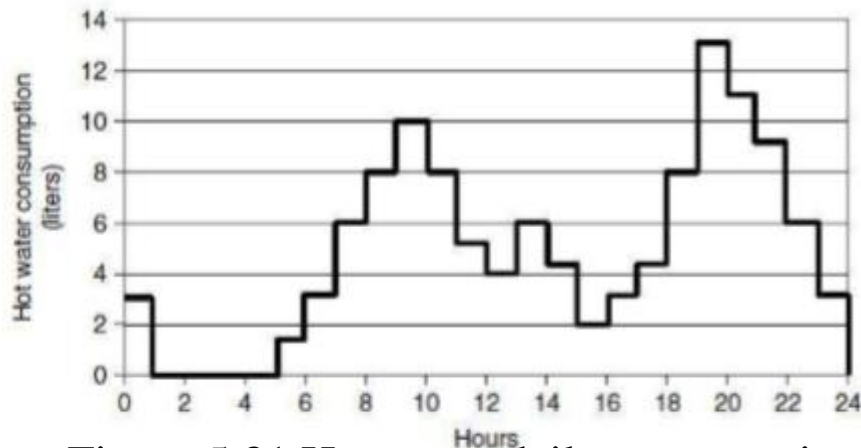


Figure 5.31 Hot water daily consumption profile

Guideline	Low	Medium	High
Normal consumption	26	40	54
Maximum consumption	66	85	104

Table 3.4 Hot Water Daily Demand for a Family of Four Persons in Liters per Person



# Symbol and Formula Used



$$Q_u = A_c F_R [S - U_L (T_i - T_a)]$$

- $Q_u$  = useful energy or output of the collector (J/m<sup>2</sup>)
- $F_R$  = heat removal factor
- $A_c$  = collector area (m<sup>2</sup>)
- $S$  = solar energy absorbed by a solar collector (J/m<sup>2</sup>)
- $U_L$  = overall heat loss coefficient between the black plate and the surroundings (W/m<sup>2</sup>C)
- $T_i$  = the fluid inlet temperature
- $T_a$  = the ambient temperature

**(Note:  $QU$  would be 0 if the result of calculation is negative value)**



# Question



The solar energy absorbed by a solar collector  $S$  and the ambient temperatures are given in the table below. The collector has  $U_L = 5.2$   $\text{W/m}^2\text{C}$ ,  $A_c = 1$   $\text{m}^2$  and  $F_R = 0.92$ . Determine the useful output of the collector for the day in the question if the inlet temperature is constant at 35 C.

Hour	$S$ , $\text{MJ/m}^2$	$T_a$ , C	Hour	$S$ , $\text{MJ/m}^2$	$T_a$ , C
7 – 8	0.01	-3	12 – 1	3.42	9
8 – 9	0.40	0	1 – 2	3.21	11
9 – 10	1.90	4	2 – 3	1.54	5
10 – 11	2.85	5	3 – 4	1.07	1
11 – 12	3.02	7	4 – 5	0.52	-4



# Solution



- Identify data given from question:

$$U_L = 5.2 \text{ W/m}^2\text{C}, F_R = 0.92, A_c = 1 \text{ m}^2, T_i = 35^\circ\text{C}$$

- Identify data given from table:

*10 hourly S and T<sub>a</sub> are given, starting 7- 8 a.m.*

*Example: 7 – 8 a.m. S = 0.01 MJ/m<sup>2</sup>, T<sub>a</sub> = -3°C*

- Apply formula to find useful/output energy from collector

$$Q_u = A_c F_R [S - U_L (T_i - T_a)]$$

$$Q_u = 0 \text{ MJ} / \text{m}^2$$





# Solution



Hour	$S$ MJ/m <sup>2</sup>	$T_a$ C	$U_L(T_i - T_a)$ MJ/m <sup>2</sup>	$q_u$ MJ/m <sup>2</sup>
7 – 8	0.01	-3	0.711	0
8 – 9	0.40	0	0.655	0
9 – 10	1.90	4	0.580	1.214
10 – 11	2.85	5	0.562	2.105
11 – 12	3.02	7	0.524	2.296
12 – 1	3.42	9	0.487	2.699
1 – 2	3.21	11	0.449	2.540
2 – 3	1.54	5	0.562	0.900
3 – 4	1.07	1	0.636	0.399
4 – 5	0.52	-4	0.730	0
			SUM	11.080

Hence, useful energy of the collector for the day = 11.080 MJ/m<sup>2</sup>

## H.w



Q1: Design a system for 500LPD for domestic used. The useful output of a solar collectors are  $3 \text{ MJ/m}^2 \text{ h}$  from 10 Am until 3 Pm . The collector has  $U_L = 6.2 \text{ W/m}^2 \text{ }^\circ\text{C}$ , and  $FR = 0.747$ , the inlet temperature is constant at  $35 \text{ }^\circ\text{C}$  and the solar energy absorbed by a solar collector and the ambient temperature are  $S=2.85 \text{ MJ/m}^2 \text{ h}$ ,  $T_a= 2 \text{ }^\circ\text{C}$  respectively. What kind of system you will prefer? How many collectors will you use?

