

# Engineering Mechanics



#### Al-Mustagbal University College

## **Chapter Two: Resultant of Force Systems**

**Resultant:** simplest force system which have same external effect of the original system.

### 2.1 Resultant of Coplanar Concurrent Force System

In x-y plane, the resultant of coplanar concurrent force system where the lines of action of all forces pass through a common point can be found by the following formulas:

$$R_x = \sum F_x \to^+$$

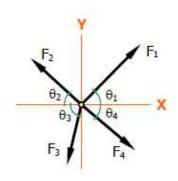
$$R_{x} = F_{1x} - F_{2x} - F_{3x} + F_{4x}$$

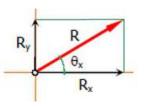
$$R_y = \sum F_y \quad \uparrow^+$$

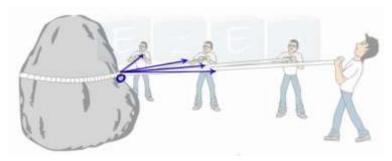
$$R_{\nu} = F_{1\nu} + F_{2\nu} - F_{3\nu} - F_{4\nu}$$

$$R = \sqrt{{R_x}^2 + {R_y}^2}$$

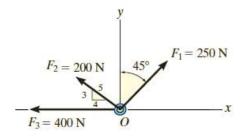
$$\theta_{x} = \tan^{-1}\left(\frac{R_{y}}{R_{x}}\right)$$







**Example No. 1:** Determine the magnitude and direction of the resultant forces system shown in Figure.



#### **Solution:**

$$F_{1x} = 250 \times \sin 45 = 176.8 \, N \rightarrow$$

$$F_{1y} = 250 \times \cos 45 = 176.8 \, N$$
 ↑

$$F_{2x} = 200 \times \frac{4}{5} = 160 \, N \quad \leftarrow$$

$$F_{2y} = 200 \times \frac{3}{5} = 120 \, N \uparrow$$

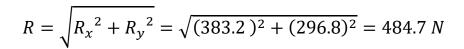
$$F_{3x} = 400 N \leftarrow$$

$$F_{3y} = 0$$

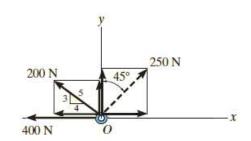
$$\rightarrow^+ R_{\chi} = \sum F_{\chi} = 176.8 - 160 - 400$$

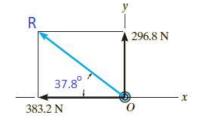
$$R_x = -383.2 N = 383.2 N \leftarrow$$

$$\uparrow^+ R_y = \sum F_y = 176.8 + 120 + 0 = 296.8 \, N \, \uparrow$$

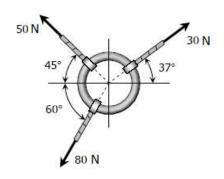


$$\theta_x = \tan^{-1}\left(\frac{R_y}{R_x}\right) = \tan^{-1}\left(\frac{296.8}{383.2}\right) = 37.8^\circ$$





**Example No. 2:** Find the resultant force on the ring due to the three applied forces.



#### **Solution:**

$$\to^+ R_{\chi} = \sum F_{\chi}$$

$$R_x = 30\cos 37 - 50\cos 45 - 80\cos 60$$

$$R_x = -51.40 \ N = 51.40 \ N \leftarrow$$

$$\uparrow^+ R_y = \sum F_y$$

$$R_y = 30\sin 37 + 50\sin 45 - 80\sin 60$$

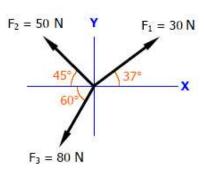
$$R_y = -15.87 N = 15.87 N \downarrow$$

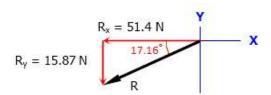
$$R = \sqrt{{R_x}^2 + {R_y}^2} = \sqrt{(51.40)^2 + (15.87)^2}$$

$$R = 53.79 N$$

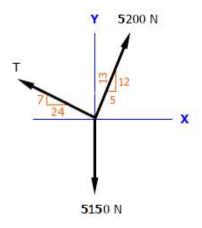
$$\theta_{x} = \tan^{-1} \left( \frac{R_{y}}{R_{x}} \right)$$

$$\theta_x = \tan^{-1}\left(\frac{15.87}{51.40}\right) = 17.16^{\circ}$$





**Example No. 3:** The resultant of the three forces is horizontal. Determine the magnitude of the resultant.



#### **Solution:**

Since the resultant is horizontal, therefore:

$$R_y = 0$$
,  $R = R_x$ 

$$c = \sqrt{24^2 + 7^2} = 25$$

$$\uparrow^+ R_y = \sum F_y$$

$$0 = T \times \frac{7}{25} + 5200 \times \frac{12}{13} - 5150$$

$$\therefore T = 1250 \, N$$

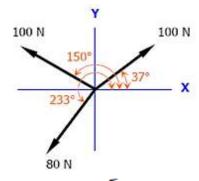
$$\to^+ R_x = R = \sum F_x$$

$$R = -T \times \frac{24}{25} + 5200 \times \frac{5}{13}$$

$$R = 800 N \rightarrow$$

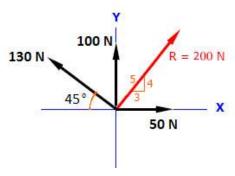
#### **Problems:**

**1.** Determine the magnitude and direction of the resultant forces system shown in Figure.



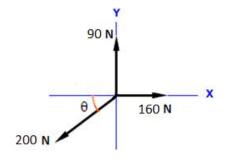
**Answer**:  $R = 71.8 \, N$ ,  $\theta_x = 40.15^{\circ}$ 

**2.** If the resultant of fourth forces is 200 N as shown in figure. Find the unknown for the force.



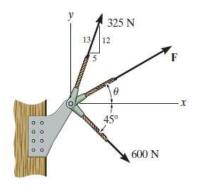
**Answer**:  $F_4 = 165 N$ ,  $\theta_x = 11.153^{\circ}$ 

3. The resultant of the three forces as shown in figure is vertical, determine the angle  $\theta$ , and magnitude of the resultant.



**Answer**:  $R = 30 N \downarrow$ ,  $\theta = 36.87^{\circ}$ 

**4.** If the resultant force acting on the bracket is to be 750 N directed along the positive x - axis, determine the magnitude of **F** and its direction  $\theta$ .



**Answer**:  $F = 236.1 \, N$ ,  $\theta = 31.76^{\circ}$