



كلية المستقبل الجامعة  
قسم هندسة تقنيات البناء والانشاءات



# TWO WAY SOLID SLAB

المرحلة الثالثة

م.م يسار امير علي

## Two way slab

slab must be continuously supported on all four edges

W: uniformly distributed load on slab

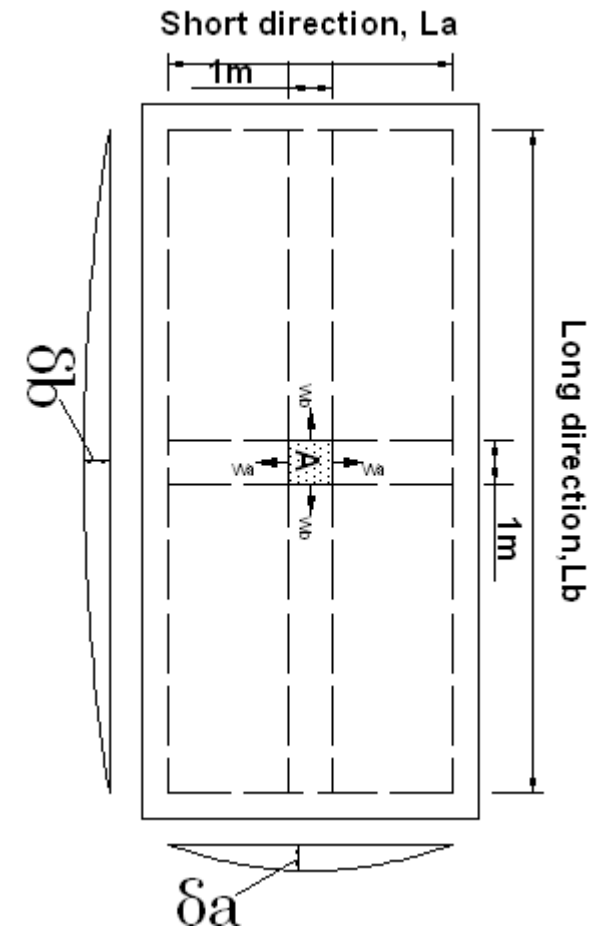
$$\delta = \frac{5W_a \cdot l_a^4}{384E_c I_e} = \frac{5W_b \cdot l_b^4}{384 E_c I_e}$$

$$\frac{W_a}{W_b} = \left(\frac{l_b}{l_a}\right)^4$$

$$W = W_a + W_b \dots \dots \dots (1)$$

let aspect ratio of slab

$$\frac{l_b}{l_a} = 2$$



$$\frac{W_a}{W_b} = (2)^4 = 16 \dots \dots \dots (2)$$

solve eq 1) and eq 2) we get

$$W_a = \frac{16}{17} W = 0.94 W$$

$$W_b = \frac{1}{17} W = 0.06 W$$

If  $\frac{l_b}{l_a} \geq 2.0$  Design as one way slab

If  $\frac{l_b}{l_a} < 2.0$  Design as two way slab

## Two way solid slab design

### Method 3

coefficient method (ACI code 1963 elastic)

Design middle strip design for  $M_1$  and  $M_2$

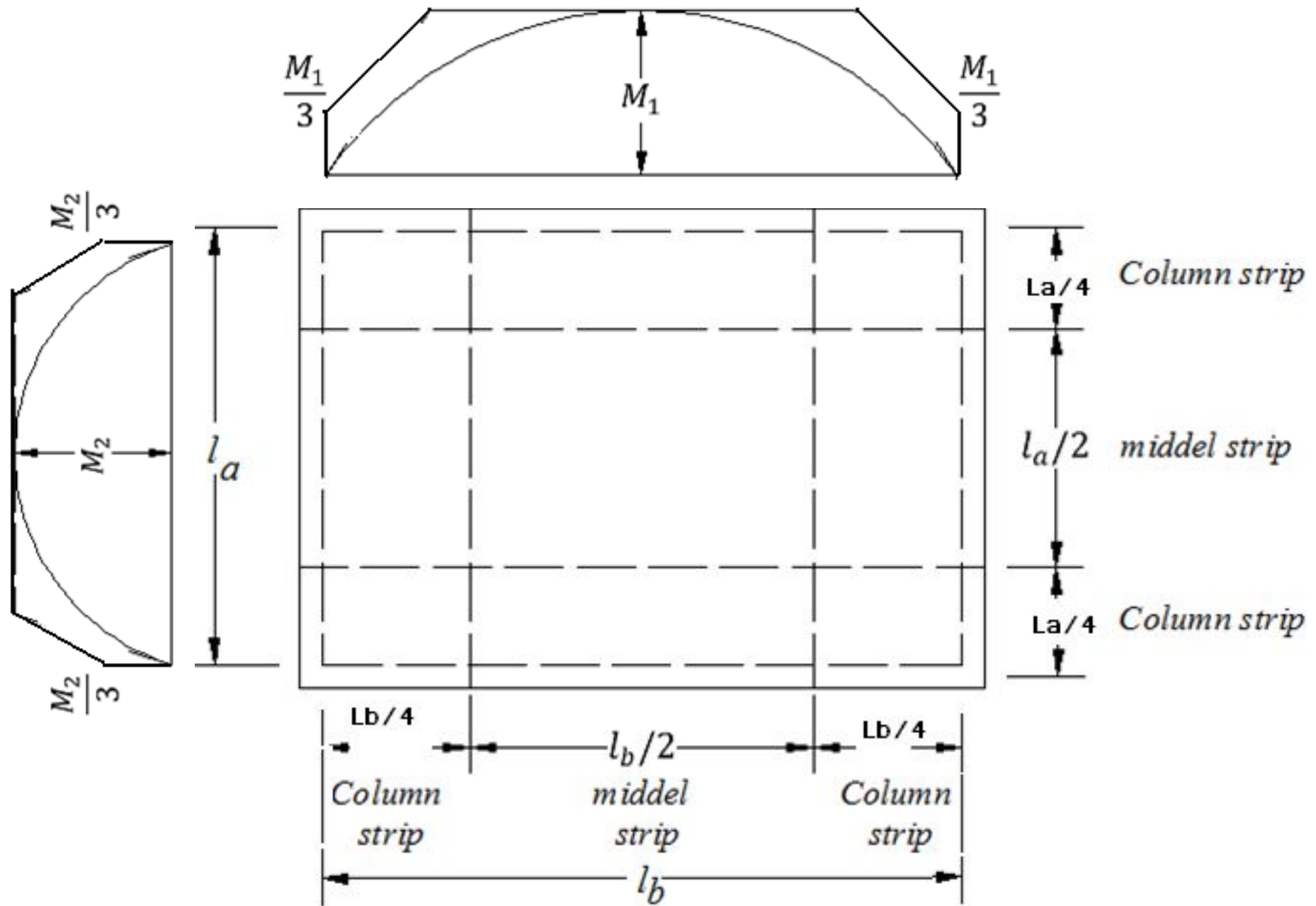
Design column strip design for  $\frac{1}{2} \left( M_1 + \frac{M_1}{3} \right) = \frac{2}{3} M_1$

As we find ( $A_s$ ) and ( $S$ ) for middle strip  $\rightarrow$

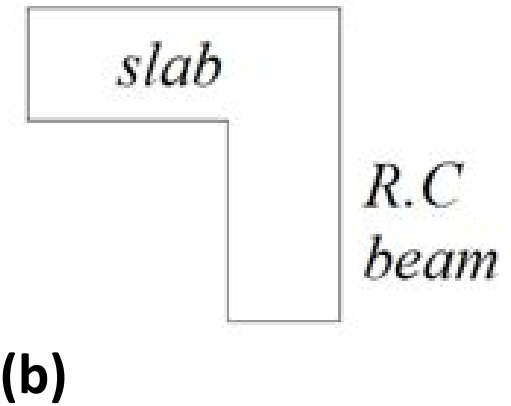
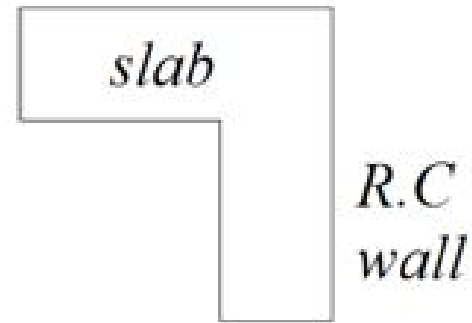
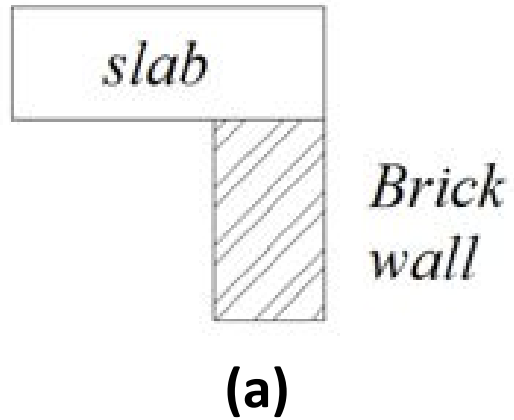
$$A_{s_{column\ strip}} = \frac{2}{3} A_{s_{middle\ strip}}$$


$$S_{column\ strip} = \frac{3}{2} S_{middle\ strip}$$

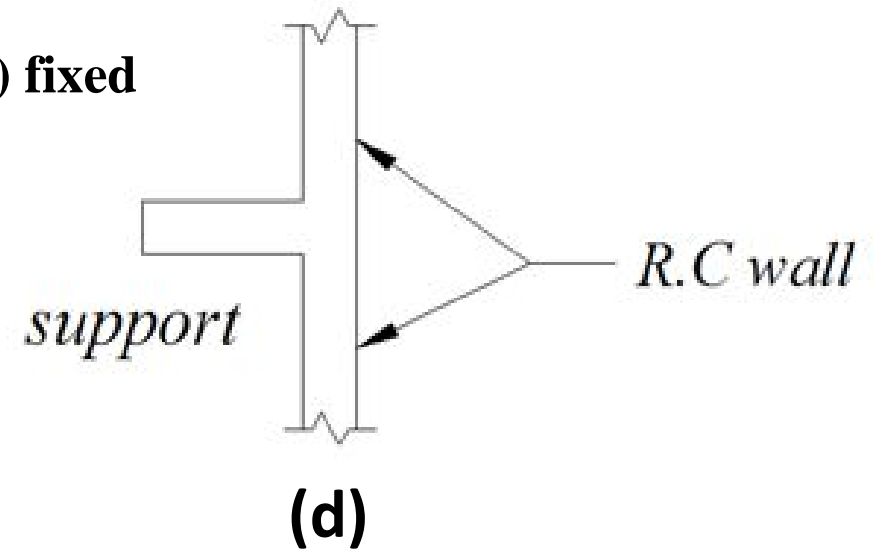
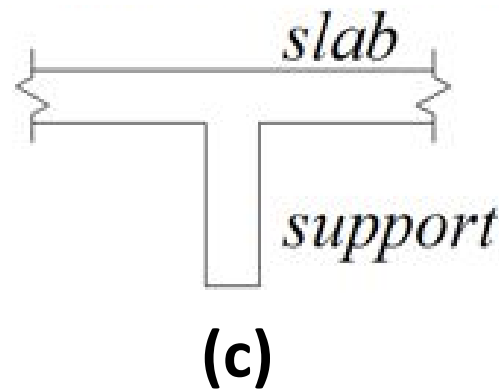
Aspect ratio  $l_a/l_b = (1.0 \leftrightarrow 0.5)$



|(a)discontinuous slab or (b)supporting have small torsional resistance



 (c) slab is continuous a cross support (d) fixed



			7
7	9	9	8
	8	2	8
	4	9	4

Table 8.3 coefficients for negative moment in slabs

$$M_a = (C_a) \cdot W \cdot L_a^2$$

$$M_b = (C_b) \cdot W \cdot L_b^2$$

Where W = total uniform live load plus live load

Ratio m = l <sub>a</sub> /l <sub>b</sub>		Case1	Case2	Case3	Case4	Case5	Case6	Case7	Case8	Case9
1.00	Ca-		.045		.050	.075	.071		.033	.061
	Cb-		.045	.076	.050			.071	.061	.033
0.95	Ca-		.050		.055	.079	.075		.038	.065
	Cb-		.041	.072	.045			.067	.056	.029
0.90	Ca-		.055		.060	.080	.079		.043	.068
	Cb-		.037	.070	.040			.062	.052	.025
0.85	Ca-		.060		.066	.082	.083		.049	.072
	Cb-		.031	.065	.034			.057	.046	.021
0.80	Ca-		.065		.071	.083	.086		.055	.075
	Cb-		.027	.061	.029			.051	.041	.017
0.75	Ca-		.069		.076	.085	.088		.061	.078
	Cb-		.022	.056	.024			.044	.036	.014
0.70	Ca-		.074		.081	.086	.091		.068	.081
	Cb-		.017	.050	.019			.038	.029	.011
0.65	Ca-		.077		.085	.087	.093		.074	.083
	Cb-		.014	.043	.015			.031	.024	.008
0.60	Ca-		.081		.089	.088	.095		.080	.085
	Cb-		.010	.035	.011			.024	.018	.006
0.55	Ca-		.084		.092	.089	.096		.085	.086
	Cb-		.007	.028	.008			.019	.014	.005
0.50	Ca-		.086		.094	.090	.097		.089	.088
	Cb-		.006	.022	.006			.014	.010	.003



Table 8.4 coefficients for dead load positive moment in slabs

$$M_{a+.dL} = (C_a + .dL) * W_d * L_a^2$$

$$M_{b+.dL} = (C_b + .dL) * W_d * L_b^2$$

Where  $W_d$  = total uniform dead load

Ratio $m=l_a/l_b$		Case1	Case2	Case3	Case4	Case5	Case6	Case7	Case8	Case9
1.00	Ca.d1	.036	.018	.018	.027	.027	.033	.027	.020	.023
	Cb.d1	.036	.018	.027	.027	.018	.027	.033	.023	.020
0.95	Ca.d1	.040	.020	.021	.030	.028	.036	.031	.022	.024
	Cb.d1	.033	.016	.025	.024	.015	.024	.031	.021	.017
0.90	Ca.d1	.045	.022	.025	.033	.029	.039	.035	.025	.026
	Cb.d1	.029	.014	.024	.022	.013	.021	.028	.019	.015
0.85	Ca.d1	.050	.024	.029	.036	.031	.042	.040	.029	.028
	Cb.d1	.026	.012	.022	.019	.011	.017	.025	.017	.013
0.80	Ca.d1	.056	.026	.034	.039	.032	.045	.045	.032	.029
	Cb.d1	.023	.011	.020	.016	.009	.015	.022	.015	.010
0.75	Ca.d1	.061	.028	.040	.043	.033	.048	.051	.036	.031
	Cb.d1	.019	.009	.018	.013	.007	.012	.020	.013	.007
0.70	Ca.d1	.068	.030	.046	.046	.035	.051	.058	.040	.033
	Cb.d1	.016	.007	.016	.011	.005	.009	.017	.011	.006
0.65	Ca.d1	.074	.032	.054	.050	.036	.054	.065	.044	.034
	Cb.d1	.013	.006	.014	.009	.004	.007	.014	.009	.005
0.60	Ca.d1	.081	.034	.062	.053	.037	.056	.073	.048	.036
	Cb.d1	.010	.004	.011	.007	.003	.006	.012	.007	.004
0.55	Ca.d1	.088	.035	.071	.056	.038	.058	.081	.052	.037
	Cb.d1	.008	.003	.009	.005	.002	.004	.009	.005	.003
0.50	Ca.d1	.095	.037	.080	.059	.039	.061	.089	.056	.038
	Cb.d1	.006	.002	.007	.004	.001	.003	.007	.004	.002



Table 8.5 coefficients for live load positive moment in slabs

$$M_{a+.LL} = (C_{a+.LL}) * WL * L_a^2$$

$$M_{b+.LL} = (C_{b+.LL}) * WL * L_b^2$$

Where WL = total uniform live load

Ratio $m=l_a/l_b$		Case1	Case2	Case3	Case4	Case5	Case6	Case7	Case8	Case9
1.00	$C_{a+.LL}$	.036	.027	.027	.032	.032	.035	.032	.028	.030
	$C_{b+.LL}$	.036	.027	.032	.032	.027	.032	.035	.030	.028
0.95	$C_a$	.040	.030	.031	.035	.034	.038	.036	.031	.032
	$C_b$	.033	.025	.029	.029	.024	.029	.032	.027	.025
0.90	$C_a$	.045	.034	.035	.039	.037	.042	.040	.035	.036
	$C_b$	.029	.022	.027	.026	.021	.025	.029	.024	.022
0.85	$C_a$	.050	.037	.040	.043	.041	.046	.045	.040	.039
	$C_b$	.026	.019	.024	.023	.019	.022	.026	.022	.020
0.80	$C_a$	.056	.041	.045	.048	.044	.051	.051	.044	.042
	$C_b$	.023	.017	.022	.020	.016	.019	.023	.019	.017
0.75	$C_a$	.061	.045	.051	.052	.047	.055	.056	.049	.046
	$C_b$	.019	.014	.019	.016	.013	.016	.020	.016	.013
0.70	$C_a$	.068	.049	.057	.057	.051	.060	.063	.054	.050
	$C_b$	.016	.012	.016	.014	.011	.013	.017	.014	.011
0.65	$C_a$	.074	.053	.064	.062	.055	.064	.070	.059	.054
	$C_b$	.013	.010	.014	.011	.009	.010	.014	.011	.009
0.60	$C_a$	.081	.058	.071	.067	.059	.068	.077	.065	.059
	$C_b$	.010	.007	.011	.009	.007	.008	.011	.009	.007
0.55	$C_a$	.088	.062	.080	.072	.063	.073	.085	.070	.063
	$C_b$	.008	.006	.009	.007	.005	.006	.009	.007	.006
0.50	$C_a$	.095	.066	.088	.077	.067	.078	.092	.076	.067
	$C_b$	.006	.004	.007	.005	.004	.005	.007	.005	.004



TABLE 8.0 RATIO OF LOAD  $w$  IN  $l_a$ ,  $l_b$  DIRECTIONS FOR SHEAR IN SLAB <sup>and</sup> <sub>load</sub> <sub>on</sub> supports

Ratio $m=l_a/l_b$		Case1	Case2	Case3	Case4	Case5	Case6	Case7	Case8	Case9
1.00	Wa	.50	.50	.17	.50	.83	.71	.29	.33	.67
	Wb	.50	.50	.83	.50	.17	.29	.71	.67	.33
0.95	Wa	.55	.55	.20	.55	.86	.75	.33	.38	.71
	Wb	.45	.45	.80	.45	.14	.25	.67	.62	.29
0.90	Wa	.60	.60	.23	.60	.88	.79	.38	.43	.75
	Wb	.40	.40	.77	.40	.12	.21	.62	.57	.25
0.85	Wa	.66	.66	.28	.66	.90	.83	.43	.49	.79
	Wb	.34	.34	.72	.34	.10	.17	.57	.51	.21
0.80	Wa	.71	.71	.33	.71	.92	.86	.49	.55	.83
	Wb	.29	.29	.67	.29	.08	.14	.51	.45	.17
0.75	Wa	.76	.76	.39	.76	.94	.88	.56	.61	.86
	Wb	.24	.24	.61	.24	.06	.12	.44	.39	.14
0.70	Wa	.81	.81	.45	.81	.95	.91	.62	.68	.89
	Wb	.19	.19	.55	.19	.05	.09	.38	.32	.11
0.65	Wa	.85	.85	.53	.85	.96	.93	.69	.74	.92
	Wb	.15	.15	.47	.15	.04	.07	.31	.26	.08
0.60	Wa	.89	.89	.61	.89	.97	.95	.76	.80	.94
	Wb	.11	.11	.39	.11	.03	.05	.24	.20	.06
0.55	Wa	.92	.92	.69	.92	.98	.96	.81	.85	.95
	Wb	.08	.08	.31	.08	.02	.04	.19	.15	.05
0.50	Wa	.94	.94	.76	.94	.99	.97	.86	.89	.97
	Wb	.06	.06	.24	.06	.01	.03	.14	.11	.03

## Table 8.3 Negative moment (total load)

$$M_a = C_a^- W_u l_a^2$$

$$M_b = C_b^- W_u l_b^2$$

$$W_u = 1.2 * W_d + 1.6 W_l$$

$$d_s = t - 25\text{mm}$$

$$d_l = d_s - 10 \text{ mm}$$

## Table 8.4 positive moment (for dead load)

$$M_a^+ = C_{a_{DL}}^+ W_{uDL} l_a^2$$

$$M_b^+ = C_{b_{DL}}^+ W_{uDL} l_b^2$$

## Table 8.5 positive moment (for live load)

$$M_a^+ = C_{a_{LL}}^+ W_{uLL} l_a^2$$

$$M_b^+ = C_{b_{LL}}^+ W_{uLL} l_b^2$$

Total positive moment

$$\text{Total } M_a^+ = C_{a_{DL}}^+ W_{uDL} l_a^2 + C_{a_{LL}}^+ W_{uLL} l_a^2$$

$$\text{Total } M_b^+ = C_{b_{DL}}^+ W_{uDL} l_b^2 + C_{b_{LL}}^+ W_{uLL} l_b^2$$

$$\text{Total } M_a^+ = (C_{a_{DL}}^+ W_{uDL} + C_{a_{LL}}^+ W_{uLL}) l_a^2$$

$$\text{Total } M_b^+ = (C_{b_{DL}}^+ W_{uDL} + C_{b_{LL}}^+ W_{uLL}) l_b^2$$

## Table 8.6 (Ratio of load in $l_a$ , $l_b$ direction)

To find

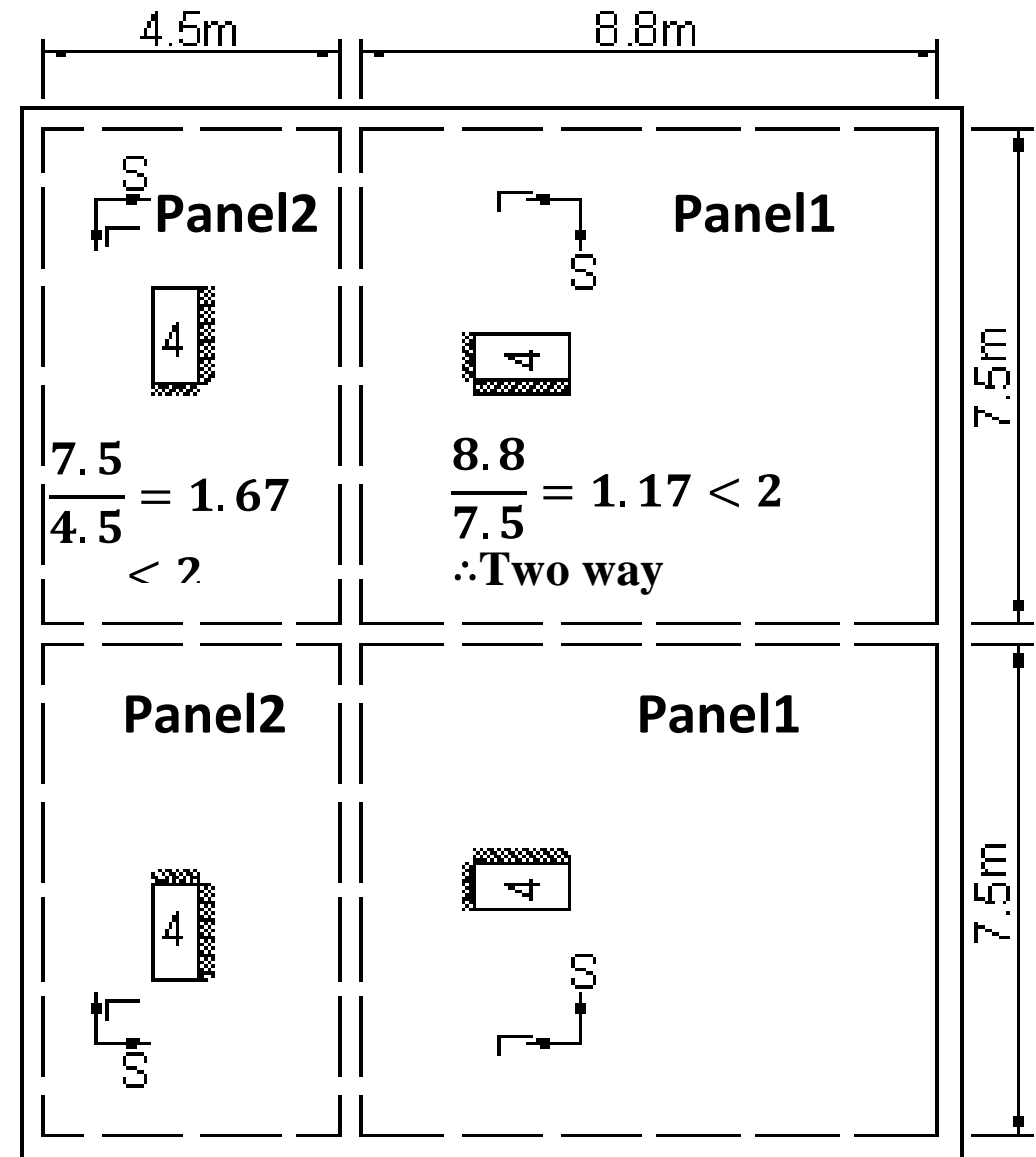
$W_a$  → to check shear

$W_b$  and load transferred to beam.

**Example :**  $f_c' = 30 \text{ MPa}$ ,  $f_y = 400 \text{ MPa}$ ,  $W_{1.1} = 5 \text{ kN/m}^2$ , all supports are R.C beams .Design floor slab.

## Solution

$$\begin{aligned}
 t &= \frac{\text{Perimeter}}{180} \\
 &= \frac{(8.8 + 7.5) * 2}{180} \\
 &= 0.181 \rightarrow \text{use } t \\
 &= 190 \text{ mm}
 \end{aligned}$$



## Dead load

$$\text{Slab weight} = 0.19 * 24.5 = 4.66 \frac{\text{kN}}{\text{m}^2}$$

$$\text{tiling with moetar} = 0.04 * 24.5 = 0.98 \frac{\text{kN}}{\text{m}^2}$$

$$\text{plastring} = 0.48 \frac{\text{kN}}{\text{m}^2}$$

$$\Sigma \text{D.L} = 6.12 \frac{\text{kN}}{\text{m}^2}$$

$$W_u = 1.2 * W_d + 1.6 W_l = 1.2 * 6.12 + 1.6 * 5 = 15.34 \frac{\text{kN}}{\text{m}^2}$$

$$d_s = t - 25 = 165\text{mm}$$

$$d_l = d_s - 10 = 155\text{mm}$$



panel	direction	C <sup>-</sup>	C <sub>+H</sub>	C <sub>+D</sub>	M <sup>-</sup>	M <sup>+</sup>	R <sup>-</sup>	R <sup>+</sup>	$\omega^-$	$\omega^+$	$\bar{\rho} = \omega$ $\ast \frac{f'c'}{fy}$	$\rho^+$	As <sub>-</sub>	As <sub>+</sub>
Case 4 m=4.5 =7.5 0.6	Short L=4.5 m d <sub>s</sub> =165 mm	0.089	0.067	0.053	27.65→ 36	18.75	0.0489	0.0254	0.0505	0.026	0.0038	0.00195	625	322→ 342
	Long L=7.5 m d <sub>s</sub> =155 mm	0.011	0.009	0.007	9.49	6.94	0.01463	0.0107	0.0145	0.011	0.00109	0.00082	169→ 342	128→ 342
Case 4 m=7.5 =8.8 0.85	Short L=7.5 m d <sub>s</sub> =165 mm	0.066	0.043	0.036	56.95	34.22	0.0775	0.0465	0.0810	0.048	0.00607	0.0036	1002	594
	Long L=8.8 m d <sub>s</sub> =155 mm	0.034	0.023	0.019	40.4→36	25	0.0555	0.0385	0.0575	0.0395	0.0043	0.00296	668	459
									$\wedge$ max	$\wedge$ max				

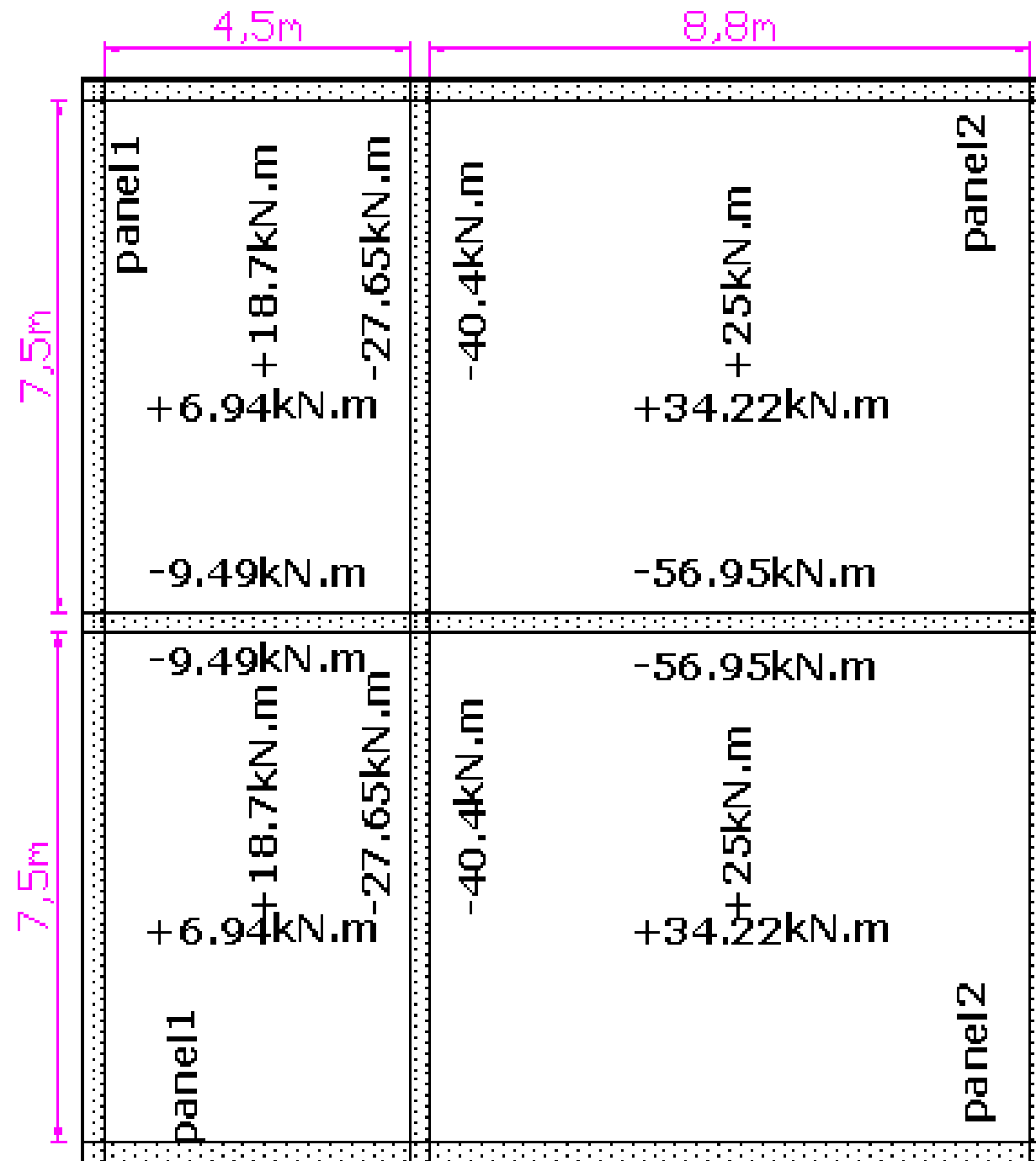
$$M^-_{\text{short}} = C_{-}W_u l_n^2 = 0.089 * 15.34 * (4.5)^2 = 27.65 \text{ kN.m}$$

$$M^-_{\text{long}} = 0.011 * 15.34 * (7.5)^2 = 9.49 \text{ kN.m}$$

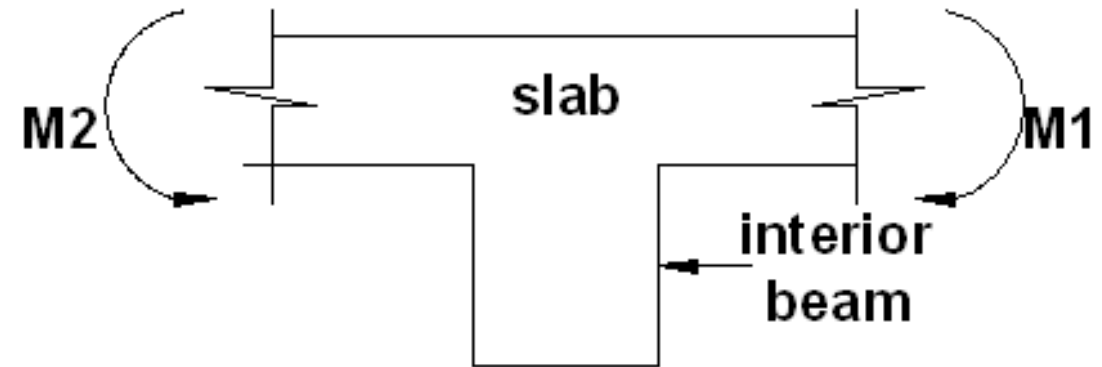
$$M^+ = (C_{+D} 1.2W_d + C_{+L} * 1.6 * W_l) l_n^2$$

$$M^+_{\text{short}} = (0.053 * 1.2 * 6.12 + 0.067 * 1.6 * 5) * (4.5)^2 \\ = 18.75 \text{ kN.m}$$

$$M^+_{\text{long}} = (0.007 * 1.2 * 6.12 + 0.009 * 1.6 * 5) * (7.5)^2 \\ = 6.94 \text{ kN.m}$$



$$M1 > M2$$

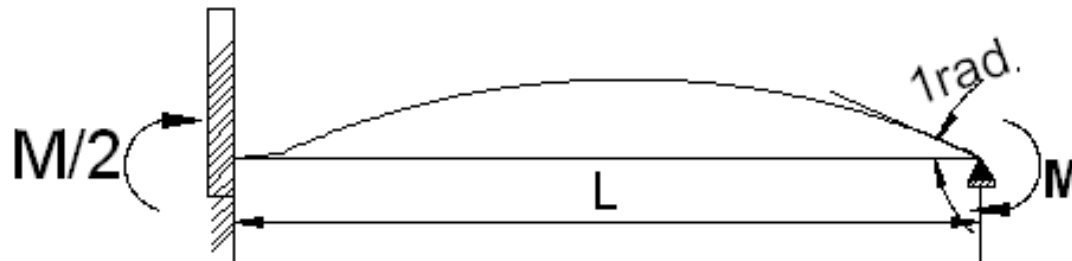


if  $\frac{M2}{M1} \geq 0.8 \rightarrow$  design for max. moment

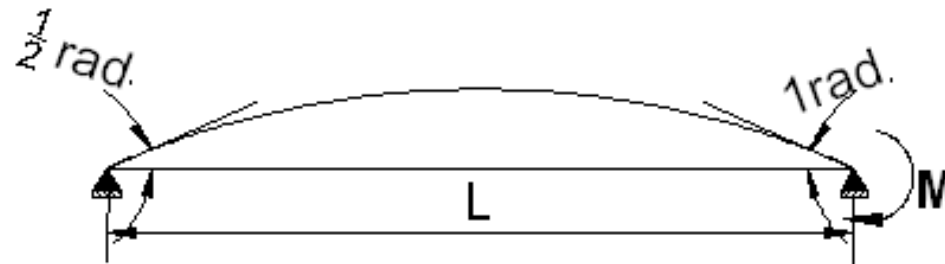
if  $\frac{M2}{M1} < 0.8 \rightarrow$  redistribute the difference between  $M1$  &  $M2$  in

accordance with the relative flexural stiffness of the panels.

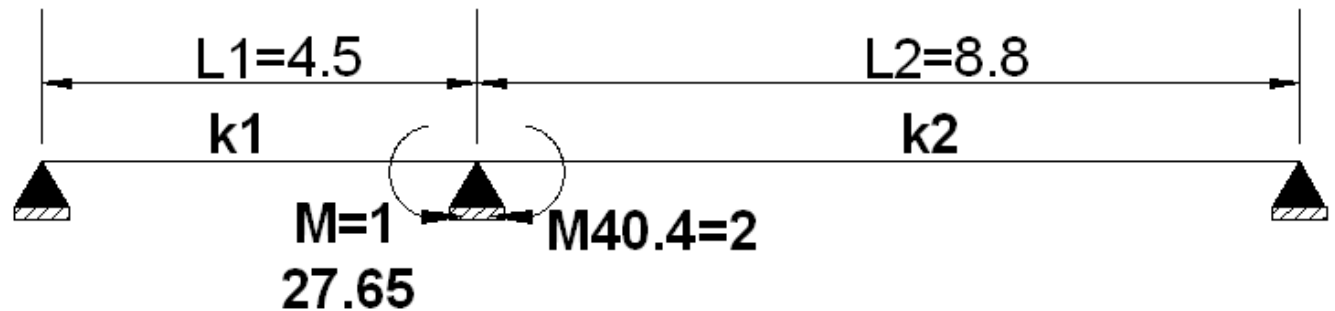
# flexural stiffness



$$M = k(\text{flexural stiffness}) = \frac{4EI}{L}$$



$$M = k(\text{flexural stiffness}) = \frac{3EI}{L}$$



$$\frac{M1}{M2} = \frac{27.65}{40.4} = 0.65 < 0.8 \rightarrow$$

$\therefore$  redistribute the – ve moments

$$\overline{k1} = \text{relative stiffness of panel 1} = \frac{k1}{k1 + k2}$$

$$= \frac{\frac{3EI}{L1}}{\frac{3EI}{L1} + \frac{3EI}{L2}} = \frac{L2}{L1 + L2} = \frac{8.8}{4.5 + 8.8} = 0.66$$

$$\bar{k}_2 = \text{relative stiffness of panel 2} = \frac{k_2}{k_1 + k_2} = 0.34$$

$$M = M_1 + \bar{k}_1 \Delta M = 27.65 + 0.66(40.4 - 27.65) = 36 \text{ kN.m}$$

$$\begin{aligned} \text{OR } M &= M_2 - \bar{k}_2 \Delta M = 40.4 + 0.34(40.4 - 27.65) \\ &= 36 \text{ kN.m} \end{aligned}$$

Let  $\phi=0.9$  to be check later

$$R = \frac{Mu}{\phi f_c' b d^2} = \frac{36}{0.9 * 30000 * 1 * 0.165^2} = 0.0489$$

$$\omega_{max} = 0.364\beta_1 = 0.364 * 0.83 = 0.302 \rightarrow \text{all } \omega$$

$$< \omega_{max} \text{ O.K}$$

$$\rho = \omega \frac{f_y}{f_c'}$$



$$\rho_t = 0.85\beta_1 \frac{f_c'}{f_y} \frac{\epsilon_{cu}}{\epsilon_{cu} + 0.005}$$

$$= 0.85 * .83 * \frac{30}{400} * \frac{0.003}{0.003 + 0.005} = 0.198 \rightarrow \text{all } \rho < \rho_t$$

$\rightarrow \therefore \phi = 0.9 \text{ O.K}$

for  $f_y = 400 \text{ MPa}$ ,  $A_{s_{min}} = 0.0018bt$

$$= 0.0018 * 1000 * 190 = 342 \text{ mm}^2 / \text{m}_{width}$$

$S_{max}$

$$= \min(3t = 3 * 190$$

$$= 570 \text{ mm}, 450 \text{ mm}) \text{ code 1963 method 3}$$

$$S_{max}$$

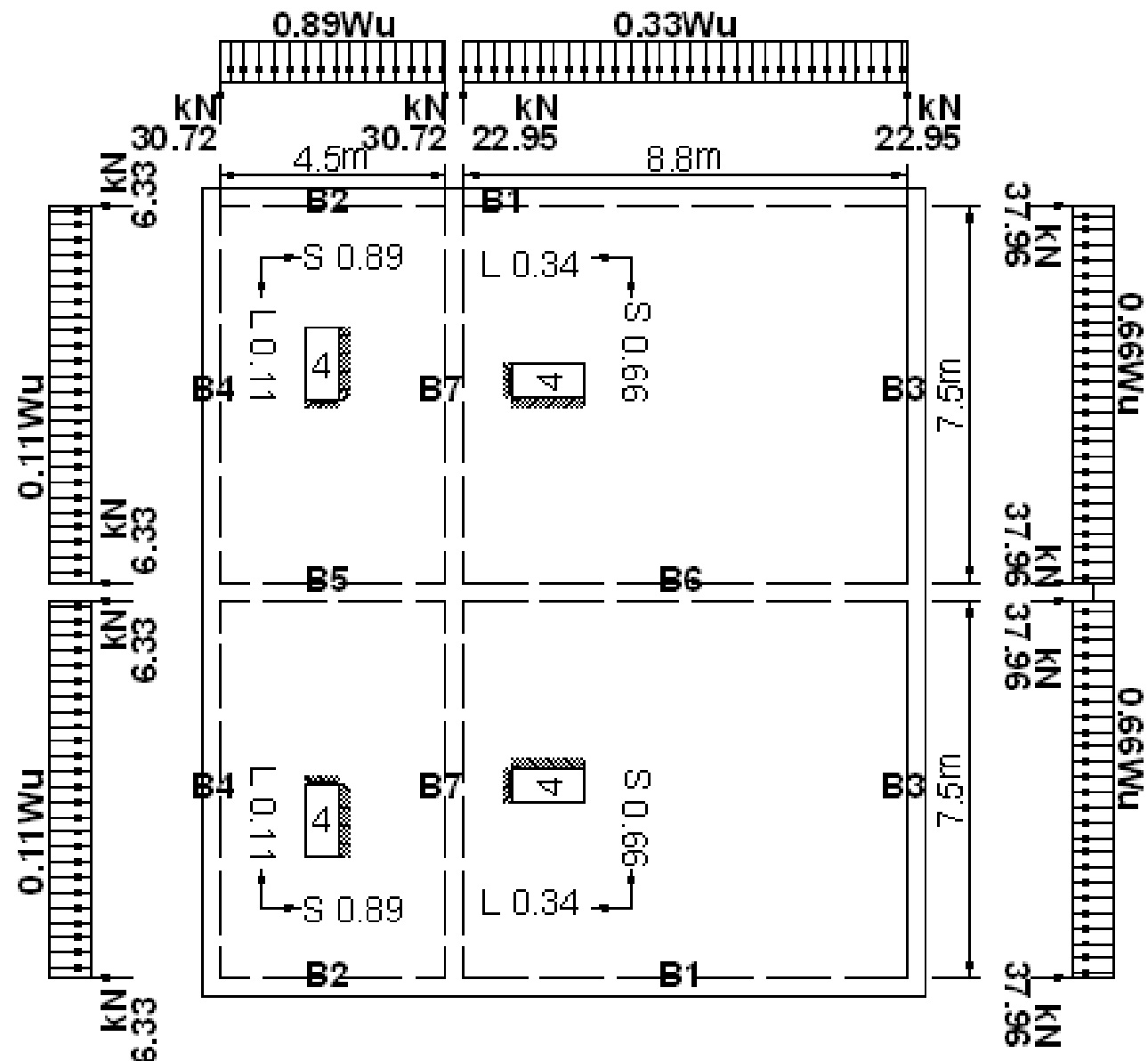
$$= \min(2t = 2 * 190$$

$$= 380\text{mm}, 500\text{mm}) \text{ code 2002 direct design method, ACI 13.3.2}$$

$$\therefore S_{max} = 400\text{mm}$$

$$A_{s_{col.strip}} = \frac{2}{3} A_{s_{middle strip}} \rightarrow S_{col.strip} = \frac{3}{2} S_{middle strip}$$

# Check shear capacity



Max. reaction( $V_u$ )=37.96kN

$$V_{ud}=37.96-0.66*15.34*0.165=36.29\text{kN}$$

$$V_c = 0.17\sqrt{30} * 1.0 * 0.165 = 0.153\text{MN}$$

$$\frac{V_{ud}}{\phi} = \frac{36.29}{0.75} = 48.38\text{kN} < V_c \text{ OK}$$

## Load transferred to beams

- Elastic stage:

$$B1 \left\{ \begin{array}{l} Wd = 0.66 * 6.12 * \frac{7.5}{2} = 15.15 \frac{kN}{m} \rightarrow 17.42 \frac{kN}{m} \\ Wl = 0.66 * 5 * \frac{7.5}{2} = 12.37 \frac{kN}{m} \rightarrow 14.23 \frac{kN}{m} \end{array} \right.$$

$$B2 \left\{ \begin{array}{l} Wd = 0.11 * 6.12 * \frac{7.5}{2} = 2.52 \frac{kN}{m} \rightarrow 9.18 \frac{kN}{m} \\ Wl = 0.11 * 5 * \frac{7.5}{2} = 2.06 \frac{kN}{m} \rightarrow 7.5 \frac{kN}{m} \end{array} \right.$$

$$B3 \begin{cases} Wd = 0.34 * 6.12 * \frac{8.8}{2} = 9.15 \frac{kN}{m} \rightarrow 15.3 \frac{kN}{m} \\ Wl = 0.34 * 5 * \frac{8.8}{2} = 7.48 \frac{kN}{m} \rightarrow 12.5 \frac{kN}{m} \end{cases}$$

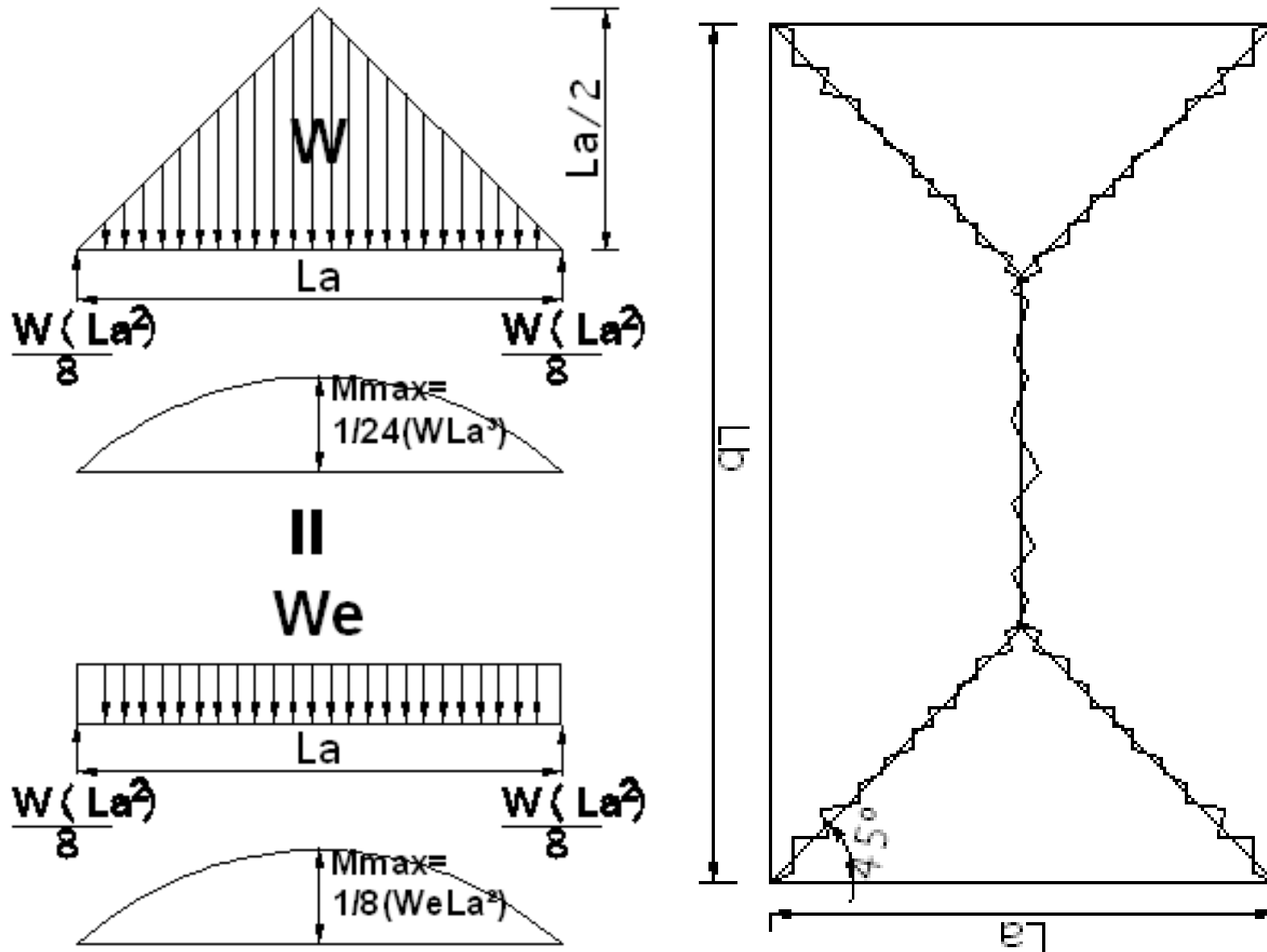
$$B4 \begin{cases} Wd = 0.89 * 6.12 * \frac{4.5}{2} = 12.25 \frac{kN}{m} \\ Wl = 0.89 * 5 * \frac{4.5}{2} = 10.01 \frac{kN}{m} \end{cases}$$

$$B5 \begin{cases} Wd = \left( 0.11 * 6.12 * \frac{7.5}{2} \right) * 2 = 5.49 \frac{kN}{m} \rightarrow 18.36 \frac{kN}{m} \\ Wl = \left( 0.11 * 5 * \frac{7.5}{2} \right) * 2 = 4.12 \frac{kN}{m} \rightarrow 15 \frac{kN}{m} \end{cases}$$

$$B6 \left\{ \begin{array}{l} Wd = \left( 0.66 * 6.12 * \frac{7.5}{2} \right) * 2 = 30.29 \frac{kN}{m} \rightarrow 34.85 \frac{kN}{m} \\ Wl = \left( 0.66 * 5 * \frac{7.5}{2} \right) = 24.75 \frac{kN}{m} \rightarrow 28.46 \frac{kN}{m} \end{array} \right.$$

$$B7 \left\{ \begin{array}{l} Wd = 0.34 * 6.12 * \frac{8.8}{2} + 0.89 * 6.12 * \frac{4.5}{2} = 21.41 \frac{kN}{m} \rightarrow 27.42 \frac{kN}{m} \\ Wl = 0.34 * 5 * \frac{8.8}{2} + 0.89 * 5 * \frac{4.5}{2} = 17.5 \frac{kN}{m} \rightarrow 22.4 \frac{kN}{m} \end{array} \right.$$

- Loads transferred to beams at failure stage of slab





$$\left(\frac{W_e l a^2}{8}\right) = \left(\frac{W l a^3}{24}\right) \rightarrow W_e = \frac{W l a}{3} \text{ short panel}$$

$$W_e = \frac{W l a}{3} \left(\frac{3 - m^2}{2}\right), \quad m = \frac{l a}{l b} \text{ long panel}$$

$$B1 = \begin{cases} W_{ed} = \frac{6.12 * 7.5}{3} \left(\frac{3 - 0.85^2}{2}\right) = 17.42 \frac{kN}{m} \\ W_{el} = \frac{5 * 7.5}{3} \left(\frac{3 - 0.85^2}{2}\right) = 14.23 \frac{kN}{m} \end{cases}$$

$$B2 = \begin{cases} W_{ed} = \frac{6.12 * 4.5}{3} = 9.18 \frac{kN}{m} \\ W_{el} = \frac{5 * 4.5}{3} = 7.5 \frac{kN}{m} \end{cases}$$

$$B3 = \begin{cases} W_{ed} = \frac{6.12 * 7.5}{3} = 15.3 \frac{kN}{m} \\ W_{el} = \frac{5 * 7.5}{3} = 12.5 \frac{kN}{m} \end{cases}$$

$$B4 = \begin{cases} W_{ed} = \frac{6.12 * 4.5}{3} \left( \frac{3 - 0.6^2}{2} \right) = 12.12 \frac{kN}{m} \\ W_{el} = \frac{5 * 4.5}{3} \left( \frac{3 - 0.6^2}{2} \right) = 9.9 \frac{kN}{m} \end{cases}$$

$$B5 = \begin{cases} W_{ed} = \left( \frac{6.12 * 4.5}{3} \right) * 2 = 18.36 \frac{kN}{m} \\ W_{el} = \left( \frac{5 * 4.5}{3} \right) * 2 = 15 \frac{kN}{m} \end{cases}$$

$$B6 = \begin{cases} W_{ed} = \left[ \frac{6.12 * 7.5}{3} \left( \frac{3 - 0.85^2}{2} \right) \right] * 2 = 34.85 \frac{kN}{m} \\ W_{el} = \left[ \frac{5 * 7.5}{3} \left( \frac{3 - 0.85^2}{2} \right) \right] * 2 = 28.46 \frac{kN}{m} \end{cases}$$

$$B7 = \begin{cases} W_{ed} = \frac{6.12 * 7.5}{3} + \frac{6.12 * 4.5}{3} \left( \frac{3 - 0.6^2}{2} \right) = 27.42 \frac{kN}{m} \\ W_{el} = \frac{5 * 7.5}{3} + \frac{5 * 4.5}{3} \left( \frac{3 - 0.6^2}{2} \right) = 22.4 \frac{kN}{m} \end{cases}$$

Bent and cut off points in two way slab(approximate values):

Bent:  $L_n/6$  from face of support

Cut off:  $L_n/4$  from face of support

<p>Panel 1 Long dir. Middle Strip</p>	<p><math>A_s^+ = 342\text{mm}^2</math>, use <math>\text{Ø}10@225\text{mm}(2b, 1s)</math>  <math>\langle S_{\text{max.}} \rangle = 349\text{mm}^2 &gt; A_s^+ = 342\text{mm}^2</math>  At discontinuous edge: <math>\text{Ø}10@225(2b)</math>  <math>\rightarrow 2/3 * 349 = 232\text{mm}^2 &lt; A_{s_{\text{min}}}</math> add(<math>\text{Ø}8@450 = 111\text{mm}^2</math>)  <math>S_{\text{av}} = (225 + 450)/2 = 337\text{mm} &lt; S_{\text{max}}</math> OK</p>
	<p><math>A_{s_{\text{req}}}^- = 342\text{mm}^2 &lt; A_{s_{\text{prov}}}^- = (2/3 * 349) * 2 = 465\text{mm}^2</math> OK</p>

<p>Panel 1 Long dir. Column Strip</p>	<p>Since <math>A_{s_{\text{min}}}</math> control for middle strip, therefore, the reinforcement distribution will be fixed for column strip</p>
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<p>Panel 2 Short dir. Middle Strip</p>	<p><math>A_s^+ = 594\text{mm}^2</math>, use <math>\text{Ø}12 @ 175\text{mm}((2b, 1s)</math>  <math>\langle S_{\text{max.}} \rangle = 646\text{mm}^2 &gt; A_s^+ = 594\text{mm}^2</math>  At discontinuous edge: <math>\text{Ø}12 @ 175(2b)</math>  <math>\rightarrow 2/3 * 646 = 430\text{mm}^2 &gt; A_{s_{\text{min}}}</math> OK  Spacing (175, 350mm) <math>\langle S_{\text{max}}</math> OK</p>
	<p><math>A_{s_{\text{req}}}^- = 1002\text{mm}^2</math>    <math>A_{s_{\text{prov}}}^- = (2/3 * 646) * 2 = 861\text{mm}^2 &lt; A_s^-</math>  <math>= 1002\text{mm}^2</math>  <math>A_{s_{\text{add}}}^- = 1002 - 861 = 141\text{mm}^2</math> (use  <math>\text{Ø}8 @ 350 = 143\text{mm}^2 &gt; 141\text{mm}^2</math>)</p>

<p>Panel 2 Short dir. Column Strip</p>	<p> <math>A_s^+_{req} = 2/3 * 594 = 396 \text{mm}^2 &gt; A_{s_{min}}</math>,  use <math>\text{Ø}12 @ 3/2 * 175 = 260 \text{mm} ((2b, 1s) &lt; S_{max.}) = 435 \text{mm}^2 &gt;</math>  <math>A_s^+ = 396 \text{mm}^2</math> OK  At discontinuous edge: <math>\text{Ø}12 @ 260(2b)</math>  <math>\rightarrow 2/3 * 435 = 290 \text{mm}^2 &lt; A_{s_{min}}</math>  <math>A_{s_{add}} = 342 - 290 = 52 \text{mm}^2</math> (use  <math>\text{Ø}8 @ 780 = 64 \text{mm}^2 &gt; 52 \text{mm}^2</math>)  <math>S_{av} = (260 + 520 \text{mm}) / 2 = 390 \text{mm} &lt; S_{max}</math> OK </p>
	<p> <math>A_s^-_{req} = 2/3 * 1002 = 668 \text{mm}^2</math>    <math>A_s^-_{prov} =</math>  <math>(2/3 * 435) * 2 = 580 \text{mm}^2 &lt; A_s^- = 668 \text{mm}^2</math> </p>

$$A_{s_{add}} = 668 - 580 = 88 \text{mm}^2 \text{ (use } \emptyset 8 @ 520 = 96 \text{mm}^2 > 88 \text{mm}^2 \text{)}$$

Panel  
1  
Short  
dir.  
Middle  
Strip

$$A_{s_{req}}^+ = 342 \text{mm}^2,$$

$$\text{use } \emptyset 10 @ 225 \text{mm} ((2b, 1s) < S_{max.}) = 349 \text{mm}^2 >$$

$$A_{s}^+ = 342 \text{mm}^2$$

At discontinuous edge:  $\emptyset 10 @ 225 (2b)$

$$\rightarrow 2/3 * 349 = 232 \text{mm}^2 < A_{s_{min}}$$

$$A_{s_{add}} = 342 - 232 = 110 \text{mm}^2 (\emptyset 8 @ 450 = 111 \text{mm}^2 > 110)$$

$$S_{av} = (225 + 450) / 2 = 337 \text{mm} < S_{max} \text{ OK}$$



$$A_s^-_{req} = 625 \text{ mm}^2 \quad A_s^-_{prov} = (2/3 * 349) = 232 \text{ mm}^2$$

Panel  
2  
Long  
dir.  
Middle  
Strip

$$A_s^+ = 459 \text{ mm}^2, \text{ use } \emptyset 12 @ 225 \text{ mm} ((2b, 1s))$$

$$\langle S_{max.} \rangle = 503 \text{ mm}^2 > A_s^+ = 459 \text{ mm}^2$$

At discontinuous edge:  $\emptyset 12 @ 225 (2b)$

$$\rightarrow 2/3 * 503 = 335 \text{ mm}^2 < A_{s_{min}}$$

$$A_{s_{add}} = 342 - 335 = 7 \text{ mm}^2 \text{ (use } \emptyset 8 @ 675 = 74 \text{ mm}^2 > 7 \text{ mm}^2)$$

$$S_{av} = (225 + 450) / 2 = 337 \text{ mm} < S_{max} \text{ OK}$$

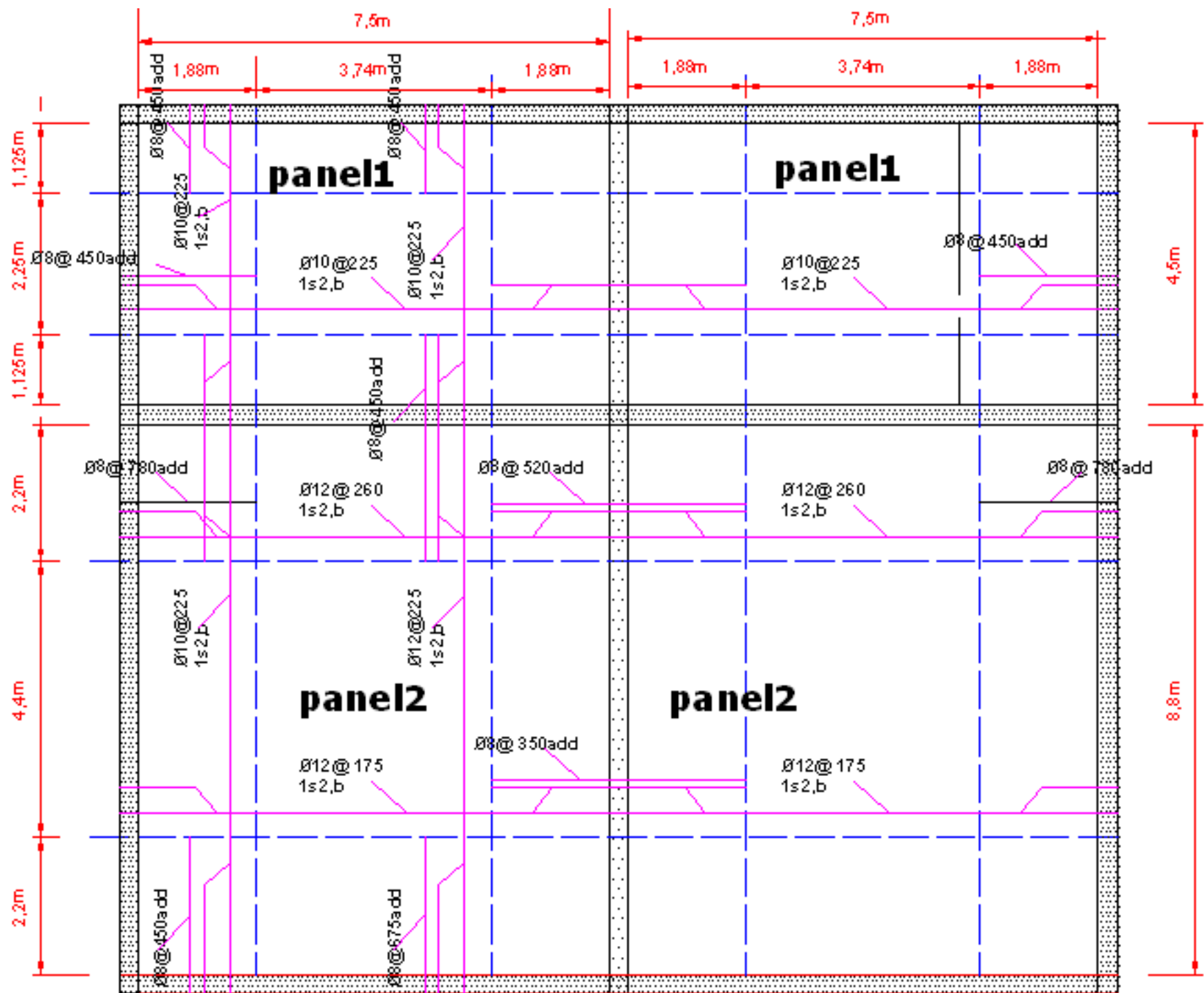
$$A_s^-_{req} = 668 \text{ mm}^2 \quad A_s^-_{prov} = (2/3 * 503) = 335 \text{ mm}^2$$

(Panel 2 Long dir.+ Panel 1 Short dir.) Middle Strip	$A_s^-_{req} = 668\text{mm}^2, A_s^-_{prov} = 335 + 232 = 567\text{mm}^2 <$ $668\text{mm}^2$ $\text{use } \emptyset 8 @ 450\text{mm} = 111\text{mm}^2 \text{ add } > 668 -$ $567 = 101\text{mm}^2$
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Panel 1 Short dir. Column Strip	Since $A_{s_{min}}$ control for middle strip, therefore, the reinforcement distribution will be fixed for column strip
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<p>Panel 2 Long dir. Column Strip</p>	<p> <math>A_s^+_{req} = 2/3 * 459 = 306 \text{mm}^2 &lt; A_{s_{min}}</math>,  use <math>\text{Ø}10@225 = 349 \text{mm}^2 ((2b, 1s) &gt; A_{s_{min}}</math>  At discontinuous edge: <math>\text{Ø}10@225(2b)</math>  <math>\rightarrow 2/3 * 349 = 232 \text{mm}^2 &lt; A_{s_{min}}</math>  <math>A_{s_{add}} = 342 - 232 = 110 \text{mm}^2</math> (use  <math>\text{Ø}8@450 = 111 \text{mm}^2 &gt; 110 \text{mm}^2</math>)  <math>S_{av} = (225 + 450 \text{mm}) / 2 = 337 \text{mm} &lt; S_{max}</math> OK </p>
	<p> <math>A_s^-_{req} = 2/3 * 668 = 445 \text{mm}^2 &lt; A_s^-_{prov} =</math>  <math>2/3(349 + 349) = 465 \text{mm}^2</math> </p>





# Corner reinforcement:

