



Refrigeration and Air conditioning Engineering.

3rd year – refrigeration and Air conditioning Course

M.Sc. Zahraa F. Hussain



Pumps selection part 2

Lecture -13 -

M.Sc. Zahraa F. Hussain

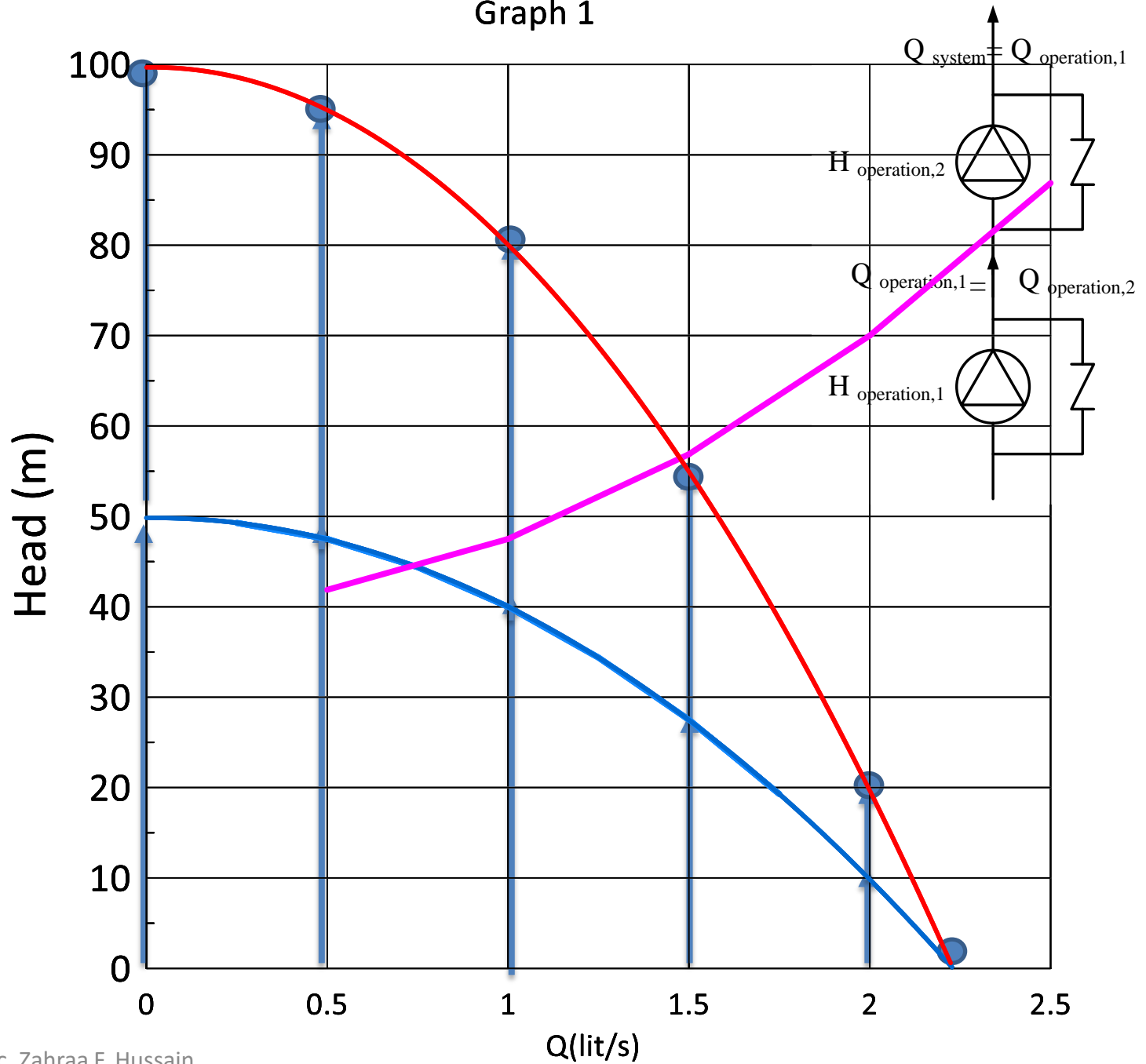
Msc. Zahraa F. Hussain



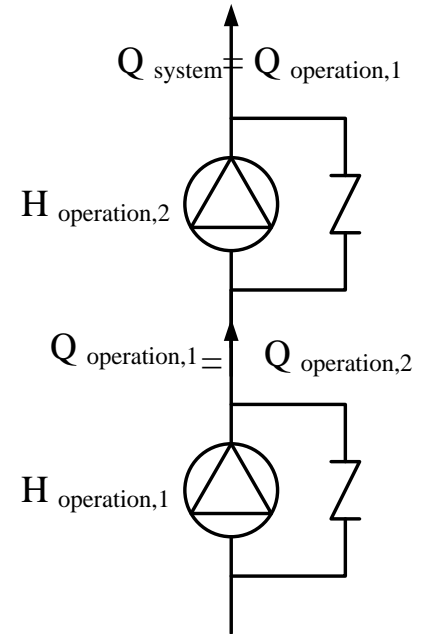
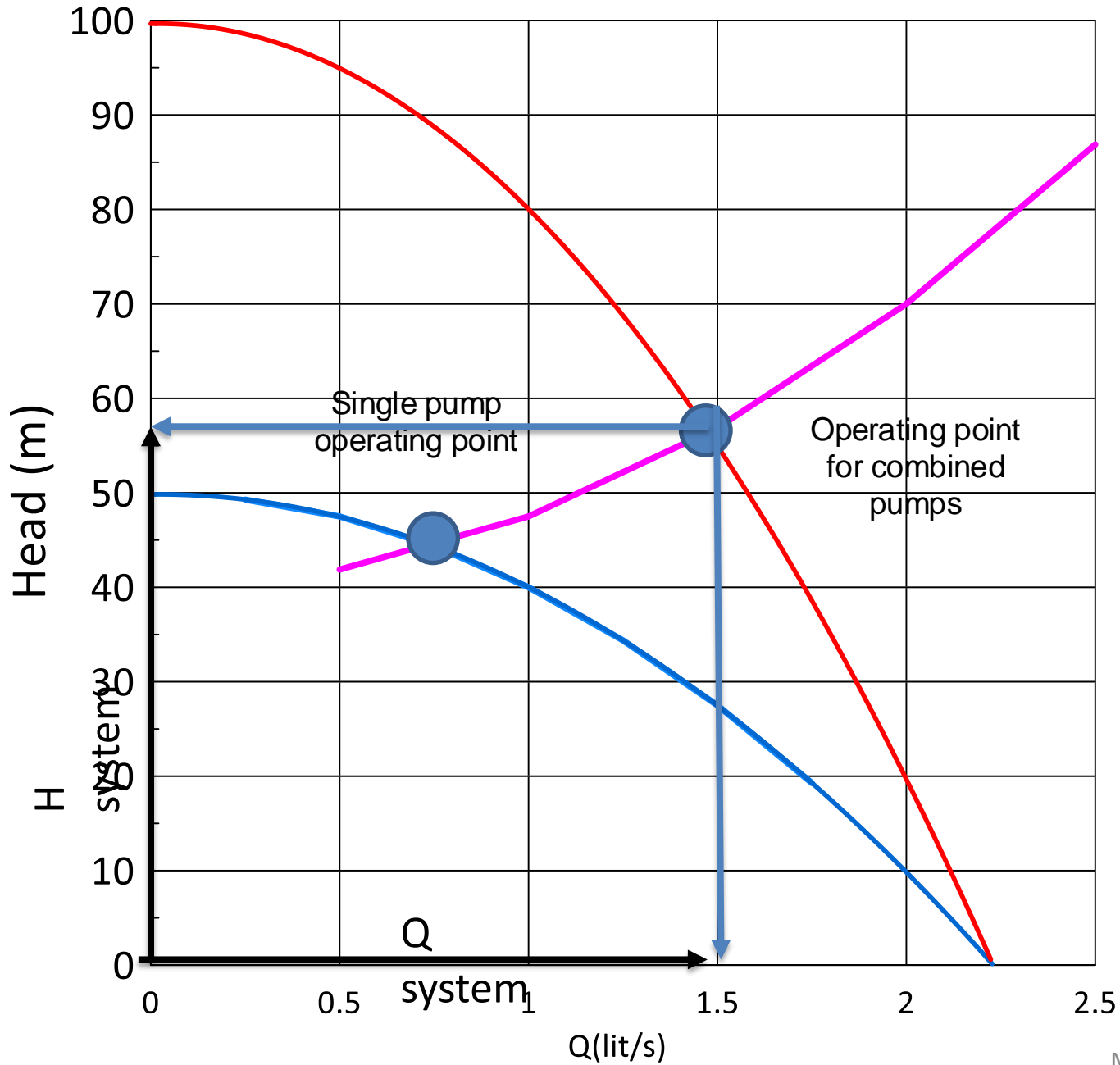
Pumps operated in series:

- Centrifugal pumps are rarely connected in serial, but a multi-stage pump can be considered as a serial connection of single-stage pumps.
- However, single stages in multistage pumps cannot be uncoupled. If one of the pumps in a serial connection is not operating, it causes a considerable resistance to the system.
- To avoid this, a bypass with a non-return valve could be build-in, see figure 8. The head at a given flow for a serial-connected pump is found by adding the single heads vertically.

Graph 1



Graph 1





Pump laws

- Various pump laws show the relationships between pressure, flow rate, efficiency and power. These can be used to calculate each factor:

$$\frac{Q_2}{Q_1} = \frac{rpm_2}{rpm_1} \quad (5-7)$$

$$\frac{p_2}{p_1} = \left(\frac{rpm_2}{rpm_1} \right)^2 \quad (5-8)$$

$$\frac{P_2}{P_1} = \left(\frac{rpm_2}{rpm_1} \right)^3 \quad (5-9)$$

$$\frac{p_2}{p_1} = \frac{\rho_2}{\rho_1} \quad (5-10)$$

$$\frac{Q_2}{Q_1} = \left(\frac{D_2}{D_1} \right)^3 \quad (5-11)$$

$$\frac{p_2}{p_1} = \left(\frac{D_2}{D_1} \right)^2 \quad (5-12)$$

$$\frac{P_2}{P_1} = \left(\frac{D_2}{D_1} \right)^5 \quad (5-13)$$



- Where:
- Q = volume flow rate (m^3/s)
- rpm = revolution speed (r
- P = pressure developed (Pa.)
- W = power (W)
- D = diameter of the impeller (m)
- ρ = density. (kg/m^3)



Pump Sizing

- **Key design inputs:**
- Details of fluid, for example water, glycol solution or oil.
- Design flow and return temperatures ($^{\circ}\text{C}$)
- System mass flow rates (kg/s)
- System pressure drops (Pa)
- Ambient conditions including the surrounding air temperature ($^{\circ}\text{C}$)



Design outputs:

- Schematic of pump layout installation, mounting and pipework connections
- Schedule of pump types, flow rates, pressure and efficiencies including motor requirements, drive type and adjustment, speed control and stand by provision
- Media details, such as water/refrigerant, and temperature.
- A schedule of electricity supply requirements



Calculation procedure:



- **Step 1.** Calculate the index run pressure drop and total system mass flow rate.
- **Step 2.** Convert mass flow rate to volume flow rate in l/s.
- **Step 3.** Determine system equations constant R. This can be done by substituting the required Δp and Q into the equation $\Delta p = R \cdot Q^2$ and then solving for R.
- **Step 4** Select a pump that will operate within the required parameters and plot the system and pump characteristics on the same graph.
- **Step 5.** Determine the operating point. Identify operating pressure and flow rate.
- **Step 6.** Calculate pump speed to achieve required values or select another pump.



- **Design tip:** With belt-driven pumps it is easy to vary the speed by changing the pulleys. If the pump is inverter-driven this can be done automatically.
- **Design tip:** If you use an additional margin with the required pressure drop to allow for differences between design pipe work layout and physical installations on site, do so carefully, as over sizing a pump will only result in excess energy usage.



Example

- A system has a volume flow rate requirement of 1 lit/s with an index run $\Delta p = 30\text{kPa}$. Find an appropriate pump from the A manufacturer's catalogue gives the following information for a centrifugal pump operating at 12 rev/s:

P	49.38	47.5	44.38	40	34.38	27.5	19.38
Q	0.25	0.5	0.75	1	1.25	1.5	1.75



- Step 1 and step 2: Pressure drop and volume flow rate are available in the units required.
- Step 3. The constant R in the system characteristic curve equation can be calculated as shown below:
 - $\Delta p = R \cdot Q^2$
 - $30 = R \cdot 1^2$
 - $R=30$
 - Then rewrite the equation above.
 - $\Delta p = 30 \cdot Q^2$

Q	0.25	0.5	0.75	1	1.25	1.5	1.75
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$$\Delta p = 30 \cdot Q^2$$

$$\Delta p = 30 \times 0.25^2 = 1.875$$

$$\Delta p = 30 \times 0.5^2 = 7.5$$

$$\Delta p = 30 \times 0.75^2 = 16.875$$

$$\Delta p = 30 \times 1^2 = 30$$

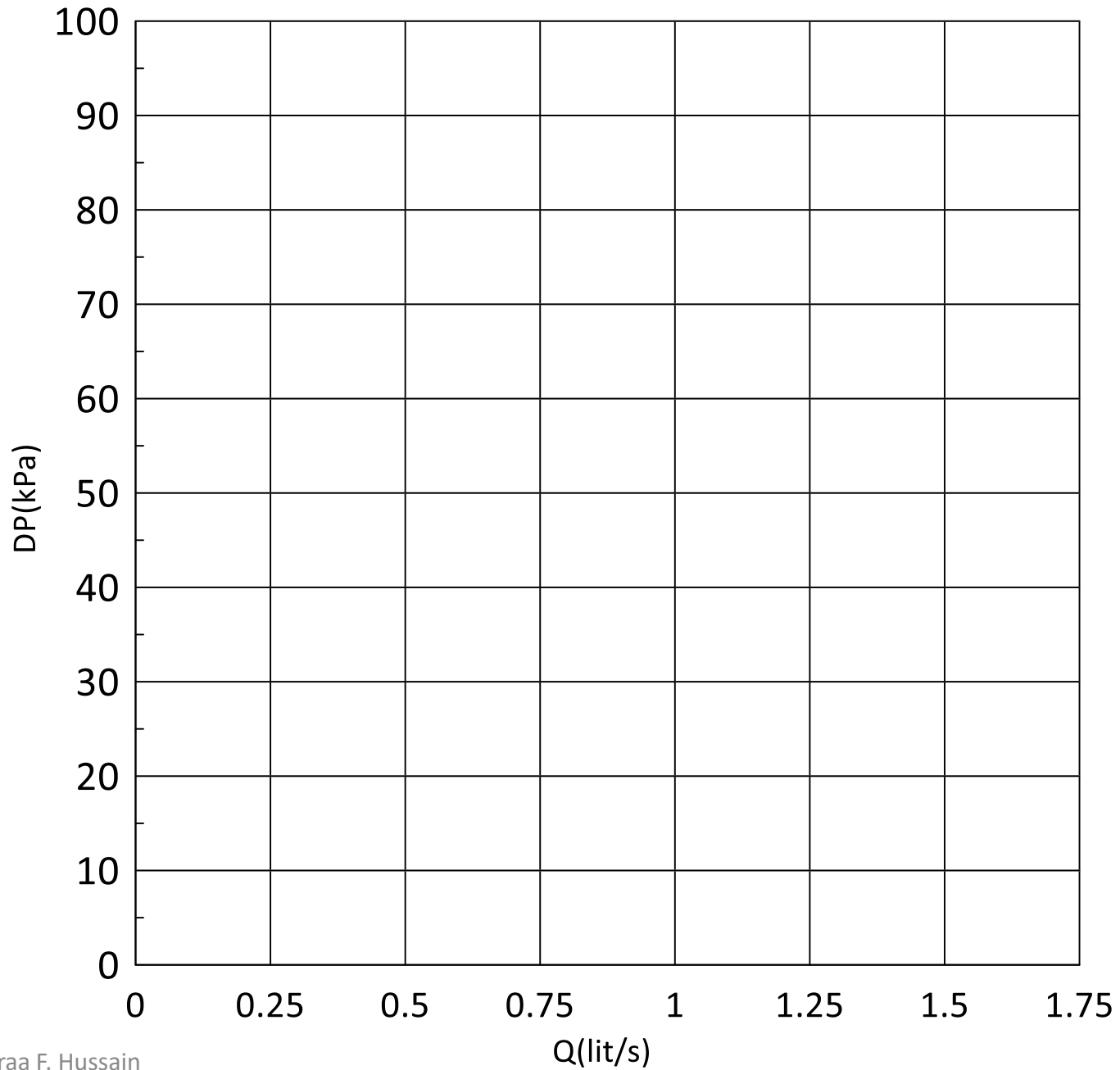
$$\Delta p = 30 \times 1.25^2 = 46.875$$

$$\Delta p = 30 \times 1.5^2 = 67.5$$

$$\Delta p = 30 \times 1.75^2 = 91.875$$

Q	$\Delta p = 30 \cdot Q^2$
0.25	1.875
0.5	7.5
0.75	16.875
1	30
1.25	46.875
1.5	67.5
1.75	91.875

Graph 1

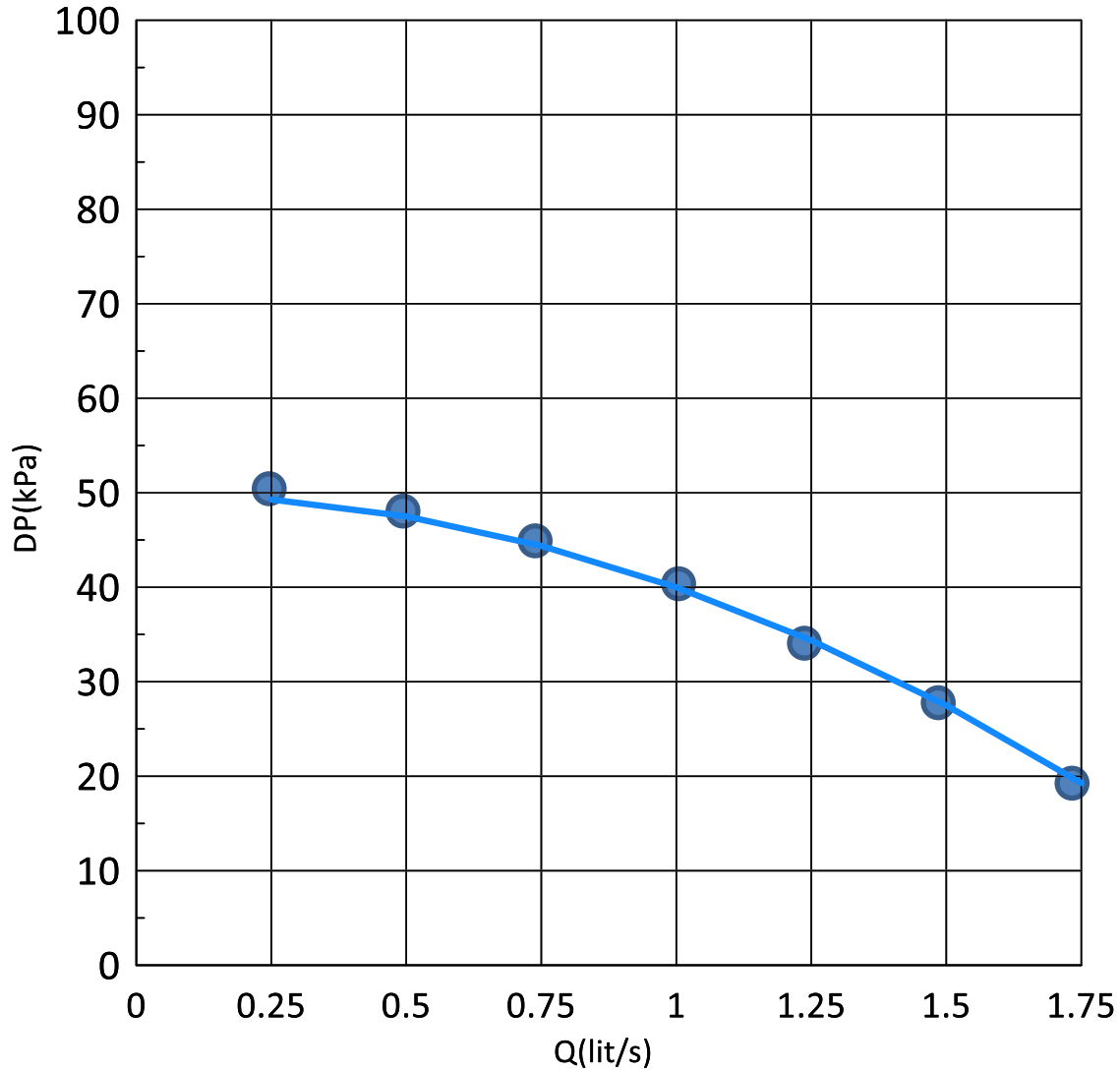


- draw the pump characteristic curve using manufacturer's catalogue

P	49.38	47.5	44.38	40	34.38	27.5	19.38
Q	0.25	0.5	0.75	1	1.25	1.5	1.75

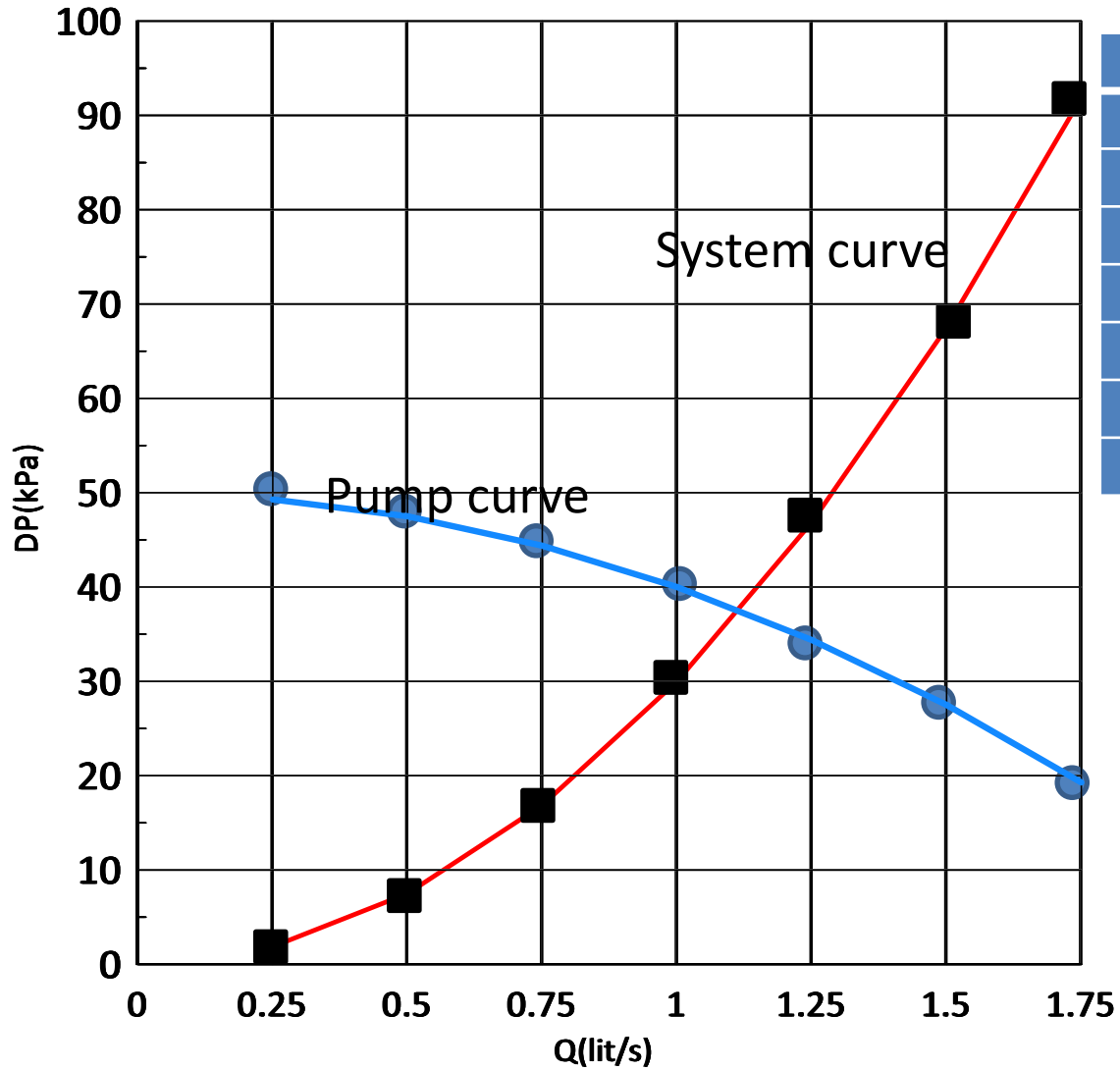
P	49.38	47.5	44.38	40	34.38	27.5	19.38
Q	0.25	0.5	0.75	1	1.25	1.5	1.75

Graph 1



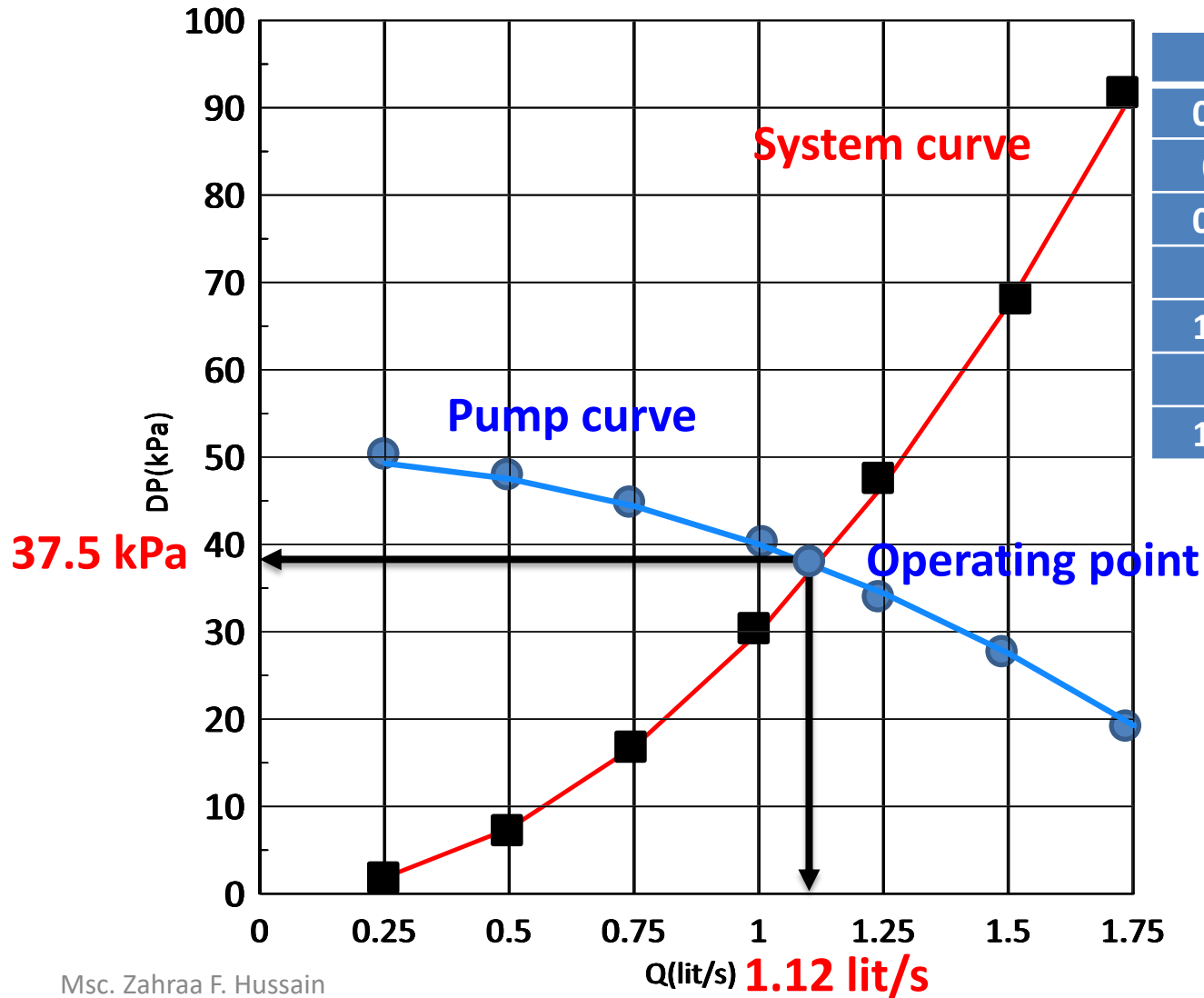
- Then on the same graph, draw the system characteristic curve, as shown bellows:

Graph 1



Q	$\Delta p = 30 \cdot Q^2$
0.25	1.875
0.5	7.5
0.75	16.875
1	30
1.25	46.875
1.5	67.5
1.75	91.875

Graph 1





- The intersection between the two curves gives the operating points of the system and pump.
- The operating point occurs when the two curves intersect, 1.12 lit/s at 37.5 kPa
- As 1.12 1/s is too high, the pump will need to be slowed down in order to achieve the required flow rate.



- Alternatively, a different pump may give a closer value. This is worth considering when comparing the efficiency of different pumps at different speeds and pressures.



- *Required $Q_2 = 1 \text{ lit/s}$, $\Delta p_2 = 30 \text{ kPa}$*
- *Results $Q_1 = 1.12 \text{ l/s}$, $\Delta p_1 = 37.5$, $rpm_1 = 12$*
- $$\frac{Q_2}{Q_1} = \frac{rpm_2}{rpm_1}$$
- $$rpm_2 = rpm_1 \cdot \frac{Q_2}{Q_1} = 12 \times \frac{1}{1.12} = 10.7 \text{ rps}$$
- This can also be achieved by using equation (5-8) for example
- $$\frac{p_2}{p_1} = \left(\frac{rpm_2}{rpm_1} \right)^2$$
- $$rpm_2 = rpm_1 \cdot \left(\frac{p_2}{p_1} \right)^{0.5} = 12 \times \left(\frac{30}{37.5} \right)^{0.5} = 10.7 \text{ rps}$$
- Then to get $Q_2 = 1 \text{ lit/s}$, $\Delta p_2 = 30 \text{ kPa}$, the rps should be 10.7 rps



Design tip

- A functioning pump will have operating losses such as belt or drive losses. The pump and system performance curves do not take this into account.



Design tip

- The use of inverters to control the speed of the pump is the most efficient method of controlling and restricting the flow.
- The cost and maintenance requirements of the inverter need to be considered.
- An alternate method is to adjust a globe valve on the pump discharge side to achieve the required flow.
- However the latter method is wasteful of energy and only works if all other parameters remain constant