

(Home works lecture 2)

Q2: Calculate the activity of ^{137}Cs after: (a) 2 years, (b) 15 years, (c) 30 years; if its activity at production was (10 μCi) and the half – life of ^{137}Cs is (30 years)?

$$A_o = 10 \mu\text{Ci} \text{ (Activity at production)}$$

$$t_{1/2} = 30 \text{ y}$$

$$\text{(Activity at t)} \quad A = A_o e^{-\lambda t}$$

$$\lambda = \frac{0.693}{t_{1/2}} = \frac{0.693}{30 \text{ y}} = 0.0231 \text{ y}^{-1}$$

$$\text{(a) (At } t = 2 \text{ y)} \quad A = 10 \mu\text{Ci} \times e^{-0.0231 \text{ y}^{-1} \times 2 \text{ y}} = 9.5 \mu\text{Ci}$$

$$\text{(b) (At } t = 15 \text{ y)} \quad A = 10 \mu\text{Ci} \times e^{-0.0231 \text{ y}^{-1} \times 15 \text{ y}} = 7 \mu\text{Ci}$$

$$\text{(c) (At } t = 30 \text{ y)} \quad A = 10 \mu\text{Ci} \times e^{-0.0231 \text{ y}^{-1} \times 30 \text{ y}} = 5 \mu\text{Ci}$$

Q3: Radioactive element was produced at 8 – 1 – 2020 with radioactivity 5 mCi half-life of this source is 5.6 y. calculate its activity on today's date?

$$A_o = 5 \text{ mCi} \text{ (Activity at production)}$$

$$t_{1/2} = 5.6 \text{ y}$$

$$\lambda = \frac{0.693}{t_{1/2}} = \frac{0.693}{5.6 \text{ y} \times 365.25} = 0.00034 \text{ day}^{-1}$$

$$t = (26 - 2 - 2024) - (5 - 1 - 2020) = 21 \text{ day} + 1 \text{ month} + 4 \text{ year}$$

$$t = 21 \text{ day} + 1 \times 30 \text{ day} + 4 \times 365.25 = 1512 \text{ day}$$

$$A = A_o e^{-\lambda t}$$

$$A = 5 \text{ mCi} \times e^{-0.00034 \text{ day}^{-1} \times 1512 \text{ day}} = 5 \text{ mCi} \times 0.59 = 2.9 \text{ mCi}$$

(Home Work lecture 4)

Examples 1: Gamma photon emitted from the cesium source ^{137}Cs , has energy $0.662 \mu\text{eV}$, and was absorbed with the electron in the ground level of the hydrogen atom by the photoelectric interaction. Hydrogen binding energy 13.6 eV , calculate the kinetic energy of the electron?

فوتون كما المنبعث من مصدر السيزيزم ^{137}Cs وطاقته $0.662 \mu\text{eV}$ امتصت مع الالكترن في المستوي الارضي لذرة الهيدروجين تفاعلا كهروضوئيا طاقة ربط الهيدروجين 13.6 eV احسب الطاقة الحركية للالكترن المتحرر؟

Answer:

$$h\nu = E_B + E_K$$

Where: $h\nu$ = Energy of incident photon.

E_B = Binding energy of electron.

E_K = Kinetic energy of electron.

$$E_K = h\nu - E_B \quad E_k = 0.662 \times 10^6 \text{ eV} - 13.6 \text{ eV} = 661986.4 \text{ eV} = 0.6619 \mu \text{ eV}$$

Example 2: Calculate the energy, frequency and wavelength of the scattered photons at an angle $\Phi = 90^\circ$ when the energy of the incident photons is $1.173 \mu\text{eV}$; Calculate the kinetic energy of the outgoing electron?

احسب الطاقة والتردد والطول الموجي للفوتونات المستطارة بزاوية $\Phi = 90$ عندما تكون طاقة الفوتونات الساقطة $1.173 \mu \text{ eV}$ ثم احسب الطاقة الحركية للالكترن المتحرر؟

Answer:

$$h\nu^- = \frac{h\nu}{1 + \frac{h\nu}{m_0c^2}(1 - \cos\Phi)}$$

$$h\nu^- = \frac{1.173}{1 + \frac{1.173}{0.511}(1 - \cos 90)}$$

$$h\nu^- = 0.355 \mu \text{ eV} = 0.355 \times 10^6 \times 1.6 \times 10^{-19} = 0.568 \times 10^{-13} \text{ J}$$

$$E^- = h\nu^- \quad 0.568 \times 10^{-13} \text{ J} = 6.6 \times 10^{-34} \text{ J.S} \times \nu^- \quad \ast \quad \nu^- = 0.0856 \times 10^{21} \text{ sec}^{-1}$$

$$C = \lambda \cdot \nu \quad \lambda = C / \nu \quad \lambda = 3 \times 10^8 \text{ ms}^{-1} / 0.0856 \times 10^{21} \text{ sec}^{-1} = 35.04 \times 10^{-13} \text{ m}$$

$$h\nu = h\nu^- + E_K \quad E_K = h\nu - h\nu^- \quad E_K = 1.173 \mu \text{ eV} - 0.355 \mu \text{ eV} = 0.818 \mu \text{ eV}$$

Example 3: Calculate the kinetic energy of the positron resulting from the pair production interaction when the energy of the incident photon is 2.022 μeV ?

احسب الطاقة الحركية لبوزترون الناتج من تفاعل انتاج الزوج عندما تكون طاقة الفوتون الساقط 2.022 $\mu \text{ eV}$ ؟

$$h\nu = m_{o_e} C^2 + m_{o_e} C^2 + E_{K_{e^-}} + E_{K_{e^+}}$$

$$h\nu = 2 m_0 C^2 + 2 E_k \quad 2.022 = 2 \times 0.511 + 2 E_k$$

$$2 E_k = 1 \quad E_k = 0.5 \mu \text{ eV}$$

Example 4: Calculate the thickness of the water layer that reduces the number of photons to 80% of its original number? Where $(\mu_m)_{\text{water}} = 0.0706 \text{ cm}^2/\text{g}$; $\rho = 1 \text{ g/cm}^3$

احسب سمك طبقة الماء التي تقلل عدد الفوتونات الى 80% من عددها الاصلي حيث $(\mu_m)_{\text{water}} = 0.0706 \text{ cm}^2/\text{g}$ ؟ $\rho = 1 \text{ g/cm}^3$

$$I = I_0 e^{-\mu x}$$

$$\mu_m = \mu_l / \rho \quad \mu_l = \mu_m \times \rho \quad \mu_l = 0.0706 \text{ cm}^2/\text{g} \times 1 \text{ g/cm}^3 = 0.0706 \text{ cm}^{-1}$$

$$I = 0.8 I_0$$

$$0.8 I_0 = I_0 e^{-0.0706 x}$$

$$\text{Ln } 0.8 = -0.0706 x$$

$$x = 3.16 \text{ cm}$$