Second stage
Medical Physical Department

# Digital Electronics 

Lab 4 : Boolean expression

## By

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## Boolean expression

## Objectives

- To learn how to directly convert a Boolean expression to circuit.
- To learn how to analyze a given digital logic circuit by finding the Boolean expression thatrepresents the circuit
- To learn how to analyze a given digital logic circuit by finding the truth table that represents thecircuit.


## Example:

$$
Z=A+B \cdot C^{\prime}
$$

The above function is implemented in the following digital logic Circuit


Now after drawing the circuit above using EWB we find that its truth table is as shown below ( notice thatlogic 1 means connect the input to the Vcc line, and logic $\mathbf{0}$ means connecting the input to the ground)

| $\mathbf{A}$ | $\mathbf{B}$ | $\mathbf{C}$ | $\mathbf{Z}$ |
| :---: | :---: | :---: | :---: |
| $\mathbf{0}$ | 0 | 0 | $\mathbf{0}$ |
| $\mathbf{0}$ | 0 | 1 | $\mathbf{0}$ |
| $\mathbf{0}$ | 1 | 0 | $\mathbf{1}$ |
| $\mathbf{0}$ | 1 | 1 | $\mathbf{0}$ |
| $\mathbf{1}$ | 0 | 0 | $\mathbf{1}$ |
| $\mathbf{1}$ | 0 | 1 | $\mathbf{1}$ |
| $\mathbf{1}$ | 1 | 0 | $\mathbf{1}$ |
| $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ |

## Lab Tasks

Task 1: Converting Boolean expressions into circuits

Convert the following Boolean expression to a circuit, draw the circuit on EWB and simulate it to fill-in its truth table shown below.

$$
X=Y+Z . Y^{\prime}
$$



Draw the circuit in the space below

Now, fill-in the truth table of the circuit you drawn

| $\mathbf{Y}$ | $\mathbf{Z}$ | $\mathbf{X}$ |
| :--- | :--- | :--- |
| $\mathbf{0}$ | 0 |  |
| $\mathbf{0}$ | 1 |  |
| $\mathbf{1}$ | 0 |  |
| $\mathbf{1}$ | $\mathbf{1}$ |  |

Task 2: Converting Boolean expressions into circuits
Convert the following Boolean expression to a circuit, draw the circuit on EWB and simulate it to fill-in itstruth table shown below.

> A

日

| A | B | C | D |
| :---: | :---: | :---: | :---: |
| $\mathbf{0}$ | 0 | 0 |  |
| $\mathbf{0}$ | 0 | 1 |  |
| $\mathbf{0}$ | 1 | 0 |  |
| $\mathbf{0}$ | 1 | $\mathbf{1}$ |  |


| $\mathbf{1}$ | 0 | 0 |  |
| :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | 0 | 1 |  |
| 1 | 1 | 0 |  |
| $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ |  |

## Task 3: Digital logic circuit analysis - Finding the Boolean expression of a given circuit

Find the Boolean expression of the following circuit, draw the circuit on EWB and simulate it to fill-in its truth table shown below.
$\mathrm{W}=$


Note: the logic converter tool from EWB to fill-in the following table. For that, you need to connect the A, B and C inputs of the logic converter to $\mathrm{X}, \mathrm{Y}$ and Z lines, respectively. Further, you need to connect the 'out' line of the logic converter to W . As shown in the following diagram


| $\mathbf{X}$ | Y | Z | W |
| :--- | :--- | :--- | :--- |
| $\mathbf{0}$ | 0 | $\mathbf{0}$ |  |
| $\mathbf{0}$ | 0 | 1 |  |
| $\mathbf{0}$ | 1 | 0 |  |
| $\mathbf{0}$ | 1 | 1 |  |
| $\mathbf{1}$ | 0 | 0 |  |
| $\mathbf{1}$ | 0 | $\mathbf{1}$ |  |
| $\mathbf{1}$ | 1 | 0 |  |
| $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ |  |

