

وزارة التعليم العالي والبحث العلمي جامعة المستقبل

LEC - SIX

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Lecture Title : NETWORK THEOREMS (DC)

NETWORK THEOREMS (DC)

9.2 SUPERPOSITION THEOREM

The current through, or voltage across, any element of a network is equal to the algebraic sum of the currents or voltages produced independently by each source.

When removing a voltage source from a network schematic, replace it with a direct connection (short circuit) of zero ohms. Any internal resistance associated with the source must remain in the network.

When removing a current source from a network schematic, replace it by an open circuit of infinite ohms. Any internal resistance associated with the source must remain in the network.



Removing a voltage source and a current source to permit the application of the superposition theorem.

EXAMPLE 9.1 Using the superposition theorem, determine current *11* for the network in Fig.

Due to the open circuit, resistor *R1* is in series

$$I'_{1} = \frac{V_{1}}{R_{1}} = \frac{E}{R_{1}} = \frac{30 \text{ V}}{6 \Omega} = 5 \text{ A}$$
$$I''_{1} = \frac{R_{sc}I}{R_{sc} + R_{1}} = \frac{(0 \Omega)I}{0 \Omega + 6 \Omega} = 0 \text{ A}$$
$$I_{1} = I'_{1} + I''_{1} = 5 \text{ A} + 0 \text{ A} =$$



5 A

EXAMPLE 9.2 Using the superposition theorem, determine the current through the 12 Ω resistor in Fig. Note that this is a twosource network of the type examined in the previous chapter when we applied branch- $E_1 = 54 \text{ V}$ current analysis and mesh analysis.

 R_1

 24Ω

54 V

+

E



The total resistance seen by the source is therefore

 $R_T = R_1 + R_2 || R_3 = 24 \Omega + 12 \Omega || 4 \Omega = 24 \Omega + 3 \Omega = 27 \Omega$

and the source current is

$$I_s = \frac{E_1}{R_T} = \frac{54 \text{ V}}{27 \Omega} = 2 \text{ A}$$

Using the current divider rule results in the contribution to I_2 due to the 54 V source:



Therefore, the total resistance seen by the 48 V source is

 $R_{T} = R_{3} + R_{2} \| R_{1} = 4 \Omega + 12 \Omega \| 24 \Omega = 4 \Omega + 8 \Omega = 12 \Omega$

and the source current is

$$I_s = \frac{E_2}{R_T} = \frac{48 \text{ V}}{12 \Omega} = 4 \text{ A}$$

Applying the current divider rule results in

$$I''_{2} = \frac{R_{1}(I_{s})}{R_{1} + R_{2}} = \frac{(24 \ \Omega)(4 \ A)}{24 \ \Omega + 12 \ \Omega} = 2.67 \ A$$

It is now important to realize that current *I2 due to each source has a* different direction, as shown in Fig. The net current therefore is the difference of the two and the direction of the larger as follows:

 $I_2 = I''_2 - I'_2 = 2.67 \text{ A} - 0.5 \text{ A} = 2.17 \text{ A}$



9.3 THÉVENIN'S THEOREM

Any two-terminal dc network can be replaced by an equivalent circuit consisting solely of a voltage source and a series resistor as shown in Fig.



Thévenin's Theorem Procedure

 Remove that portion of the network where the Thévenin equivalent circuit is found. In Fig., this requires that the load resistor RL be temporarily removed from the network.
Mark the terminals of the remaining two-terminal network.



RTh:

3.Calculate RTh by first setting all sources to zero (voltage sources are replaced by short circuits, and current sources by open circuits) and then finding the resultant resistance between the two marked terminals. (If the internal resistance of the voltage and/or current sources is included in the original network, it must remain when the sources are set to zero.)

ETh:

4.Calculate ETh by first returning all sources to their original position and finding the opencircuit voltage between the marked terminals. (This step is invariably the one that causes most confusion and errors. In all cases, keep in mind that it is the open circuit potential between the two terminals marked in step 2.)

Conclusion:

5.Draw the Thévenin equivalent circuit with the portion of the circuit previously removed replaced between the terminals of the equivalent circuit. This step is indicated by the placement of the resistor RL between the terminals of the Thévenin equivalent circuit as shown in Fig. 9.25(b).

EXAMPLE 9.7 Find the Thévenin equivalent circuit for the network in the shaded area of the network in Fig.



 $R_{Th} = R_1 + R_2 = 4 \ \Omega + 2 \ \Omega = 6 \ \Omega$



In this case, since an open circuit exists between the two marked terminals, the current is zero between these terminals and through the 2 Ω resistor. The voltage drop across R_2 is, therefore,

and
$$V_2 = I_2 R_2 = (0) R_2 = 0 V$$

 $E_{Th} = V_1 = I_1 R_1 = I R_1 = (12 \text{ A})(4 \Omega) = 48 \text{ V}$

9.4 NORTON'S THEOREM

Any two-terminal linear bilateral dc network can be replaced by an equivalent circuit consisting of a current source and a parallel resistor, as shown in Fig.



Norton's Theorem Procedure

- 1. Remove that portion of the network across which the Norton equivalent circuit is found.
- 2.Mark the terminals of the remaining two-terminal network. RN:

3.Calculate RN by first setting all sources to zero (voltage sources are replaced with short circuits, and current sources with open circuits) and then finding the resultant resistance between the two marked terminals. (If the internal resistance of the voltage and/or current sources is included in the original network, it must remain when the sources are set to zero.) Since RN = RTh, the procedure and value obtained using the approach described for Thévenin's theorem will determine the proper value of RN. IN:

4.Calculate IN by first returning all sources to their original position and then finding the short- circuit current between the marked terminals. It is the same current that would be measured by an ammeter placed between the marked terminals.

Conclusion:

5. Draw the Norton equivalent circuit with the portion of the circuit previously removed replaced between the terminals of the equavilant circuit

The Norton and Thévenin equivalent circuits can also be found from each other by using the source transformation discussed earlier in this chapter and reproduced in Fig.



EXAMPLE 9.11 Find the Norton equivalent circuit for the network in the shaded area in Fig.





$$R_N = R_1 \| R_2 = 3 \Omega \| 6 \Omega = \frac{(3 \Omega)(6 \Omega)}{3 \Omega + 6 \Omega} = \frac{18 \Omega}{9} = 2 \Omega$$
$$V_2 = I_2 R_2 = (0)6 \Omega = 0 V$$
$$I_N = \frac{E}{R_1} = \frac{9 V}{3 \Omega} = 3 \Lambda$$



EXAMPLE 9.12 Find the Norton equivalent circuit for the network external to the 9 Ω resistor in Fig.

 $R_N = R_1 + R_2 = 5 \ \Omega + 4 \ \Omega = 9 \ \Omega$







 $I_N = \frac{R_1 I}{R_1 + R_2} = \frac{(5 \ \Omega)(10 \ \text{A})}{5 \ \Omega + 4 \ \Omega} = \frac{50 \ \text{A}}{9} = 5.56 \ \text{A}$



GOOD LUCK