Logic Gate

College of
Engineering & Technology

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Level 1 , Semester 1
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Binary Adders

The majority of this course material is based on text and presentations of :

Binary Addition

The rules for binary addition are

0 + 0 = 0	Sum = 0, carry = 0
0 + 1 = 0	Sum = 1, carry = 0
1 + 0 = 0	Sum = 1, carry = 0
1 + 1 = 10	Sum = 0, carry = 1

When an input carry = 1 due to a previous result, the rules are

1 + 0 + 0 = 01	Sum = 1, carry = 0
1 + 0 + 1 = 10	Sum = 0, carry = 1
1 + 1 + 0 = 10	Sum = 0, carry = 1
1 + 1 + 1 = 10	Sum = 1, carry = 1

Binary Addition

Example Add the binary numbers 00111 and 10101 and show the equivalent decimal addition.

Solution

$$\begin{array}{r} {\scriptstyle 0\,1\,1\,1} \\ 00111 \\ 10101 \\ \hline 11100 \end{array} \quad \begin{array}{r} 7 \\ 21 \\ \hline = 28 \end{array}$$

Binary Subtraction

The rules for binary subtraction are

$$0 - 0 = 0$$
$$1 - 1 = 0$$
$$1 - 0 = 1$$
$$10 - 1 = 1 \text{ with a borrow of } 1$$

Example Subtract the binary number 00111 from 10101 and show the equivalent decimal subtraction.

Solution

```
  1 1 1
  1̸0̸1̸01      21
  00111       7
  -----     ---
  01110  =  14
```

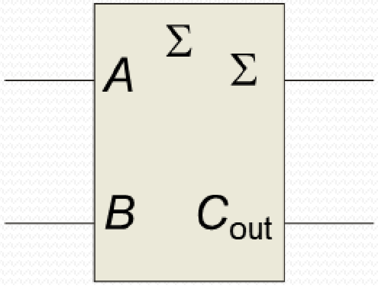
Half-Adder

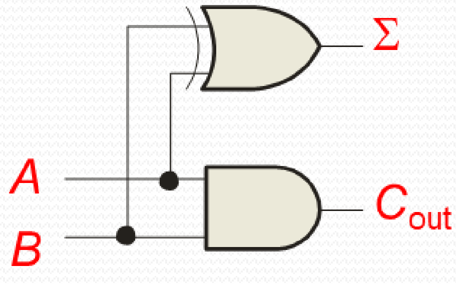
Basic rules of binary addition are performed by a **half adder**, which has two binary inputs (*A* and *B*) and two binary outputs (Carry out and Sum).

The inputs and outputs can be summarized on a truth table.

Inputs		Outputs	
A	*B*	C_{out}	Σ
0	0	0	0
0	1	0	1
1	0	0	1
1	1	1	0

The logic symbol and equivalent circuit are:



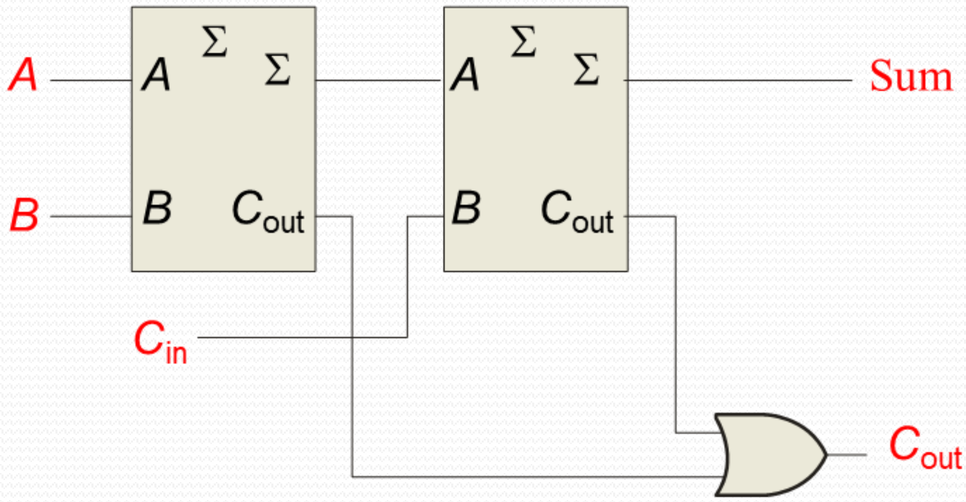


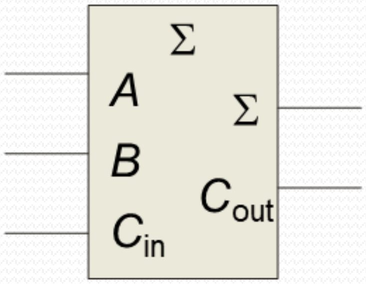
Full-Adder

By contrast, a **full adder** has three binary inputs (*A*, *B*, and Carry in) and two binary outputs (Carry out and Sum). The truth table summarizes the operation.

A full-adder can be constructed from two half adders as shown:

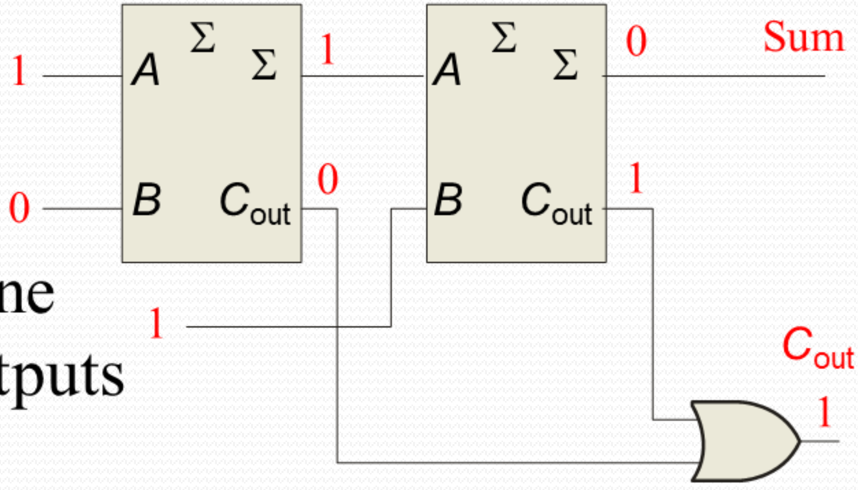
Inputs			Outputs	
A	*B*	C_{in}	C_{out}	Σ
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1





Symbol

Full-Adder



Example

For the given inputs, determine the intermediate and final outputs of the full adder.

Solution

The first half-adder has inputs of 1 and 0; therefore the Sum =1 and the Carry out = 0.

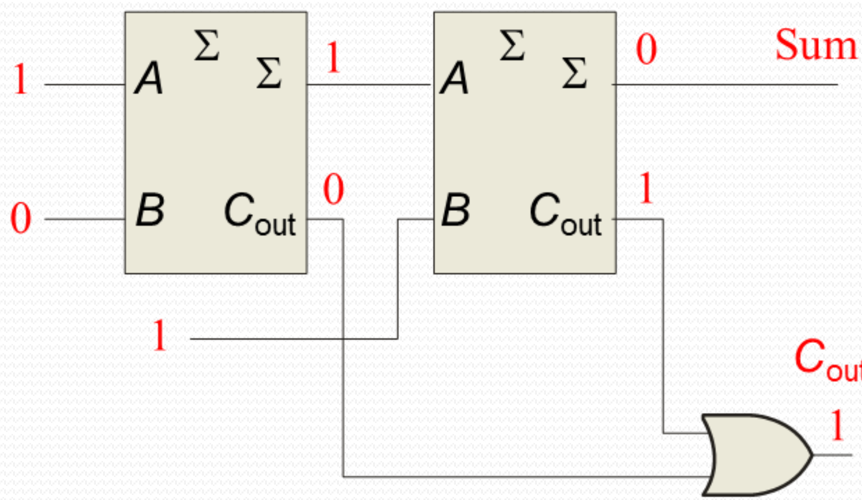
The second half-adder has inputs of 1 and 1; therefore the Sum = 0 and the Carry out = 1.

The OR gate has inputs of 1 and 0, therefore the final carry out = 1.

Full-Adder

Notice that the result from the previous example can be read directly on the truth table for a full adder.

Inputs			Outputs	
A	B	C_{in}	C_{out}	Σ
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1



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Binary Numbers

For digital systems, the binary number system is used. Binary has a radix of two and uses the digits 0 and 1 to represent quantities.

The column weights of binary numbers are powers of two that increase from right to left beginning with $2^0 = 1$:

$$\ldots 2^5\ 2^4\ 2^3\ 2^2\ 2^1\ 2^0.$$

For fractional binary numbers, the column weights are negative powers of two that decrease from left to right:

$$2^2\ 2^1\ 2^0.\ 2^{-1}\ 2^{-2}\ 2^{-3}\ 2^{-4}\ \ldots$$

Binary Conversions

The decimal equivalent of a binary number can be determined by adding the column values of all of the bits that are 1 and discarding all of the bits that are 0.

Example Convert the binary number 100101.01 to decimal.

Solution Start by writing the column weights; then add the weights that correspond to each 1 in the number.

2^5 2^4 2^3 2^2 2^1 2^0. 2^{-1} 2^{-2}

32 16 8 4 2 1 . ½ ¼

1 0 0 1 0 1. 0 1

32 +4 +1 +¼ = 37¼

Binary Conversions

You can convert a decimal whole number to binary by reversing the procedure. Write the decimal weight of each column and place 1's in the columns that sum to the decimal number.

Example Convert the decimal number 49 to binary.

Solution The column weights double in each position to the right. Write down column weights until the last number is larger than the one you want to convert.

2^6	2^5	2^4	2^3	2^2	2^1	2^0.
64	32	16	8	4	2	1.
0	1	1	0	0	0	1.