

## ALMUSTAQBAL UNIVERSITY

DEPARTMENT OF BUILDING \& CONSTRUCTION ENGINEERING TECHNOLOGY

## YIELD LINE THEORY SOLVED EXAMPLES II

EXAMPLE 13: by using the yield line theory, determine the moment (m) for the simply supported two-way reinforced concrete slab shown in the figure below which is subjected to a uniformly distributed load (w) kPa. SOLUTION:
$W_{E}=w \times A \times$ displacement
$=\left(w \times\left(\frac{1}{2} \times r \times r \beta\right) \times \frac{1}{3}\right) \times \frac{2 \pi}{\beta}=\frac{w \pi r^{2}}{3}$

$$
W_{I}=m \times l \times \theta
$$

$$
=\left(m \times r \beta \times \frac{1}{r}\right) \times \frac{2 \pi}{\beta}=2 \pi m
$$

$W_{E}=W_{I}$
$\frac{w \pi r^{2}}{3}=2 \pi m \rightarrow \therefore m=\frac{w \pi r^{2}}{6 \pi}=\frac{w r^{2}}{6}$.


EXAMPLE 14: the circular slab of a radius ( r ) is supported by 4 columns. Find the ultimate resisting moment (m) per linear meter required just to sustain a concentrated factored load of P kN .

## SOLUTION:

$W_{E}=P \times 1=P$
$W_{I}=\left(m \times \frac{r \sqrt{2}}{2} \times 2 \times \frac{1}{r}\right) \times 4=4 \sqrt{2} m$
$W_{E}=W_{I}$

$\therefore P=4 \sqrt{2} m \rightarrow m=\frac{P}{4 \sqrt{2}}$


EXAMPLE 15: the circular slab with a diameter of 20 m is supported by three columns as shown in the figure below. Find the ultimate resisting moment per linear meter ( m ) if the slab is subjected to a concentrated load of P kN at the centre of the slab.

SOLUTION:
$W_{E}=P \times 1=P$
$W_{I}=m \times l \times \theta$
$=\left(m \times 17.32 \times \frac{1}{10}\right) \times 3=5.196 m$
$W_{E}=W_{I}$
$m=\frac{P}{5.196}$


EXAMPLE 16: the same circular slab shown in example 15, but it is subjected to a uniformly distributed ultimate load of (20) kPa. Determine the ultimate resisting moment per linear meter (m). Assume that the displacement of a single segment is 0.5513 m .

## SOLUTION:

$W_{E}=w \times A \times$ displacement

$$
\begin{aligned}
& =20 \times\left(\frac{120}{360} \times \pi \times 10^{2}\right) \times 0.5513 \times 3 \\
& =3464 \mathrm{kN} . \mathrm{m}
\end{aligned}
$$

$W_{I}=\left(m \times 17.32 \times \frac{1}{10}\right) \times 3=5.196 m$
$W_{E}=W_{I}$
$\therefore m=667 k N . m$


EXAMPLE 17: The two-way slab shown in the figure below is supported by four columns. Determine the ultimate resisting moment per linear meter (m) if the slab was subjected to uniformly distributed load of (w) kPa .

## SOLUTION:

$W_{E}=w \times A \times$ displacement.
$=w \times\left(4 \times 2 \times \frac{1}{2}\right) \times \frac{1}{3} \times 4=\frac{16}{3} w$.
$W_{I}=m \times l \times \theta$
$=m \times 4 \times \frac{1}{2} \times 4=8 m$.
$W_{E}=W_{I}$
$\therefore m=\frac{16}{24} w$.


