Al-Mustaqbal university
Engineering technical college
Department of Building
&Construction Engineering



Mathematics
First class
Lecture No.4

Assist. Lecture

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Lecture Four:

Derivatives :-

$$- f(x) = k \Rightarrow f(x) = 0$$

$$f(x) = 5 \Rightarrow f(x) = 0$$

$$- f(x) = \chi^n \Rightarrow f(x) = n \chi^{n-1}$$

$$f(x) = \chi^6 \Rightarrow f(x) = 6 \chi^5$$

$$- f(x) = K \times^{n} \Rightarrow f(x) = K_{*n} \times^{n-1}$$

$$f(x) = 5x^{3} + 5 \Rightarrow f(x) = 5 *_{3} \times^{2} + 0 = 15 \times^{2}$$

$$= 30 \times_{A} - 9 \times_{S} + 18 \times$$

$$= 18 \times_{A} - 9 \times_{S} + 18 \times_{A} + 18 \times_{S} + 18 \times_{A} +$$

$$- f(x) = \frac{g(x)}{h(x)} \Rightarrow \frac{h(x) g(x) - g(x) \cdot h(x)}{(h(x))^2} = f(x)$$

$$f(x) = \frac{\chi_{5}+1}{3\chi_{5}+\chi-5} \implies f(x) = \frac{(\chi_{5}+1)_{5}}{(\chi_{5}+1)_{6}(2\chi_{7}+2)(3\chi_{5}+\chi-5)(5\chi+6)}$$

$$= \frac{(x^{2}+1)(6x+1) - (3x^{2}+x-2)(2x)}{(x^{2}+1)^{2}}$$

$$= \frac{6x^{3}+x^{2}+6x+1-6x^{3}-2x^{2}+ux}{(x^{2}+1)^{2}}$$

$$= \frac{-x^{2}+10x+1}{(x^{2}+1)^{2}}$$

$$= \frac{-(x^{3}+x^{2}+6x+1)}{(x^{2}+1)^{2}}$$

$$= \frac{-(x^{3}+x^{2}+6x+1)}{(x^{3}+1)^{2}}$$

$$= \frac{-$$

$$-f(x) = K \Rightarrow f(x) = k \qquad g(x) \qquad \ln k$$

$$f(x) = 5 \Rightarrow f(x) = 5 \qquad (6x + 0) \cdot \ln 5$$

$$= 5 \qquad (6x^{3} + 1) \qquad (6x^{2} + 1) \cdot \ln 5$$

$$-f(x) = e^{g(x)} \Rightarrow f(x) = e^{g(x)} \cdot g(x)$$

$$f(x) = e^{3x} \Rightarrow f(x) = e^{3x} (-3) = -3e^{3x}$$

$$-f(x) = \ln(g(x)) \Rightarrow f(x) = \frac{g(x)}{g(x)}$$

$$f(x) = \ln(5x^{2} + 3x) \Rightarrow f(x) = \frac{\log(x)}{g(x)}$$

Differentiation of Trigonometric Functions:

$$-f(x) = \sin x \Rightarrow f(x) = \cos x$$

$$f(x) = Sin 5x \Rightarrow f(x) = Cos 5x * 5 = 5 (os 5x)$$

$$- f(x) = \cos x \implies \hat{f}(x) = -\sin x$$

$$f(x) = \cos(3x^2) \Rightarrow f(x) = -\sin(3x^2) * 6x = -6x \sin(3x^2)$$

$$- f(x) = fan x \Rightarrow f(x) = Sec^2 x$$

$$f(x) = fan X \Rightarrow f(x) = Sec^2 X * 1 = Sec^2 X$$

$$- f(x) = cot x \Rightarrow f(x) = -csc_x$$

$$f(x) = \cot x^2 \Rightarrow \hat{f}(x) = -\csc^2 x^2 * 2x = -2x \csc^2 x^2$$

- 
$$f(x) = cscx \rightarrow f(x) = -cotx cscx$$

$$f(x) = csc3x^2 \rightarrow f(x) = -cot(3x) csc(3x^2). \ \delta x$$

$$= -6 \times cof(3 \times s) CSC(3 \times s)$$

Partial derivatives of functions with two variables:-

Ex: Find 
$$\frac{\partial f}{\partial x}$$
 and  $\frac{\partial f}{\partial y}$  if  $f(x,y) = 2 - x^2 - 3y^4 - \frac{x^3}{y^3}$ 

501:

$$=-5x-\frac{2}{3x_{5}}$$

$$=-5x-\frac{2}{3x_{5}}$$

$$\frac{\partial\lambda}{\partial t} = 9 - 0 - 15\lambda_3 - \frac{\lambda_5}{x_3}$$

501:

$$\frac{\partial z}{\partial x} = e^{2X} \frac{2X + 0 - [X * 0 + Siny * 1] + 0}{(X^2 + 2y^2 - X Siny + 1)} + 2e^{2X}$$

$$= e^{2X} \frac{2X - Siny}{(X^2 + 2y^2 - X Siny + 1)} + \ln(X^2 + 2y^2 - X Siny + 1) + 2e^{2X}$$

Partial derivatives of functions with more than two variables:-

$$\int x: \frac{3x}{3b}, \frac{9x}{3\omega}$$

Ex: let 
$$f(x,y,z) = X z^2 + \alpha \overline{n}'(\frac{y}{x})$$
 find  $f_X$ ,  $f_y$ ,  $f_z$ ?

501:

$$f_{X} = Z^{2} \left[ X + \alpha n^{2} \frac{y}{x} \right]$$

$$= Z^{2} \left[ X - \frac{y/x^{2}}{1 + (y/x)^{2}} + 4\alpha n^{2} \frac{y}{x} * 1 \right]$$

$$fy = Z^{2} \left[ x * \frac{1/x}{1 + (y/x)^{2}} + fan \frac{y}{x} * 0 \right]$$

$$= Z^{2} * x * \frac{1/x}{1 + (\frac{y}{x})^{2}}$$