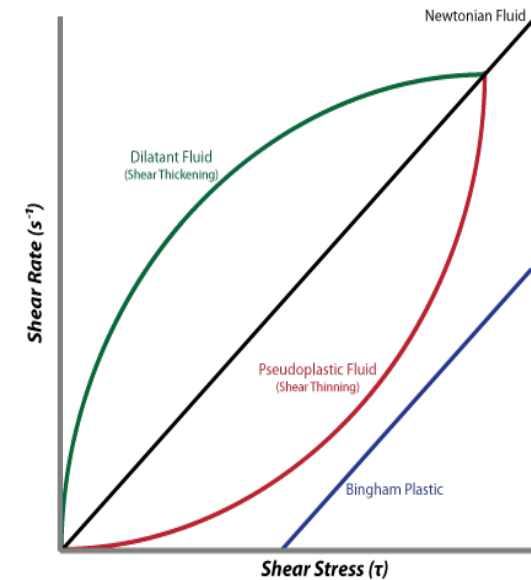


Fluid Mixing

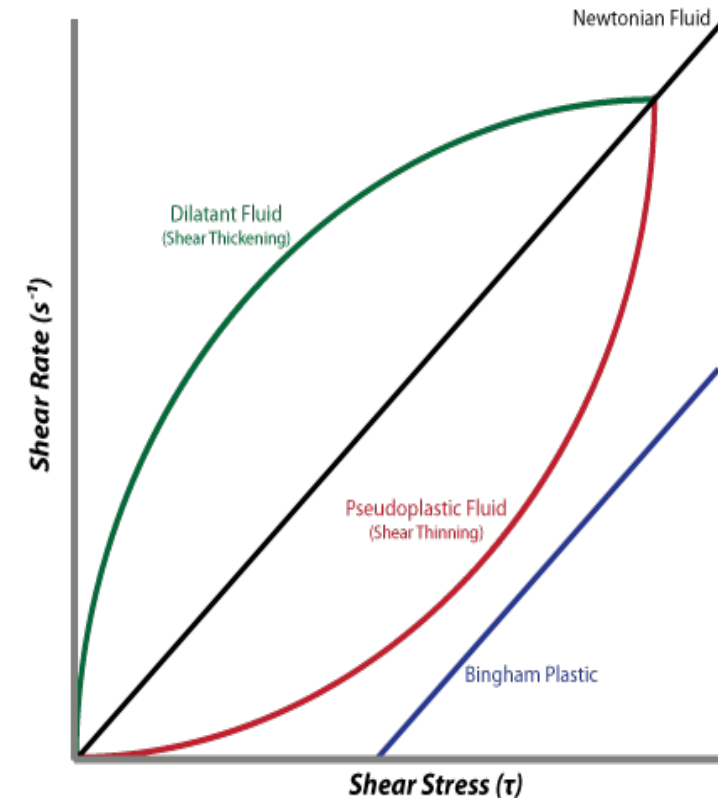
Flow Characteristics

- Fluids may be generally classified as **Newtonian and non-Newtonian**, depending on the relationship between their **shear rates and the applied stress**.
- The rate of shear may be defined as the **derivative of velocity with respect to distance measured normal to the direction of flow**.
- The **viscosity** is the ratio of shear stress to the shear rate.
- **Forces of shear** are generated by interactions between moving fluids and the surfaces over which they flow during mixing.



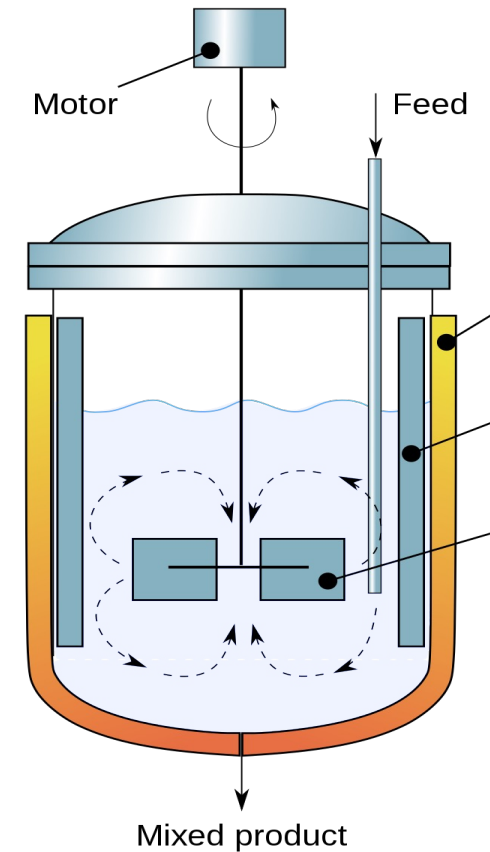
Flow Characteristics

- **Newtonian Fluid:**
- The rate of shear is **proportional to** the applied stress, and such fluids have a dynamic viscosity that is **independent** of the flow rate.
- Like **water** where **constant** viscosity; → the rate of shear increases with shear stress
- **Non-Newtonian fluid:**
- Apparent dynamic **viscosity is a function of the shear stress**. Such as
 1. **Plastic flow:** a fluid **after a certain shear stress limit**
 2. **Pseudoplastic flow:** (shear **thinning** behavior)
 3. **Dilatant flow** (shear **thickening** behavior)



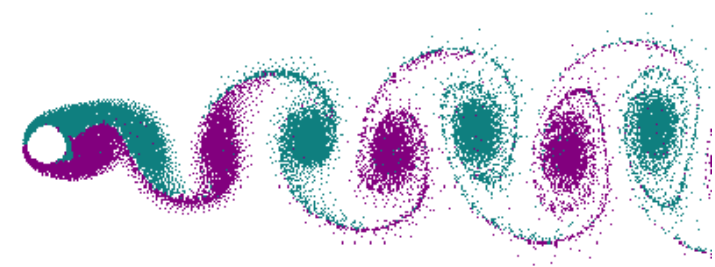
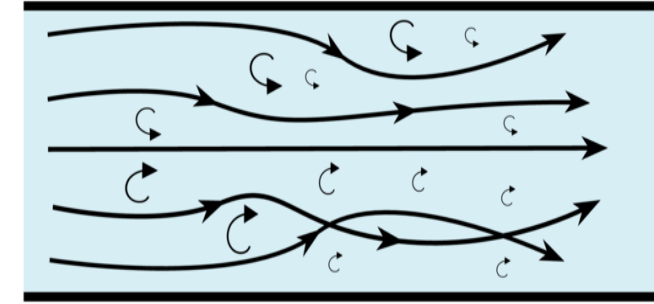
Liquid Mixing Mechanisms

- **Mixing Mechanisms:** can be divided into four mechanisms and usually more than one of them occurs in the mixing of liquid:
- **First: Bulk transport**
 - Movement of a **large portion** of liquid to be mixed from one location to another.
 - However, this mechanism **leaves a part** of the liquid within the **moving material** unmixed.
 - → A simple circulation of material **does not necessarily** result in efficient mixing.
- This mechanism is usually accomplished using paddles, revolving blades, and other devices.



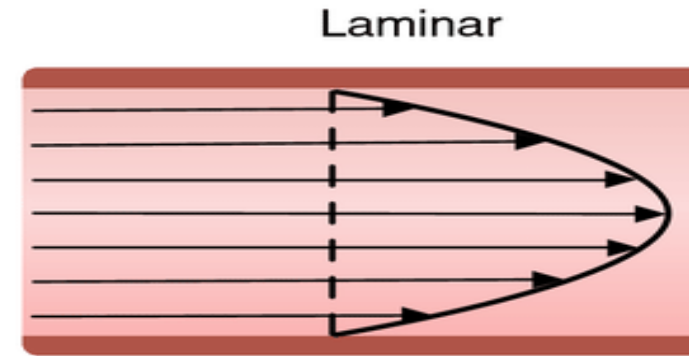
Liquid Mixing Mechanisms

- **Second: Turbulent mixing**
- This resulted directly from the **turbulent fluid flow** which is characterized by the **random fluctuation of fluid velocities** at any given point within the system.
- In this mechanism, fluid movement (mixing) can be visualized as a movement of **portions of various sizes (eddies)** that move together.
- **Eddy** is defined as a portion of fluid moving as a unit in a direction often **contrary** to that of the general flow.
- Larger eddies **tend to break up** forming smaller eddies until they are **no longer distinguishable**.



Liquid Mixing Mechanisms

- **Third: Laminar flow (streamline)**
- This type of flow happens when:
 1. Mixing **highly viscous fluids**.
 2. It can also occur if **stirring** is relatively gentle (**moderate or slow**)
 3. May exist **adjacent to stationary surfaces** in vessels in which the flow is predominantly turbulent.
- This can be described by **layers of the fluid** moving into another fluid.
- When two dissimilar liquids are mixed through laminar flow, the **shear that is generated** stretches the **interface** between them.
- https://youtu.be/_dbnH-BBSNo?si=L-9q-ohIymEs998J



Liquid Mixing: Laminar Flow

- When 2 dissimilar liquids are mixed through laminar flow, the shear that is generated **stretches** the interface between them. → If the mixer employed **folds** the layers back upon themselves, the number of layers & hence the interfacial area between them **increases exponentially with time**.
 - This relationship is observed **because** the rate of increase in interfacial area with time is proportional to the instantaneous interfacial area.

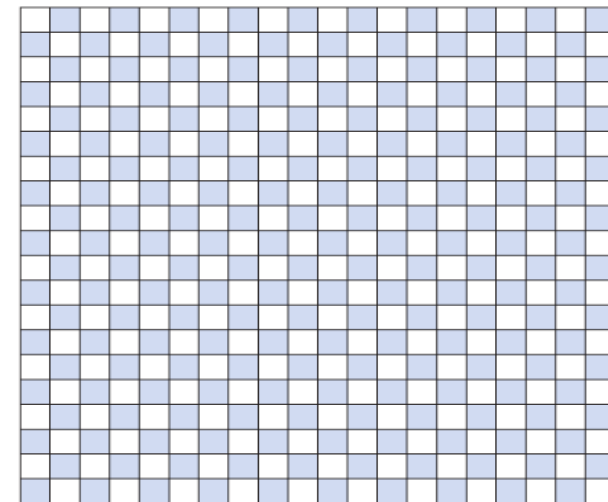
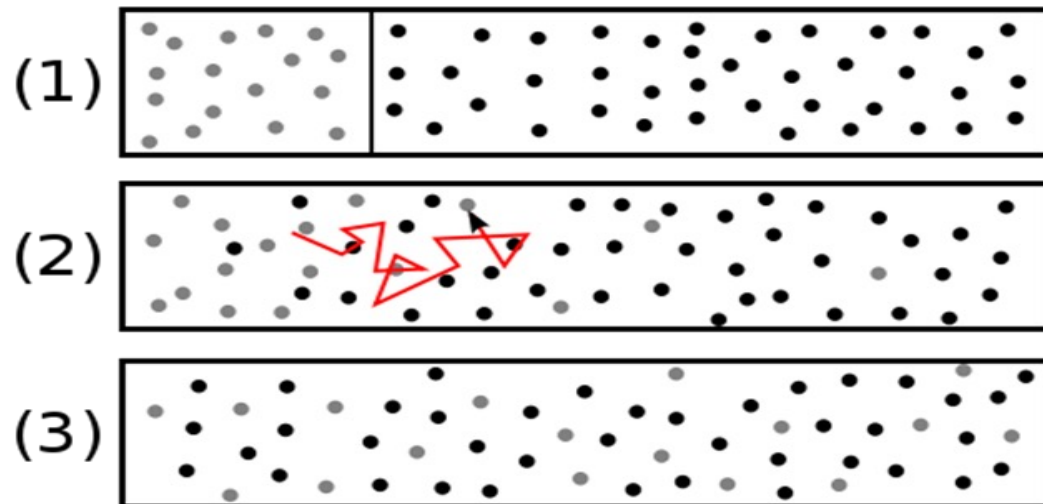


Laminar Flow: Example

- Consider the case where the mixer produces a folding effect & generates a **complete fold** every 10 seconds.
- Given an initial fluid layer thickness of **10 cm**, a thickness reduction by a factor of 10^{-8} is **necessary** to attain layers **1 nm** thick (**which approximate molecular dimensions ≈ 1 nm**). Since a single fold results in a layer thickness reduction of one-half, \rightarrow **n** folds are required where:
 - $(1/2)^n = 10^{-8} \rightarrow$ take log of both sides (since $\text{Log}(X)^y = y \text{Log} X$), $\text{Log} 10 = 1$
 - $\log(1/2)^n = n \log 1/2$ **and** $\log 10^{-8} = -8 \rightarrow n \log(1/2) = -8 \rightarrow$
 - $n = -8 / (\log 1/2) = -8 / -0.3 = 26.6$ folds required to get 1 nm
- **Since each fold requires 10 seconds \rightarrow total time required for mixing (equal to **n times 10 seconds**) = $26.6 * 10 = 226$ sec or **4.43 minutes****
- **Good mixing** at the molecular level **requires** a significant contribution by molecular diffusion **after** the layers have been reduced to reasonable thickness by laminar flow.

Liquid Mixing: Molecular Diffusion

- **Fourth: Molecular diffusion.**
- Mixing of **molecules** of one fluid through another by random **molecular motion**.
- The **primary mechanism** responsible for mixing at the molecular level is diffusion resulting from the thermal motion of the molecules when it occurs in conjunction **with laminar flow**.
- In this mechanism, molecules move according to the **concentration gradients** until they result in complete mixing.



Liquid Mixing: Molecular Diffusion

- Molecular diffusion tends to reduce the sharp discontinuities at the interface between the fluid layers and if allowed to proceed for sufficient time result in complete mixing.
- The process described by Fick's 1st law of diffusion (substances will diffuse from areas of high concentration to lower concentration)

$$dm/dt = -DA dc/dx$$

- The rate to mass transfer (dm/dt) across an interface of area **A** is proportional to the concentration gradient (dc/dx) across the interface
- **D** (diffusion coefficient) depends on the viscosity and the size of the diffusing molecules.
- The concentration gradients at the original boundaries are a decreasing function of time, approaching zero as mixing approaches completion.

Mixing Evaluation

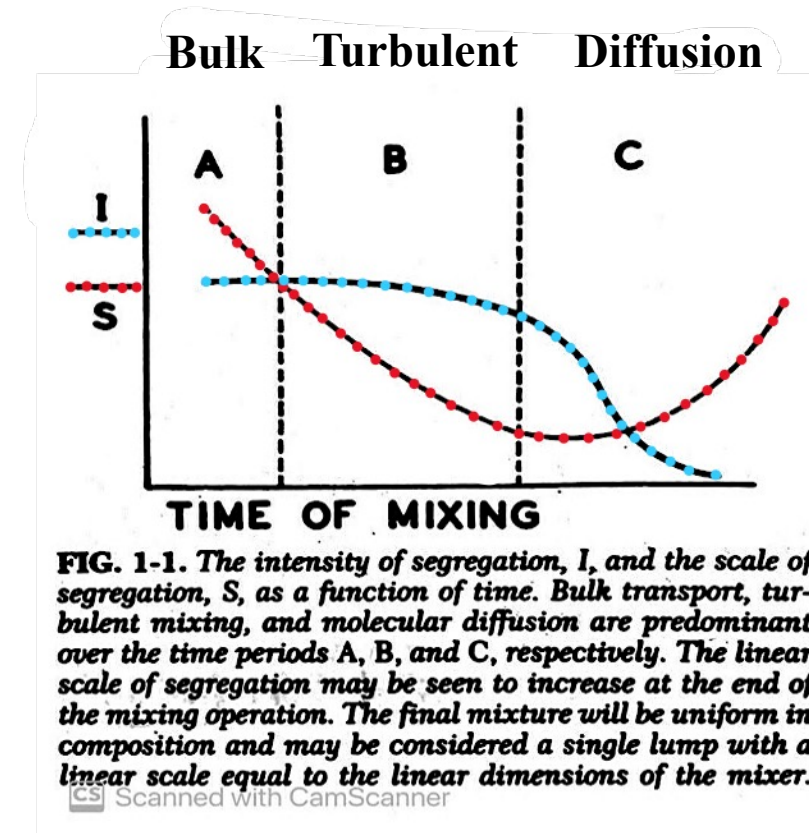
- It is important to examine each mixture during the mixing process to ensure that we have enough mixing (i.e. random mixing).
- Danckwerts has suggested **2 criteria** to describe the degree of mixing (quality of randomness or goodness of mixing)

1. The scale of segregation:

- Scale of segregation is expressed in 2 ways either linear or volume scale.
- The linear scale represents the average value of the diameter of the lumps whereas the volume scale represents the average lump volume.

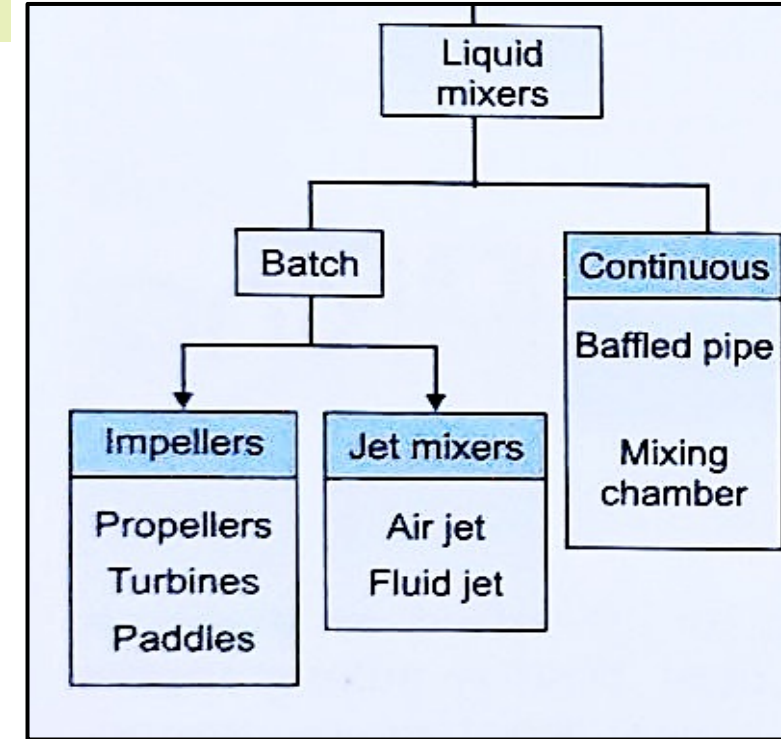
2. Intensity of segregation is a measure of the variation in composition among the various portions of the mixtures.

- Variation **will be zero** at the end of the mixing



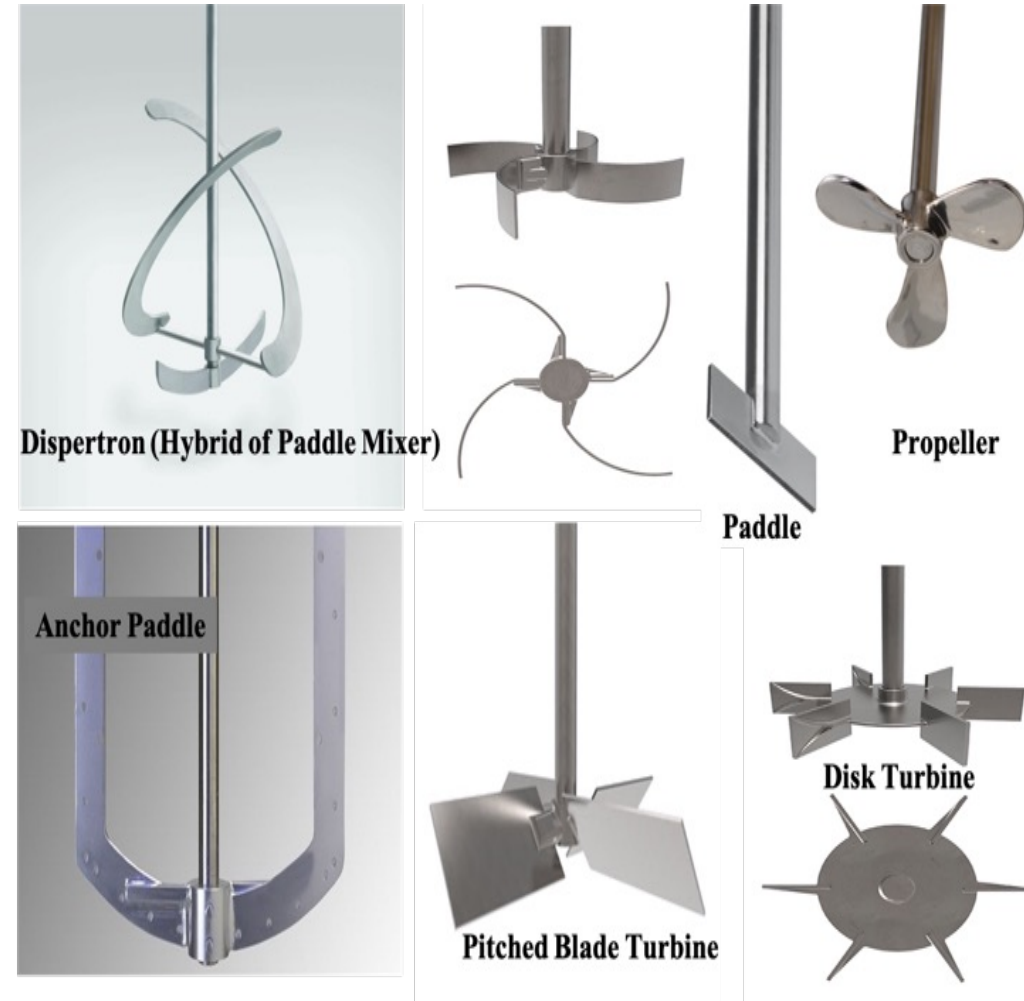
Equipment for Fluid Mixing

- Generally, fluid mixers consist of a:
 1. **Tank or a container** to hold the material being mixed and
 2. A suitable **energy transfer tool** such as an **impeller, liquid jet, or air stream**.
 - Besides supplying power, these tools also serve to direct the flow of material within the vessel.
- **Baffles, vanes, and ducts** are also used to direct the bulk movement of material in such mixers, thereby increasing their efficiency.
- When the material to be mixed is **limited in volume** so that it may be conveniently contained in a suitable mixer, **batch mixing** is usually more feasible.
- However, for **larger** volumes, **continuous mixing** is preferred.



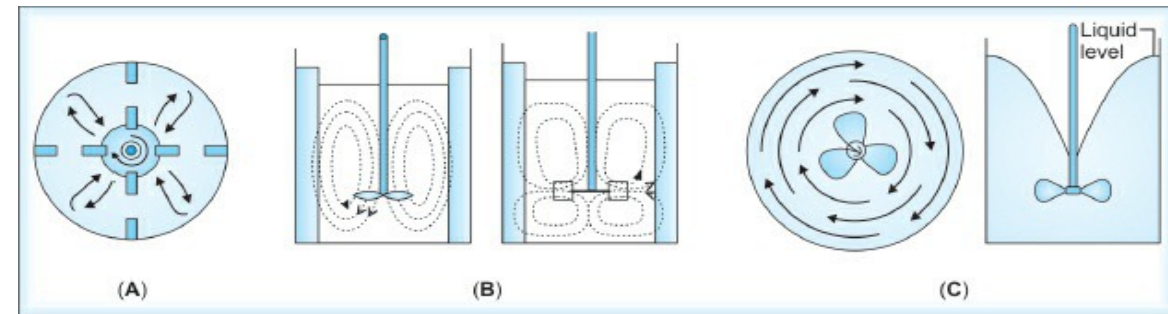
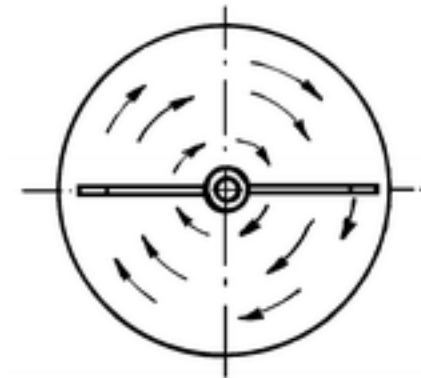
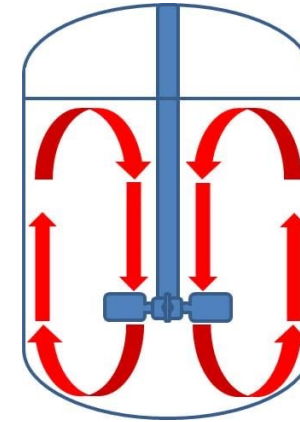
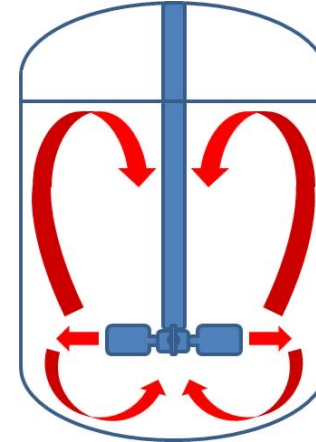
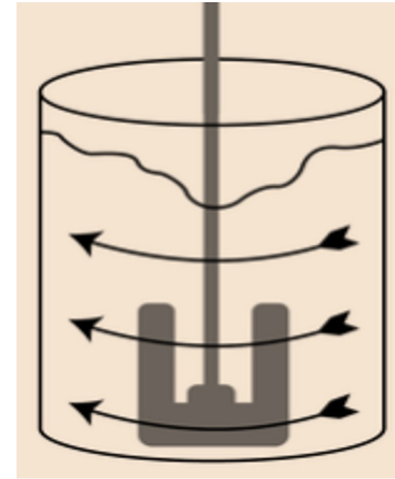
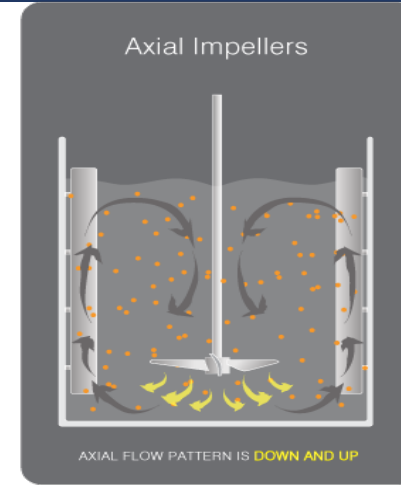
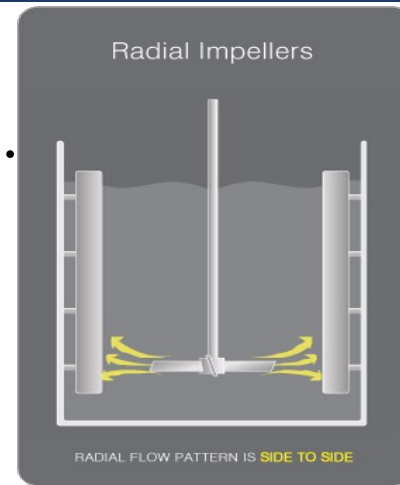
Batch Mixers

- **Batch mixers** are used for **small volumes** and they are either **impellers** or **jet mixers**.
- **Impellers:** these are the **main** mixing units in fluid mixers. It can be either **propellers**, **turbines**, or **paddles**.
- The **distinction** between impeller types is on the basis of:
 1. The type of **flow pattern** they produce, or
 2. The **shape and pitch** of the blades.
- These impellers cause turbulence and prevent the formation of dead zones.



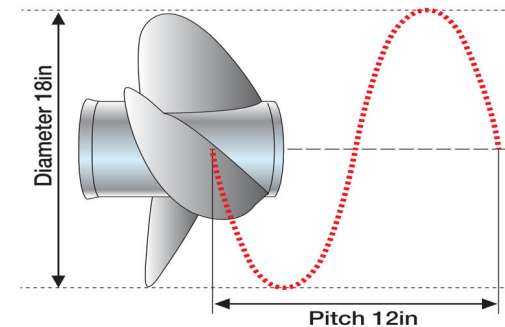
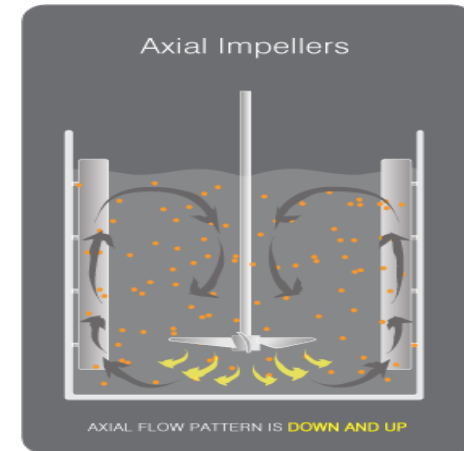
Types of flow in liquid

- The impellers **create a current or stream** of liquid that moves in all places of the tank.
- The flow pattern may be analyzed in terms of three components:
 1. **Radial:** **perpendicular** to the impeller shaft.
 2. **Axial or longitudinal (down and up):** **parallel** to the impeller shaft.
 3. **Tangential:** **tangential** to the circle of rotation around the impeller shaft.
- These may occur singly or in various combinations.



Impeller Batch Mixer: Propellers

- **Propellers** of various types and forms are used.
- Also, like the machine screws, propellers may be either right- or left-handed depending on **the direction of the slant of their blades**
- The **primary effect** is due to **axial flow**, **however**, some tangential flow does occur.
 - Also, **intense turbulence** usually occurs in the immediate vicinity of the propeller.
- Propellers are more efficient when they are run at **high speed** in liquids with **low viscosity**.

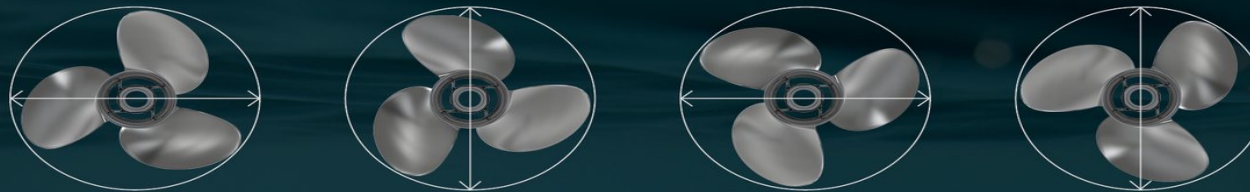


Impeller Batch Mixer: Propellers

- Although **any number** of blades may be used, the **three-blade design** is most commonly used with fluids.
- The blades may be set at any angle or pitch but for **most applications**, the **pitch** is approximately **equal to the propeller diameter**.

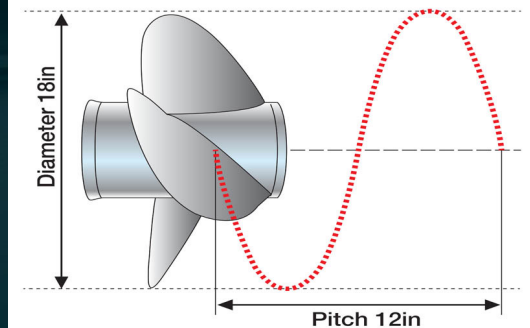
DIAMETER

Diameter is the distance across the circle made by the blade tips as the propeller rotates.



PITCH

Pitch is the distance that a propeller would move in one revolution if it were moving through a soft solid, like a screw in wood.



 **MERCURY**
GO BOLDLY.

Impeller Batch Mixer: Turbines

- They are usually distinguished from propellers in that the blades of the propeller **do not** have a constant pitch throughout their length
- When **radial-tangential** flow is desired, turbines with blades set at a **90-degree** angle to their shaft are employed
 - With these types of impellers, a radial flow is induced by the centrifugal action of the revolving blades
- **If** the turbine blade is **tilted** → it will produce **additional** axial flow **similar to the propeller**.
- Because they lend themselves to a simple and rugged design, these turbines can be operated satisfactorily in fluids **1000 times more viscous** than fluids in which a propeller of comparable size can be used.

• <https://youtu.be/kobc3DdaofE>

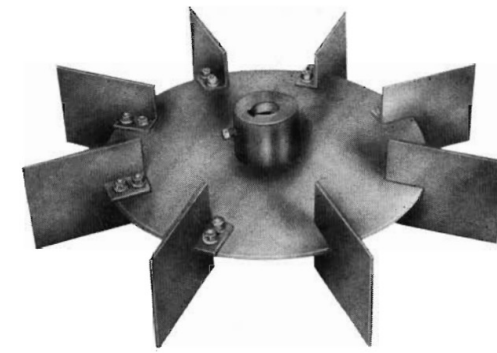
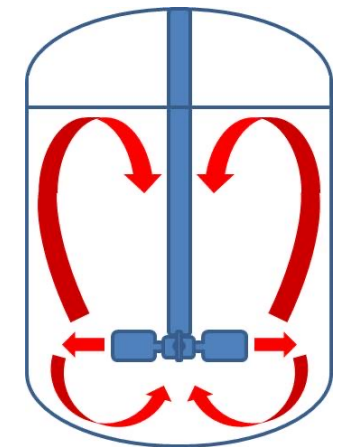
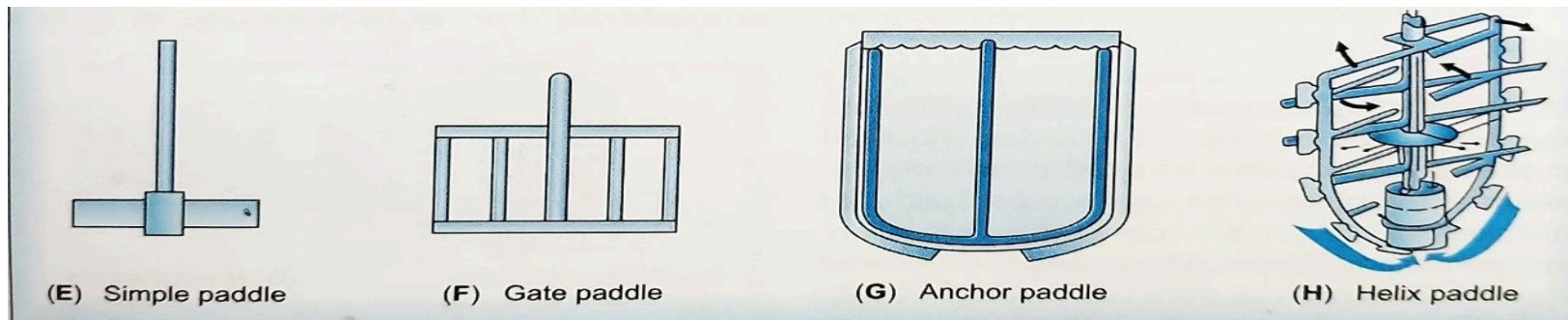


Fig. 2—Flat-blade turbine.



Impeller Batch Mixer: Paddles

- Normally operated at low speed (**lower than 50 rpm**).
- Their **blades have a large surface area** as compared to the tank in which they are employed → **they pass close to the tank walls** and **effectively mix viscous** fluids and **semisolids** which tend to cling to these surfaces.
- Circulation is primarily **tangential**, and consequently, **concentration gradients** (not complete mixing) in the axial and radial directions may persist in this type of mixer **even after** prolonged operation.
- Operating procedures should take these characteristics into account. With such mixers, for example, **ingredients should not be layered** when they are added to the mixing tank.



Figs 1.3A to H: Impeller blade types: (A) Propeller; (B-D) Turbines; (E-H) Paddles

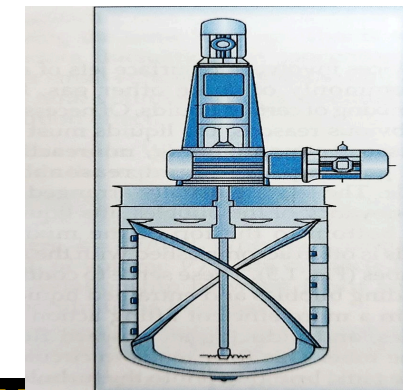
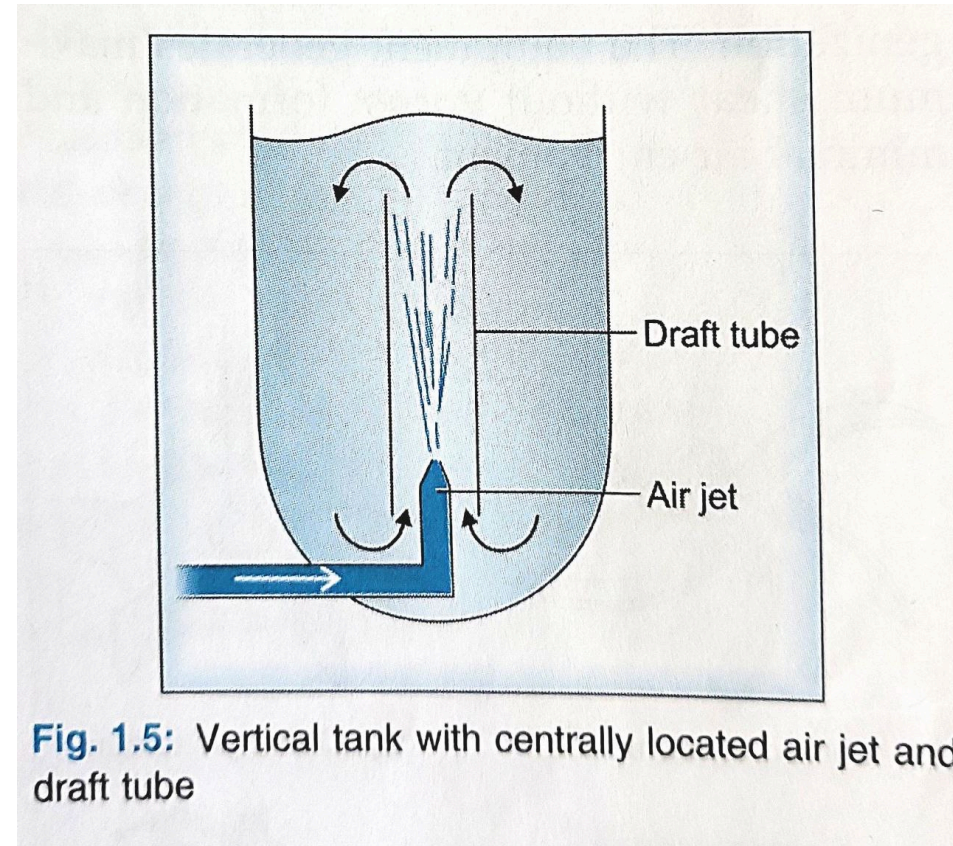


Fig. 1.4: Dispertron: Hybrid of paddle mixer

- **Air Jets** is a sub-surface stream of **air** or other gasses used to mix the fluids.
- Fluids should be of:
 1. **Low viscosity,**
 2. **Nonfoaming,**
 3. **Nonreactive** with the gas (or air),
 4. And **reasonably nonvolatile.**
- The jets are usually arranged so that the buoyancy of the bubbles lifts liquids from the **bottom to the top of the mixing vessel.**



- This is often accomplished with the aid of **draft tubes**.
 - These serve to **1- confine the expanding bubbles** and **2- entrained liquids**, → resulting in a more efficient lifting action by the bubbles, and inducing an upward fluid flow in the tube.
- This flow tends to **circulate fluid in the tank**, → bringing it into the turbulent region in the vicinity of the jet.
- The overall circulation in the mixing vessel brings fluid from **all parts** of the tank to the region of the jet itself.
- → Here, the intense turbulence generated by the jet produces intimate (deep) mixing

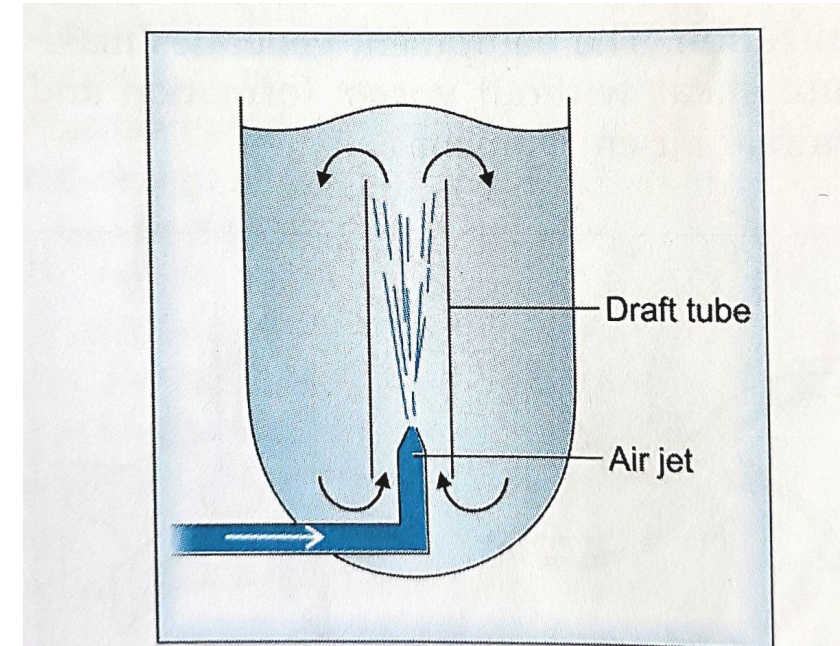
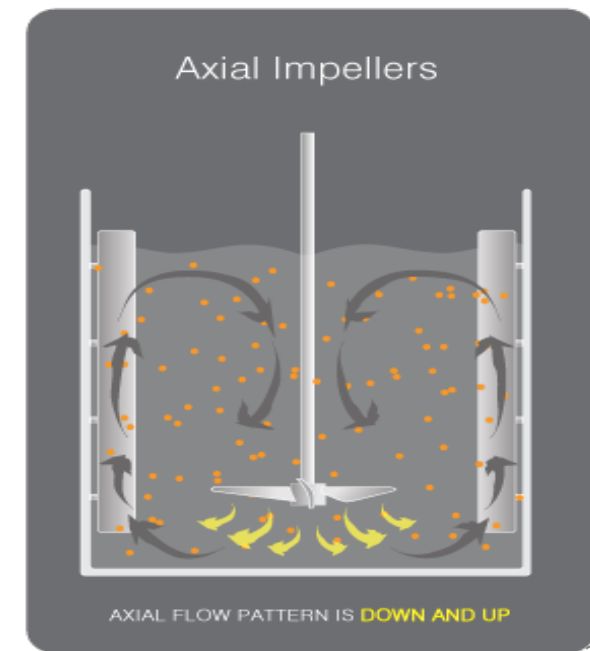
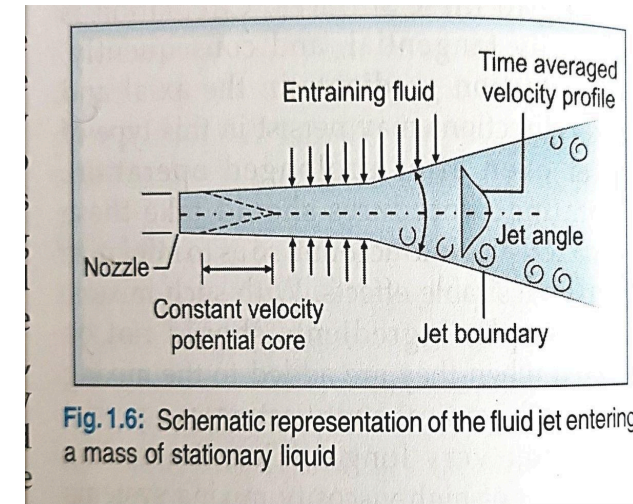


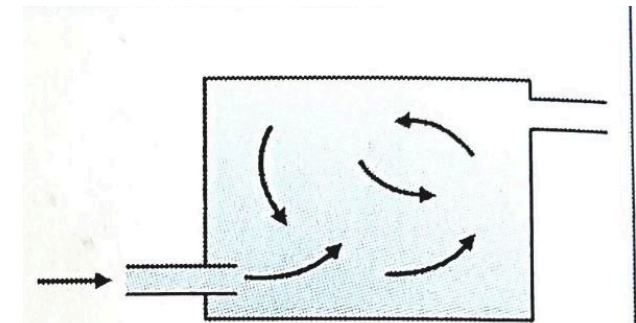
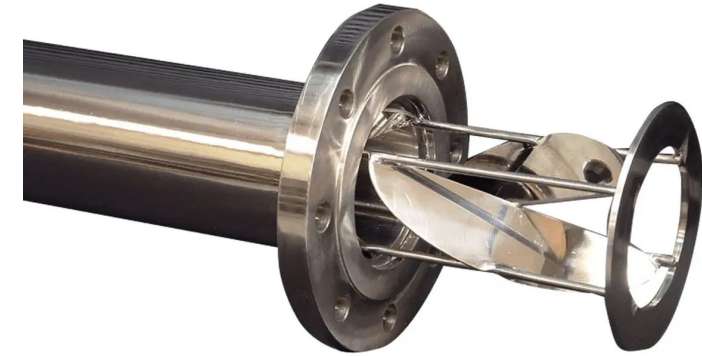
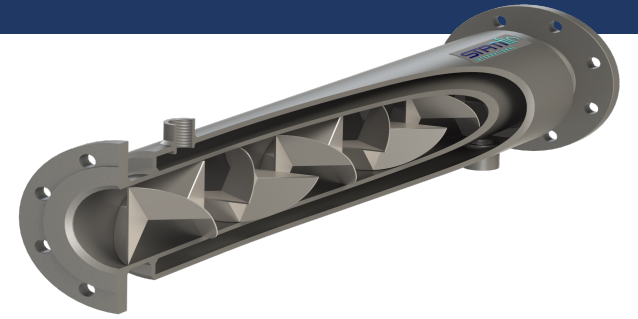
Fig. 1.5: Vertical tank with centrally located air jet and draft tube

- **Fluid jet:** liquid at high pressure is pumped into the tank.
- The power required for pumping can often be used to accomplish the mixing operation, either partially or completely.
- In such a case, the fluids are pumped through nozzles arranged to permit a good circulation of material throughout the tank.
- In operation, fluid jets behave somewhat like propellers and they generate turbulent flow axially.
 - However, they do not themselves generate tangential flow, like propellers.
- Jets also may be operated simply by pumping liquid from the tank through the jet back into the tank



Continuous or In-line Mixers

- **Advantage:** The process of continuous mixing produces an uninterrupted supply of freshly mixed material and is often desirable when **very large volumes** of materials are to be handled.
- It can be accomplished essentially in two ways:
 1. In a tube or pipe (**baffled pipe mixers**) through which the material flows and in which there is very **little backflow or recirculation**,
 2. Or in a **mixing chamber mixers** in which a considerable amount of holdup and recirculation occurs.
- To ensure good mixing efficiencies, devices such as vanes, baffles, screws, grids, or combinations of these are placed in the mixing tube.



(B) Mixing chamber

Practical Considerations: Vortexing

- **Vortexing**: a vortex develops at the **center of the vessel** when liquids are mixed by **centrally-mounted vertical shaft** impellers.
- This particularly is characteristic of the **turbine** with blades arranged perpendicular to the impeller shaft.
- The **tangential flow** will cause a centrifugal force that may cause vortexing to happen. This is why tangential flow is **not recommended**.
- The tangential flow **will not** result in **any mixing** except possibly near the **tank walls** where shear forces exist.
 - Except in the case of **very low impeller speeds** or at **very high liquid viscosities** (above 20000 cps). However, these cases are **not common** in the pharmaceutical industry.

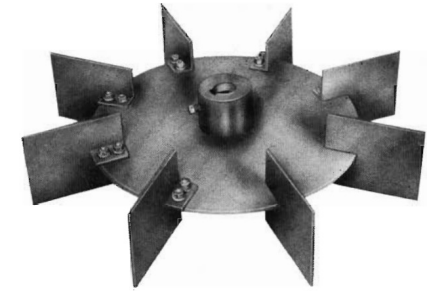


Fig. 2—Flat-blade turbine.

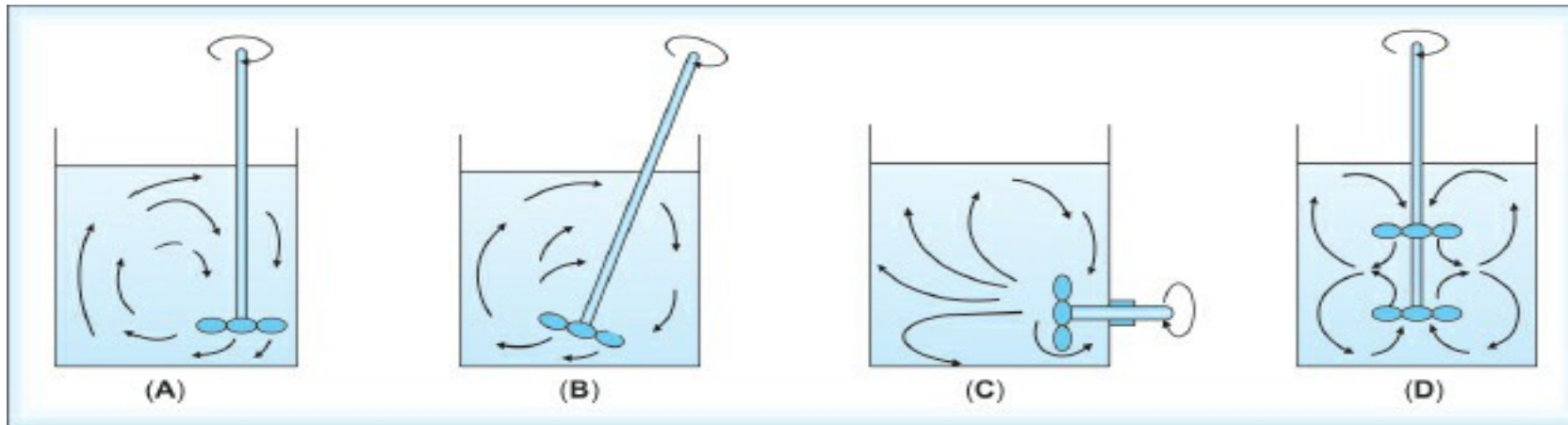


Practical Considerations: Vortexing

- Vortexing is **not recommended** in mixing due to:
 1. **Does not cause real mixing**. The full power of the impeller is **not** imparted to the liquid.
 2. **Air is drawn onto the impeller** and is dispersed into the liquid, which may lead to **foaming**, especially if surfactants are present.
 3. The **entrapped air may cause oxidation** or it can reduce the mixing intensity by reducing the velocity of the impeller relative to the surrounding fluid.

Vortex can be avoided by:

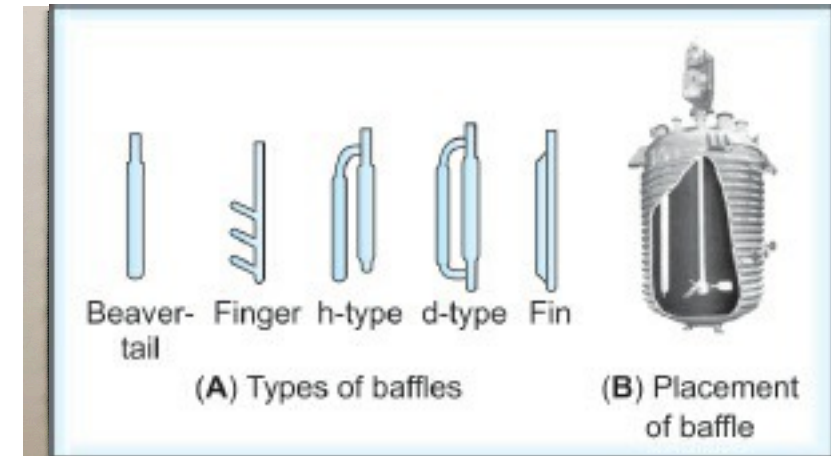
1. Changing the arrangement of the impellers: mounting the impellers off-center or inclined or side position.
2. Changing tank geometry. Asymmetric or angular geometry **but** this will increase the **time** required for mixing since there will be areas in the tank in which the circulation is poor.
3. Using a push-pull propeller: two propellers of **opposite** pitch are mounted on the same shaft to the rotary effects are in opposite directions → and cancel each other.



Figs 1.10A to D: Different arrangements of impellers in a vessel with flow pattern to prevent vortex: (A) Off-centre; (B) Inclined; (C) Side-entering; (D) Push-pull propeller

Vortex can be avoided by

- Using **baffles**: these plates will convert tangential flow into an axial flow.
- Use of diffuser/stator ring**: that fits around the impeller.



Figs 1.11A and B: Various types of commercially available baffles: (A) Types of baffles; (B) Placement of baffle



- Comparative mixing characteristics of various types of impellers

Parameter	Propellers	Turbines	Paddles
Primary flow pattern	Axial	Radial and tangential, axial (with pitched-blade turbines)	Tangential
Operational speed	High, up to 8,000 rpm	Low, 50–200 rpm	Low, < 100 rpm
Ratio of container-to-impeller blade	Large, ~ 20	Intermediate, ~ 2 to 3	Small, ~ 1.1
Pitch	Not constant	Constant	Constant
Vortex formation	Intensive	Moderate	Does not occur
Application	Positive mixtures: Solutions, elixirs	Negative mixtures: Suspensions, emulsions	Neutral mixtures: Gels, pastes, ointments
Limitations	Suitable only for liquids with low viscosity, < 5 pascal.seconds slurry of 10% solids	Suitable for liquids with moderate viscosity, ~700 pascal.seconds slurry of 60% solids	Suitable for liquids with comparative higher viscosity, > 700 pascal.seconds

Mixer selection

- **Selection will depend on:**
 1. **Physical properties** of the materials to be mixed, such as density, viscosity, and miscibility.
 2. **Economic considerations** regarding processing for example the **time required** for mixing and the power expenditure necessary.
 3. **Cost and maintenance** of the equipment.
- However, the selection of equipment depends **primarily** upon the **viscosity of the liquids** and is made according to the mechanism by which intense shearing forces can best be generated.

- **Low Viscosity Systems:**
- Fluids of relatively low viscosity encounter no problems during mixing except when the operational scale is very large.
- Low-viscosity monophasic fluids are **best mixed by the method that:**
 1. Generates a **high degree of turbulence** &
 2. At the same time circulates the entire mass of material.
- These requirements are satisfied by **air jets, fluid jets** & various **high-speed** impellers.
- A viscosity of approximately **10 poise** may be considered as a practical **upper limit** for the application of these devices.

- **High Viscosity Systems:**
- **Thick creams & ointments & pastes** are of such **high viscosity** that is **difficult** if not impossible to **generate turbulence** within their bulk & laminar mixing.
- This means molecular diffusion is very important here.
- Mixing may be done with a **turbine of flat blade design**.
 - The power consumption of these devices is **insensitive** to density and/or viscosity.
 - They are a good choice when emulsification or added solids may change these quantities (viscosity and density) during the mixing.

- The mixing of **2 immiscible** liquids requires the **subdivision** of one of these phases into **globules**, then distributed throughout the bulk of the fluid.
- These globules are successively broken down into smaller ones.
- Two primary forces play here:
 1. **The interfacial tension** of the globules in the surrounding liquid and
 2. **Forces of shear** within the fluid mass.
- The first force tends to **resist** the distortion of globule shape fragmentation to small globules whereas the **opposite** with the 2nd force.
- The selection of equipment depends upon the **viscosity** of the liquids and this is made according to the mechanism by which intense shearing forces can best be generated.

- In the case of **low-viscosity systems**, high shear rates are required and produced by passing the fluid under high pressure through small orifices or by bringing it into contact with rapidly moving surfaces.
- **Highly viscous fluids**
- Such as the ones encountered in the production of **ointments**, are efficiently dispersed by the shearing action of **2 surfaces** in close proximity and **moving at different velocities** with respect to each other.
- This is achieved in **paddle mixers** in which the blades clear out the **walls**.
- These mixers generate shear to reduce globule size and induce sufficient circulation of materials to ensure efficient mixing.

- The mixing of **finely divided solids with a liquid** of low viscosity in the production of a **suspension** depends on the separation of aggregates & distribution of these particles in the fluid.
- This process occurs in a **single mixing operation** provided that shear forces of sufficient to disrupt aggregates.
- As the % of solids is increased or if highly viscous fluids are employed, → the solid-liquid system takes on the consistency of a paste or dough. →
 - The choice of mixer is either **knead or mull** the materials.
 - **Kneaders** operate by pushing the material by squeezing & deforming them at the same time. Such mixers take several forms.
 - Usually have **counter-rotating blades or heavy arms** that work the plastic mass. Shear forces are generated by the high viscosity of the mass & are effective in the deaggregation & distribution of the solids in the fluid vehicle.