

P. 2-1. Sol 200

$$\text{Power (P)} [ML^2T^{-3}]$$

$$\text{Density } (\rho) [ML^{-3}]$$

$$\text{r.p.m (N)} [T^{-1}]$$

$$\text{Diameter (D)} [L]$$

$$\text{gr. acc. (g)} [LT^{-2}]$$

$$\text{Head (H)} [L]$$

$$P = f(\rho, N, D, g, H)$$

$$P = K(\rho^a, N^b, D^c, g^d, H^e)$$

$$[ML^2T^{-3}] = [ML^{-3}]^a [T^{-1}]^b [L]^c [LT^{-2}]^d [L]^e$$

$$\text{For } M \Rightarrow 1 = a \Rightarrow a = 1$$

$$\text{For } T \Rightarrow -3 = -b - 2d \Rightarrow b = 3 - 2d$$

$$\text{For } L \Rightarrow 2 = -3a + c + d + e$$

$$c + d + e = 5 \Rightarrow c = 5 - d - e$$

$$P = K(\rho^1, N^{3-2d}, D^{5-d-e}, g^d, H^e)$$

$$P = (\rho N^3 D^5) K \left[\left(\frac{g}{N^2 D} \right)^d \left(\frac{H}{D} \right)^e \right]$$

$$P = (\rho N^3 D^5) f \left[\frac{g}{N^2 D}, \frac{H}{D} \right] \times \frac{g H}{N^2 D^2} \times \frac{N^2 D^2}{g H} \quad (A)$$

multiple $\frac{N^2 D^2}{g H}$ since it is dimensionless group

$$P = (\rho N^3 D^5) f \left[\frac{H}{D}, \frac{N^2 D^2}{g} \right]$$

$$\therefore P = (\rho N^3 D^5) f \left[\frac{N^2 D^2}{g H} \right]$$

P 4.16. solⁿ -

$$\phi Re^2 = \frac{-\Delta P d^3 P}{4L\mu^2}$$

$$= \frac{(8000)(0.025)^3(1000)}{(4)(5)(1 \times 10^{-3})^2} = 6.25 \times 10^6$$

From 3-8 $\Rightarrow Re = 5 \times 10^4$

$$u = \frac{(5 \times 10^4)(10^{-3})}{(2000)(0.025)} = 2 \text{ m/s}$$

$$Q = \frac{2\pi}{4} (0.025)^2 = 0.982 \times 10^4 \text{ m}^3/\text{s}$$

$$\text{total } Q = \frac{10(1000)}{(2000)(3600)} = 0.3056 \text{ m}^3/\text{s}$$

$$\text{no. of tubes req.} = \frac{0.3056}{0.982 \times 10^4} = 31.1 \text{ tubes}$$

velocity of fluid if they are blocked

$$= \frac{2}{0.9} = 2.22 \text{ m/s}$$

$$Re = \frac{5 \times 10^4}{0.9} = 5.5 \times 10^4$$

From 3-7 $\phi = 0.00245$

$$\Delta P = (4)(0.00245) \left(\frac{5}{0.025} \right) (1000)(2.22)^2$$

$$= 9650 \text{ Pa}$$

P. 2.2. Sol 30

Resistance (R) $[MLT^{-2}]$

Velocity (u) $[LT^{-1}]$

length (L) $[L]$

Viscosity (μ) $[ML^{-1}T^{-1}]$

Density (ρ) $[ML^{-3}]$

gr. acc. (g) $[LT^{-2}]$

$$R = f(u, L, \mu, \rho, g)$$

$$R = k(u^a L^b \mu^c \rho^d g^e)$$

$$[MLT^{-2}] = [LT^{-1}]^a [L]^b [ML^{-1}T^{-1}]^c [ML^{-3}]^d [LT^{-2}]^e$$

$$\text{For } M \Rightarrow 1 = c + d \Rightarrow c = 1 - d$$

$$\text{For } T \Rightarrow -2 = -a - c - 2e \Rightarrow a = 2 - c - 2e$$

$$a = 1 + d - 2e$$

$$\text{For } L \Rightarrow 1 = a + b - c - 3d + e$$

$$b = e + d + 1 \Rightarrow b = 1 + d + e$$

$$R = k(u^{1+d-2e}, L^{1+d+e}, \mu^{1-d}, \rho^d, g^e)$$

$$R = (\mu L \rho) k \left[\frac{\mu \rho}{\mu} \right]^d \left[\frac{g L}{\mu^2} \right]^e$$

$$R_s (\mu L \rho) f \left[\frac{\mu \rho}{\mu}, \frac{g L}{\mu^2} \right]$$

~~incorrect~~

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~~incorrect~~

P. 2.3. Sol. 1
Discharge

$$(L^3 T^{-1}) = (L)^a (L)^b (ML^{-3})^c (MT^{-1}L)^d (LT^{-2})^e$$

form $\Rightarrow 0 = c + d \Rightarrow c = -d$

For L $\Rightarrow 3 = a + b - 3c - d + e$

For T $\Rightarrow -1 = -d - 2e \Rightarrow d = 1 - 2e$

$2e = -d + 1 \Rightarrow e = \frac{-d}{2} + \frac{1}{2}$

$3 = a + b + 3d - 1 + 2e$

$a = 3 - b - 3d + 1 - 2e$

$a = 4 - b - 3d - 2e$

$\frac{7}{2} \cdot D \cdot D \cdot D \cdot \rho \cdot H \cdot g \cdot \left(\frac{L}{2} \right)$

P. 2.3. Solⁿ.

Discharge (Q) [L³T⁻¹]

Head (h) [L]

Diameter (d) [L]

Density (ρ) [ML⁻³]

Viscosity (μ) [ML⁻¹T⁻¹]

g_{acc.} (g) [LT⁻²]

$$Q = f(M, d, \rho, \mu, g)$$

$$Q = K(M^a, d^b, \rho^c, \mu^d, g^e)$$

$$[L^3T^{-1}] = [L]^a [L]^b [ML^{-3}]^c [ML^{-1}T^{-1}]^d [LT^{-2}]^e$$

$$\text{For } M \Rightarrow 0 = c + d \Rightarrow c = -d$$

$$\text{For } T \Rightarrow -1 = -d - 2e \Rightarrow c = +\frac{1}{2} - \frac{d}{2}$$

$$\text{For } L \Rightarrow 3 = a + b - 3c - d + e$$

$$b = \frac{7}{2} - a - \frac{3d}{2}$$

$$Q = K(M^a, L^{\frac{7}{2} - a - \frac{3d}{2}}) \left(\frac{\mu}{\rho}\right)^d, \left(\frac{g}{\rho}\right)^{\frac{1}{2} - \frac{d}{2}}$$

$$Q = (L)^{\frac{7}{2}} \left(\frac{g}{\rho}\right)^{\frac{1}{2}} K \left[\frac{\mu}{d^{\frac{3}{2}} \rho g^{\frac{1}{2}}}\right]^d, \left(\frac{M}{d}\right)^a$$

$$Q = (L)^{\frac{7}{2}} \sqrt{g} f \left[\frac{\mu}{d^{\frac{3}{2}} \rho g^{\frac{1}{2}}}\right], \left(\frac{M}{d}\right)^a$$

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مع جميع المتغيرات الزمنية
أهم المتغيرات

P.2.4. Sol 8

Force (F) [MLT⁻²]

length (L) [L]

Velocity (u) [LT⁻¹]

viscosity (μ) [ML⁻¹T⁻¹]

Density (ρ) [ML⁻³]

[u, ρ, L]

$$(\varepsilon) = -v \frac{dP}{dx} = (L^3)(ML^{-3}T^{-2})(L^{-3}) = [ML^{-1}T^{-2}]$$

$$n = 6, m = 3, \pi = n - m = 3$$

no. of repeating vars. = 3 = m

repeating vars. (u, ρ, L)

$$F = K(L, u, \mu, \rho, \varepsilon)$$

$$f(F, L, u, \mu, \rho, \varepsilon) = 0$$

$$\pi_1 = u^{a_1} \rho^{b_1} L^{c_1} F$$

$$\pi_2 = u^{a_2} \rho^{b_2} L^{c_2} \mu$$

$$\pi_3 = u^{a_3} \rho^{b_3} L^{c_3} \varepsilon$$

من كل واحد
من المتغيرات
مع المتغيرات
المعادلة (u, ρ, L)

$$\text{for } \pi_1 \rightarrow [M^0 L^0 T^0] = [LT^{-1}]^{a_1} [ML^{-3}]^{b_1} [L]^{c_1} [MLT^{-2}]$$

$$\text{for } M \rightarrow 0 = b_1 + 1 \Rightarrow b_1 = -1$$

$$\text{for } T \rightarrow 0 = -a_1 - 2 \Rightarrow a_1 = -2$$

$$\text{for } L \rightarrow 0 = a_1 + c_1 - 3b_1 + 1 \Rightarrow c_1 = -2$$

$$\therefore \pi_1 = u^{-2} \rho^{-1} L^{-2} F \Rightarrow \pi_1 = \frac{F}{u^2 \rho L^2}$$

$$\text{for } \pi_2 \rightarrow [M^1 T^0] = [LT^{-1}]^{a_2} [ML^{-3}]^{b_2} [L]^{c_2} [ML^{-1}T^{-1}]$$

$$\text{for } M \rightarrow 0 = b_2 + 1 \Rightarrow b_2 = -1$$

$$\text{for } T \rightarrow 0 = -a_2 - 1 \Rightarrow a_2 = -1$$

$$\text{for } L \rightarrow 0 = a_2 - 3b_2 + c_2 - 1 \Rightarrow c_2 = -1$$

$$\therefore \pi_2 = u^{-1} \rho^{-1} L^{-1} \mu \Rightarrow \pi_2 = \frac{\mu}{u \rho L}$$

$$\text{for } \pi_3 \rightarrow [M^0 L^0 T^0] = [LT^{-1}]^{a_3} [ML^{-3}]^{b_3} [L]^{c_3} [ML^{-1}T^{-2}]$$

$$\text{for } M \rightarrow 0 = b_3 + 1 \Rightarrow b_3 = -1$$

$$\text{for } T \rightarrow 0 = -a_3 - 2 \Rightarrow a_3 = -2$$

$$\text{for } L \rightarrow 0 = a_3 - 3b_3 + c_3 - 1 \Rightarrow c_3 = 0$$

$$\pi_3 = u^{-2} \rho^{-1} L^0 \varepsilon \Rightarrow \pi_3 = \frac{\varepsilon}{u^2 \rho}$$

since $f(\pi_1, \pi_2, \pi_3) = 0$

$$\therefore f\left(\frac{F}{u^2 PL^2}, \frac{\mu}{uPL}, \frac{\Sigma}{u^2 P}\right)$$

~~$f(\pi_1, \pi_2, \pi_3)$~~

$$F = (u^2 PL^2) f\left[\left(\frac{\mu}{uPL}\right), \left(\frac{\Sigma}{u^2 P}\right)\right]$$

التيار في الأنابيب

P. 2.5. sol 5

Efficiency η $[M^0 L^0 T^0]$

Density (ρ) $[ML^{-3}]$

Viscosity (μ) $[ML^{-1}T^{-1}]$

Velocity (ω) $[T^{-1}]$

Diameter (D) $[L]$

Discharge (Q) $[L^3 T^{-1}]$

$$\eta = f(\rho, \mu, \omega, D, Q)$$

$$f(\eta, \rho, \mu, \omega, D, Q) = 0$$

$$n = 6, m = 3, \pi = n - m = 3$$

no. of repeating vars. = 3 = m

repeating vars. (ω, D, ρ)

$$\pi_1 = \omega^{a_1} D^{b_1} \rho^{c_1} \eta$$

$$\pi_2 = \omega^{a_2} D^{b_2} \rho^{c_2} \mu$$

$$\pi_3 = \omega^{a_3} D^{b_3} \rho^{c_3} Q$$

$$\text{For } \pi_1 \Rightarrow [M^0 L^0 T^0] = [T^{-1}]^{a_1} [L]^{b_1} [ML^{-3}]^{c_1} [M^0 L^0 T^0]$$

$$\text{For } M \Rightarrow 0 = c_1 \Rightarrow c_1 = 0$$

$$\text{For } T \Rightarrow 0 = -a_1 \Rightarrow a_1 = 0$$

$$\text{For } L \Rightarrow 0 = b_1 - 3c_1 \Rightarrow c_1 = 0$$

$$\therefore \pi_1 = \omega^0 D^0 \rho^0 \eta \Rightarrow \pi_1 = \eta$$

$$\text{For } \pi_2 \Rightarrow [M^0 L^0 T^0] = [T^{-1}]^{a_2} [L]^{b_2} [ML^{-3}]^{c_2} [ML^{-1}T^{-1}]$$

$$\text{For } M \Rightarrow 0 = c_2 + 1 \Rightarrow c_2 = -1$$

$$\text{For } T \Rightarrow 0 = -a_2 - 1 \Rightarrow a_2 = -1$$

$$\text{For } L \Rightarrow 0 = b_2 - 3c_2 - 1 \Rightarrow b_2 = -2$$

$$\therefore \pi_2 = \omega^{-1} D^{-2} \rho^{-1} \mu \Rightarrow \pi_2 = \frac{\mu}{\omega D^2 \rho}$$

$$\text{For } \pi_3 \Rightarrow [M^0 L^0 T^0] = [T^{-1}]^{a_3} [L]^{b_3} [ML^{-3}]^{c_3} [L^3 T^{-1}]$$

$$\text{For } M \Rightarrow 0 = c_3 \Rightarrow c_3 = 0, \text{ For } T \Rightarrow 0 = a_3 - 1 \Rightarrow a_3 = 1$$

$$\text{For } L \Rightarrow 0 = b_3 - 3c_3 + 3 \Rightarrow b_3 = -3$$

$$\therefore \pi_3 = \omega^1 D^{-3} \rho^0 Q \Rightarrow \pi_3 = \frac{Q}{\omega D^3}$$

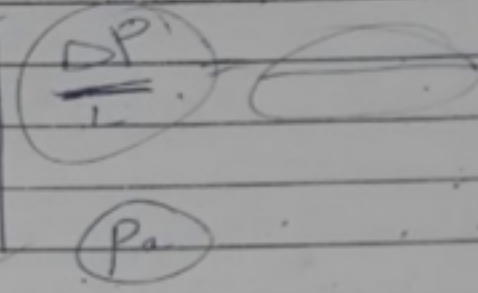
$$f(\pi_1, \pi_2, \pi_3) \Rightarrow f\left(\eta, \frac{\mu}{\omega D^2 \rho}, \frac{Q}{\omega D^3}\right)$$

$$\eta = f\left[\left(\frac{\mu}{\rho \omega D^2}\right), \left(\frac{Q}{\omega D^3}\right)\right]$$

$$\frac{128}{m \cdot s} \quad W = \frac{kg \cdot m}{s^2} \quad P = \frac{M \cdot W}{A \cdot L^2} = \frac{MLT^{-2}}{L^2}$$

P. 2.6. sol 20

- Pressure drop (ΔP) $[ML^{-1}T^{-2}]$
- Velocity (u) $[LT^{-1}]$
- length (L) $[L]$
- Diameter (D) $[L]$
- Viscosity (μ) $[ML^{-1}T^{-1}]$
- roughness (e) $[L]$



$$\Delta P = K(u, L, D, \mu, e)$$

$$f(\Delta P, u, L, D, \mu, e) = 0$$

$$n = 7, m = 3 \rightarrow \pi = n - m = 4$$

no. of repeating vars: $3 = m$

repeating vars: (u, ρ, L)

$$\pi_1 = u^{a_1} \rho^{b_1} L^{c_1} \Delta P$$

$$\pi_2 = u^{a_2} \rho^{b_2} L^{c_2} D$$

$$\pi_3 = u^{a_3} \rho^{b_3} L^{c_3} \mu$$

$$\pi_4 = u^{a_4} \rho^{b_4} L^{c_4} e$$

$$\text{for } \pi_1 \Rightarrow [ML^0T^0] = [LT^{-1}]^{a_1} [ML^{-3}]^{b_1} [L]^{c_1} [ML^{-1}T^{-2}]$$

$$\text{for } M \Rightarrow 0 = b_1 + 1 \Rightarrow b_1 = -1, \text{ for } T \Rightarrow 0 = -a_1 - 2 \Rightarrow a_1 = -2$$

$$\text{for } L \Rightarrow 0 = a_1 - 3b_1 + c_1 - 1 \Rightarrow c_1 = 0$$

$$\therefore \pi_1 = u^{-2} \rho^{-1} L^0 \Delta P \Rightarrow \pi_1 = \frac{\Delta P}{u^2 \rho}$$

$$\text{for } \pi_2 \Rightarrow [M^0T^0] = [LT^{-1}]^{a_2} [ML^{-3}]^{b_2} [L]^{c_2} [L]$$

$$\text{for } M \Rightarrow 0 = b_2, \text{ for } T \Rightarrow 0 = -a_2 \Rightarrow a_2 = 0$$

$$\text{for } L \Rightarrow 0 = a_2 - 3b_2 + c_2 + 1 \Rightarrow c_2 = -1$$

$$\therefore \pi_2 = u^0 \rho^0 L^{-1} D \Rightarrow \pi_2 = \frac{D}{L}$$

$$\text{for } \pi_3 \Rightarrow [M^0T^0] = [LT^{-1}]^{a_3} [ML^{-3}]^{b_3} [L]^{c_3} [ML^{-1}T^{-1}]$$

$$\text{for } M \Rightarrow 0 = b_3 + 1 \Rightarrow b_3 = -1$$

$$\text{for } T \Rightarrow 0 = -a_3 - 1 \Rightarrow a_3 = -1$$

$$\text{for } L \Rightarrow 0 = a_3 - 3b_3 + c_3 - 1 \Rightarrow c_3 = -1$$

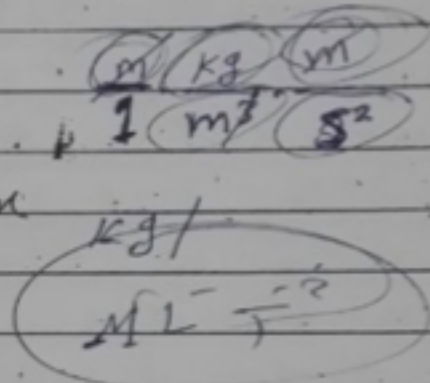
$$\therefore \pi_3 = u^{-1} \rho^{-1} L^{-1} \mu \Rightarrow \pi_3 = \frac{\mu}{u \rho L}$$

$$\text{for } \pi_4 \Rightarrow [M^0T^0] = [LT^{-1}]^{a_4} [ML^{-3}]^{b_4} [L]^{c_4} [L]$$

$$\text{for } M \Rightarrow 0 = b_4, \text{ for } T \Rightarrow 0 = -a_4 \Rightarrow a_4 = 0$$

$$\text{for } L \Rightarrow 0 = a_4 - 3b_4 + c_4 + 1 \Rightarrow c_4 = -1$$

$$\pi_4 = u^0 \rho^0 L^{-1} e \Rightarrow \pi_4 = \frac{e}{L}$$



$$f(\pi_1, \pi_2, \pi_3, \pi_4) = 0$$

$$f\left(\frac{\Delta P}{\rho u^2}, \frac{D}{L}, \frac{\mu}{\rho u L}, \frac{g}{L}\right) = 0$$

$$\Delta P = \rho u^2 f\left[\left(\frac{D}{L}\right), \left(\frac{\mu}{\rho u L}\right), \left(\frac{g}{L}\right)\right]$$

head (hs) [L],anning friction factor (f) [M⁰L⁰T⁰]

Length (L) [L]

Diameter (d) [L]

Velocity (u) [LT⁻¹]

gr. acc. (g) [LT⁻²]

$$f = \frac{L}{d} \frac{u^2}{\rho g}$$

$$h_f = K(f, L, d, u, g)$$

$$f(h_f, f, L, d, u, g) = 0$$

$$n = 6, m = 2, \pi = 6 - 2 = 4$$

no. of repeating vars = 2 = m

Selected repeating vars. (u, L)

$$\pi_1 = u^{a_1} L^{b_1} h_f$$

$$\pi_2 = u^{a_2} L^{b_2} f$$

$$\pi_3 = u^{a_3} L^{b_3} d$$

$$\pi_4 = u^{a_4} L^{b_4} g$$

$$\text{For } \pi_1 \rightarrow [M^0 L^0 T^0] = [LT^{-1}]^{a_1} [L]^{b_1} [L]$$

$$\text{For } T \rightarrow 0 = -a_1 \Rightarrow a_1 = 0, \text{ For } L \rightarrow 0 = a_1 + b_1 + 1 \Rightarrow b_1 = -1$$

$$\therefore \pi_1 = u^0 L^{-1} h_f \Rightarrow \pi_1 = \frac{h_f}{L}$$

$$\text{For } \pi_2 [M^0 L^0 T^0] = [LT^{-1}]^{a_2} [L]^{b_2} [M^0 L^0 T^0]$$

$$\text{For } T \rightarrow 0 = -a_2 \Rightarrow a_2 = 0, \text{ For } L \rightarrow 0 = a_2 + b_2 \Rightarrow b_2 = 0$$

$$\therefore \pi_2 = u^0 L^0 f \Rightarrow \pi_2 = f$$

$$\text{For } \pi_3 \rightarrow [M^0 L^0 T^0] = [LT^{-1}]^{a_3} [L]^{b_3} [L]$$

$$\text{For } T \rightarrow 0 = -a_3 \Rightarrow a_3 = 0, \text{ For } L \rightarrow 0 = a_3 + b_3 + 1 \Rightarrow b_3 = -1$$

$$\therefore \pi_3 = u^0 L^{-1} d \Rightarrow \pi_3 = \frac{d}{L}$$

$$\text{For } \pi_4 \rightarrow [M^0 L^0 T^0] = [LT^{-1}]^{a_4} [L]^{b_4} [LT^{-2}]$$

$$\text{For } T \rightarrow 0 = -a_4 - 2 \Rightarrow a_4 = -2, \text{ For } L \rightarrow 0 = a_4 + b_4 + 1 \Rightarrow b_4 = 1$$

$$\therefore \pi_4 = u^{-2} L^1 g \Rightarrow \pi_4 = \frac{gL}{u^2}$$

$$f(\pi_1, \pi_2, \pi_3, \pi_4) = 0$$

$$f\left(\frac{h_f}{L}, f, \frac{d}{L}, \frac{gL}{u^2}\right) = 0 \Rightarrow h_f \leq 1 f\left(f, \frac{d}{L}, \frac{gL}{u^2}\right)$$

$$f(\pi_1, \pi_2, \pi_3, \pi_4) = 0$$

$$f\left(\frac{\Delta P}{\rho u^2}, \frac{D}{L}, \frac{\mu}{\rho u L}, \frac{g}{L}\right) = 0$$

$$\Delta P = \rho u^2 f\left[\left(\frac{D}{L}\right), \left(\frac{\mu}{\rho u L}\right), \left(\frac{g}{L}\right)\right]$$

Head (h_f) [L], Manning friction factor [1/L]

Length (L) [L]

Diameter (d) [L]

Velocity (u) [LT⁻¹]

gr. acc. (g) [LT⁻²]

$$h_f = K(f, L, d, u, g)$$

$$f(h_f, f, L, d, u, g) = 0$$

$$n = 6, m = 2, \pi = 6 - 2 = 4$$

no. of repeating vars = 2 = m

Selected repeating vars. (u, L)

$$\pi_1 = u^{a_1} L^{b_1} h_f$$

$$\pi_2 = u^{a_2} L^{b_2} f$$

$$\pi_3 = u^{a_3} L^{b_3} d$$

$$\pi_4 = u^{a_4} L^{b_4} g$$

$$\text{For } \pi_1 \Rightarrow [M^0 L^0 T^0] = [L T^{-1}]^{a_1} [L]^{b_1} [L]$$

$$\text{For } T \Rightarrow 0 = -a_1 \Rightarrow a_1 = 0, \text{ for } L \Rightarrow 0 = a_1 + b_1 + 1 \Rightarrow b_1 = -1$$

$$\therefore \pi_1 = u^0 L^{-1} h_f \Rightarrow \pi_1 = \frac{h_f}{L}$$

$$\text{For } \pi_2 [M^0 L^0 T^0] = [L T^{-1}]^{a_2} [L]^{b_2} [M^0 L^0 T^0]$$

$$\text{For } T \Rightarrow 0 = -a_2 \Rightarrow a_2 = 0, \text{ for } L \Rightarrow 0 = a_2 + b_2 \Rightarrow b_2 = 0$$

$$\therefore \pi_2 = u^0 L^0 f \Rightarrow \pi_2 = f$$

$$\text{For } \pi_3 \Rightarrow [M^0 L^0 T^0] = [L T^{-1}]^{a_3} [L]^{b_3} [L]$$

$$\text{For } T \Rightarrow 0 = -a_3 \Rightarrow a_3 = 0, \text{ for } L \Rightarrow 0 = a_3 + b_3 + 1 \Rightarrow b_3 = -1$$

$$\therefore \pi_3 = u^0 L^{-1} d \Rightarrow \pi_3 = \frac{d}{L}$$

$$\text{For } \pi_4 \Rightarrow [M^0 L^0 T^0] = [L T^{-1}]^{a_4} [L]^{b_4} [L T^{-2}]$$

$$\text{For } T \Rightarrow 0 = -a_4 - 2 \Rightarrow a_4 = -2, \text{ for } L \Rightarrow 0 = a_4 + b_4 + 1 \Rightarrow b_4 = 1$$

$$\therefore \pi_4 = u^{-2} L^1 g \Rightarrow \pi_4 = \frac{g L}{u^2}$$

$$f(\pi_1, \pi_2, \pi_3, \pi_4) = 0$$

$$f\left(\frac{h_f}{L}, f, \frac{d}{L}, \frac{g L}{u^2}\right) = 0 \Rightarrow h_f = L f\left(f, \frac{d}{L}, \frac{g L}{u^2}\right)$$

P. 2.7. Solⁿ

$$\text{Power } (P) [ML^2T^{-3}]$$

$$\text{Diameter } (D) [L]$$

$$\text{Velocity } (w) [LT^{-1}]$$

$$\text{Discharge } (Q) [L^3T^{-1}]$$

$$\text{Density } (\rho) [ML^{-3}]$$

$$P = k(D, w, Q, \rho)$$

$$f(P, D, w, Q, \rho)$$

$$n = 5, m = 3, \pi = n - m = 2$$

no. of repeating vars. = 3 = m

Selected repeating vars. = (D, w, ρ)

$$\pi_1 = D^{a_1} w^{b_1} \rho^{c_1} P$$

$$\pi_2 = D^{a_2} w^{b_2} \rho^{c_2} Q$$

$$\text{For } \pi_1 \Rightarrow [ML^0T^0] = [L]^{a_1} [T^{-1}]^{b_1} [ML^{-3}]^{c_1} [ML^2T^{-3}]$$

$$\text{For } M \Rightarrow 0 = c_1 + 1 \Rightarrow c_1 = -1$$

$$\text{For } T \Rightarrow 0 = -b_1 - 3 \Rightarrow b_1 = -3$$

$$\text{For } L \Rightarrow 0 = a_1 - 3c_1 + 2 \Rightarrow a_1 = -5$$

$$\therefore \pi_1 = D^{-5} w^{-3} \rho^{-1} P \Rightarrow \pi_1 = \frac{P}{w^3 \rho D^5}$$

$$\text{For } \pi_2 \Rightarrow [ML^0T^0] = [L]^{a_2} [T^{-1}]^{b_2} [ML^{-3}]^{c_2} [L^3T^{-1}]$$

$$\text{For } M \Rightarrow 0 = c_2 \Rightarrow \text{For } T \Rightarrow 0 = -b_2 - 1 \Rightarrow b_2 = -1$$

$$\text{For } L \Rightarrow 0 = a_2 - 3c_2 + 3 \Rightarrow a_2 = -3$$

$$\therefore \pi_2 = D^{-3} w^{-1} \rho^0 Q \Rightarrow \pi_2 = \frac{Q}{w D^3}$$

$$f(\pi_1, \pi_2) = 0$$

$$f\left(\frac{P}{w^3 \rho D^5}, \frac{Q}{w D^3}\right) = 0$$

$$P = (w^3 \rho D^5) f\left(\frac{Q}{w D^3}\right)$$

تكرار المتغيرات

قالب المتغيرات

تكرار المتغيرات

$$(D, w, \rho)$$

تكرار المتغيرات

قالب المتغيرات

تكرار المتغيرات

$$(D, w, \rho)$$