



Al-Mustaqbal University

**College of Engineering and
Technology**

**Department of Biomedical
Engineering**

Stage: three

Signal Processing

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**Lecture (5): Discrete convolution/
Tabular method.**

Tabular Method

this is a very simple method used for FIR systems with finite number of samples $x(n)$. A rectangular table with N_1 rows (number of elements in $h(n)$) and N_2 columns (number elements of $x(n)$), or visa versa, is arranged. Then the cross multiplications are carried out. The sum of the multiplications diagonally will give the value of $y(n)$.

Example/ Use Tabular method to find the convolution between

$$x(n) = \{1, 2, 3, 4, 5\}$$

$$h(n) = \{1, 2, 3, 3, 2, 1\}$$

Solve/ $y(n)=x(n)*h(n)$

	$x(n) \rightarrow$	$y(0)=1$ 1	$y(1)=4$ 2	$y(2)=10$ 3	$y(3)=19$ 4	$y(4)=30$ 5	
1	1×1	1×2	1×3	1×4	1×5		$y(5)=36$
2	2×1	2×2	2×3	2×4	2×5		$y(6)=35$
3	3×1	3×2	3×3	3×4	3×5		$y(7)=26$
3	3×1	3×2	3×3	3×4	3×5		$y(8)=14$
2	2×1	2×2	2×3	2×4	2×5		$y(9)=5$
1	1×1	1×2	1×3	1×4	1×5		

$h(n) \downarrow$

$$y(0)=1 \times 1=1$$

$$y(1)=1 \times 2 + 2 \times 1=4$$

$$y(2)=1 \times 3 + 2 \times 2 + 3 \times 1=10$$

$$y(3)=1 \times 4 + 2 \times 3 + 3 \times 2 + 3 \times 1=19$$

$$y(4)=1 \times 5 + 2 \times 4 + 3 \times 3 + 3 \times 2 + 2 \times 1=30$$

$$y(5)=2 \times 5 + 3 \times 4 + 3 \times 3 + 2 \times 2 + 1 \times 1=36$$

$$y(6) = 3 \times 5 + 3 \times 4 + 2 \times 3 + 1 \times 2 = 35$$

$$y(7) = 3 \times 5 + 2 \times 4 + 1 \times 3 = 26$$

$$y(8) = 2 \times 5 + 1 \times 4 = 14$$

$$y(9) = 1 \times 5 = 5$$

$$y(n) = [1, 4, 10, 19, 30, 36, 35, 26, 14, 5]$$

↑

Example/ if we have $h(n) = [1, -1, 2]$ and $x(n) = [2, 1, -1, 3]$

↑
↑

The convolution between $h(n)$ and $x(n)$ can be computed as shown below:

		2	1	-1	3
1		2	1	-1	3
-1		-2	-1	1	-3
2		4	2	-1	6

↑

$$y(n) = [2, -1, 2, 6, -4, 6]$$

↑

Example: $x(n) = [4, 2, 1, 3]$ and $h(n) = [1, 2, 2, 1]$ the convolution will be

↑

		4	2	1	3
1		4	2	1	3
2		8	4	2	6
2		8	4	2	6
1		4	2	1	3

↑

$$y(n) = [4, 10, 13, 13, 10, 7, 3]$$

↑