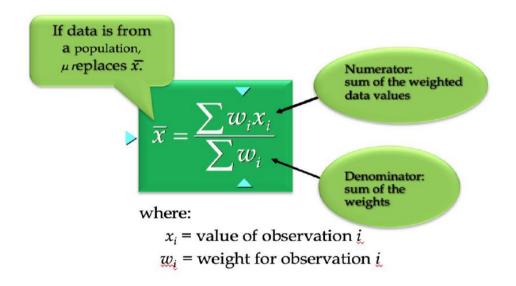
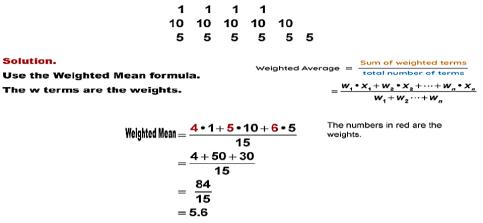
3.1 Weighted Mean

The weighted mean is a type of mean that is calculated by multiplying the weight (or probability) associated with a particular event or outcome with its associated quantitative outcome and then summing all the products together. It is very useful when calculating a theoretically expected outcome where each outcome has a different probability of occurring, which is the key feature that distinguishes the weighted mean from the arithmetic mean.



Example

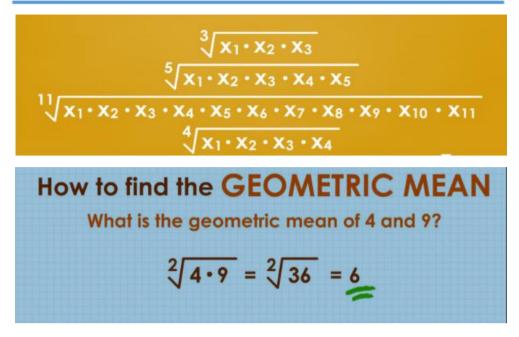
Find the mean of the following data set.



Geometric mean

In mathematics, the geometric mean is a mean or average, which indicates the central tendency or typical value of a set of numbers by using the product of their values (as opposed to the arithmetic mean which uses their sum). The geometric mean is defined as the nth root of the product of n numbers, i.e., for a set of numbers x1,x2,...,xn, the geometric mean is defined as:

Geometric mean = $\sqrt[n]{x_1 \cdot x_2 \cdot \ldots \cdot x_n}$



Harmonic mean

The harmonic mean can be expressed as the reciprocal of the arithmetic mean of the reciprocals of the given set of observations.

$$Harmonic\ mean = \frac{n}{\sum \frac{1}{x_i}}$$

Where:

n: the number of the values in a dataset

xi: the point in a dataset

Example/ consider 2, 3, 5, 7, and 60 with a number of observations as 5 find Harmonic mean?

Harmonic Mean =
$$\frac{n}{\left(\frac{1}{x_1} + \frac{1}{x_2} + \dots + \frac{1}{x_n}\right)}$$

= $\frac{5}{\left(\frac{1}{2} + \frac{1}{3} + \frac{1}{5} + \frac{1}{7} + \frac{1}{60}\right)}$
= $\frac{5}{(0.5 + 0.33 + 0.2 + 0.14 + 0.017)}$
= $\frac{5}{1.187}$
= 4.21