



الدوال المستمرة (Continuous Functions) :

The Continuity Test:

The function $y = f(x)$ is continuous at $x=c$ if and only if the following statements are true:

- 1- $f(c)$ exists
- 2- $\lim_{x \rightarrow c} f(x)$ exists
- 3- $f(c) = \lim_{x \rightarrow c} f(x)$

Example: did the function $f(x) = 8 - x^3 - 2x^2$ is continuous at the $x=2$?

Sol:

$$f(2) = 8 - 2^3 - 2 * (2)^2 = 8$$

$$\lim_{x \rightarrow 2} [8 - x^3 - 2x^2] = 8 - 2^3 - 2 * (2)^2 = 8$$

$$f(2) = \lim_{x \rightarrow 2} f(x).$$

So the function is continuous at $x=2$.

Example: did the function $f(x) = \frac{(x^2-4)}{x-2}$ is continuous at the $x=2$?

Sol:

$$f(2) = \frac{(2^2-4)}{2-2} = \frac{0}{0} \text{ not exists}$$

So the function is not continuous at $x=2$.

Lecture (6)



H.W:

1- did the function $f(x) = \frac{(x^2-9)}{x-3}$ is continuous at the $x=3$?

2- Find the limit of the function $f(x) = \frac{(x^2-1)}{x-\sqrt{1}}$ is continuous at the $x=\sqrt{1}$?