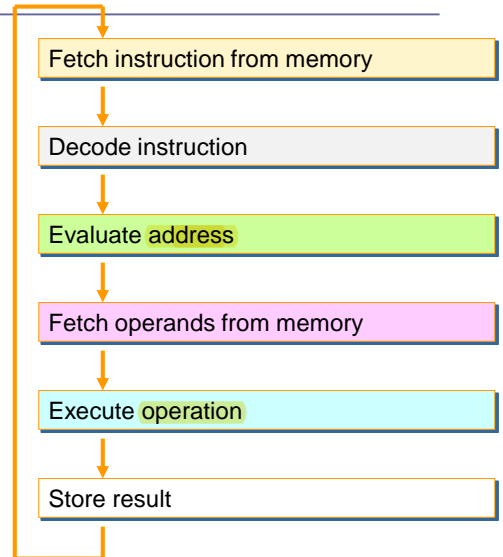


Instruction Processing

- The instruction is the fundamental unit of work.
- Specifies two things:
 - **Opcode:** operation to be performed
 - **Operands:** data/locations to be used for operation



Introduction to Main Digital Component

Introduction to Digital Logic Basics

- Hardware consists of a few simple building blocks
 - These are called *logic gates*
 - AND, OR, NOT, ...
 - NAND, NOR, XOR, ...
- Logic gates are built using transistors
- Transistors are the fundamental devices
 - Pentium consists of 3 million transistors
 - Compaq Alpha consists of 9 million transistors
 - Now chips can be built with more than 100 million transistors

Data Representation/Binary numbers

- Almost all modern computers are *digital computers*, which means that they can recognize only two distinct electronic states of electrical charge. For simplicity, these states are identified as **0** and **1**, or equivalently, **false** and **true**, or **off** and **on**. Since **0** and **1** are the most compact means of representing two states, data is represented as sequences of 0's and 1's. Sequences of 0's and 1's are binary numbers.

Integer Number

- The number system that we are used to is a **decimal number** system because it is **base 10**. For example:
 - $54318 = 5 \times 10^4 + 4 \times 10^3 + 3 \times 10^2 + 1 \times 10^1 + 8 \times 10^0$
 - $= 5 \times 10000 + 4 \times 1000 + 3 \times 100 + 1 \times 10 + 8 \times 1$
 - $= 50000 + 4000 + 300 + 10 + 8$
 - $= 54318$

Binary Number

- To convert from decimal to binary, start with the binary number and keep dividing by 2, writing the remainder (of any) after each division. Keep doing this until reach one. The result, then, is the remainders, starting from the bottom. Here's an example:
 - $132 \text{-----} 0$
 - $66 \text{-----} 0$
 - $33 \text{-----} 1$
 - $16 \text{-----} 0$
 - $8 \text{-----} 0$
 - $4 \text{-----} 0$
 - $2 \text{-----} 0$
 - 1
- Starting from the 1 at the bottom, the binary equivalent of 132 is **10000100**.

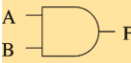
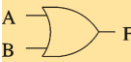
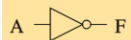
Binary Number

- The binary number system works like the decimal number system, but it is a base 2 system. To convert binary to decimal, use the same method used above but use **base 2**.

$$\begin{aligned}
 \square \text{ 11010101} &= 1 \times 2^7 + 1 \times 2^6 + 0 \times 2^5 + 1 \times 2^4 + 0 \times 2^3 + 1 \times 2^2 + 0 \times 2^1 + 1 \times 2^0 \\
 &= 1 \times 128 + 1 \times 64 + 0 \times 32 + 1 \times 16 + 0 \times 8 + 1 \times 4 + 0 \times 2 + 1 \times 1 \\
 &= 128 + 64 + 0 + 16 + 0 + 4 + 0 + 1 \\
 &= \mathbf{213}
 \end{aligned}$$

Basic Concepts

- **Logical operations (Logic Gates)**
- Simple gates
 - AND
 - OR
 - NOT
- Functionality can be expressed by a truth table
 - A truth table lists output for each possible input combination

 <p>AND gate</p>	A	B	F
	0	0	0
	0	1	0
	1	0	0
	1	1	1
 <p>OR gate</p>	A	B	F
	0	0	0
	0	1	1
	1	0	1
	1	1	1
 <p>NOT gate</p>	A	F	
	0	1	
	1	0	
Logic symbol			Truth table

Basic Concepts

- Additional useful gates
 - NAND
 - NOR
 - XOR
- **NAND = AND + NOT**
- **NOR = OR + NOT**

The image shows logic symbols and truth tables for three gates: NAND, NOR, and XOR.

NAND gate: The logic symbol shows two inputs, A and B, entering a D-shaped gate with a small circle at the output. The output is labeled F. The truth table is:

A	B	F
0	0	1
0	1	1
1	0	1
1	1	0

NOR gate: The logic symbol shows two inputs, A and B, entering a D-shaped gate with a small circle at the output. The output is labeled F. The truth table is:

A	B	F
0	0	1
0	1	0
1	0	0
1	1	0

XOR gate: The logic symbol shows two inputs, A and B, entering a gate with a curved front and a pointed back. The output is labeled F. The truth table is:

A	B	F
0	0	0
0	1	1
1	0	1
1	1	0

Labels: Logic symbol, Truth table

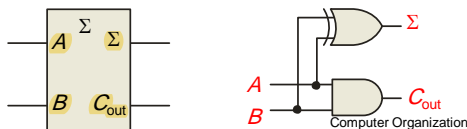
19

Half Adder

- **Arithmetic Operations: Binary Addition**
- Basic rules of binary addition are performed by a **half adder**, which has two binary inputs (*A* and *B*) and two binary outputs (Carry out and Sum).
- The inputs and outputs can be summarized on a truth table.

Inputs		Outputs	
A	B	C _{out}	Σ
0	0	0	0
0	1	0	1
1	0	0	1
1	1	1	0

- The logic symbol and equivalent circuit are:



Full-Adder

- By contrast, a **full adder** has three binary inputs (A , B , and Carry in) and two binary outputs (Carry out and Sum).
- The truth table summarizes the operation.
- A full-adder can be constructed from two half adders as shown:

Inputs			Outputs	
A	B	C_{in}	C_{out}	Σ
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1

