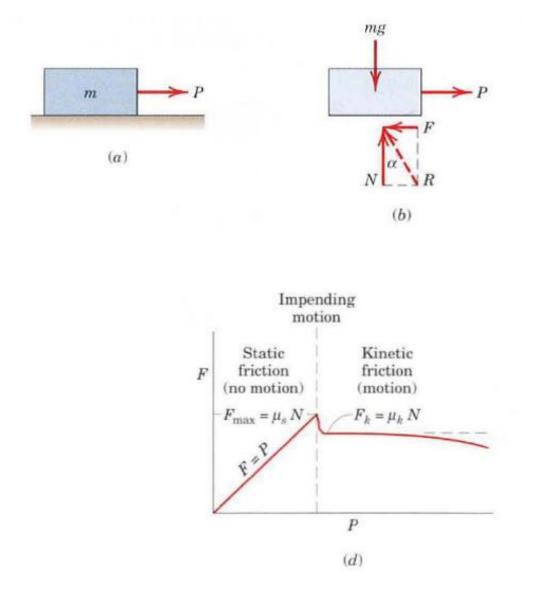




# FRICTION

Consider a solid block of mass m resting on a horizontal surface, as shown in Figures we assume that the contacting surfaces have some roughness.

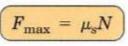






### **Static Friction**

The region in Figure d up to the point of slippage or impending motion is called the range of static friction, and in this range the value of the friction force is determined by the equations of equilibrium.



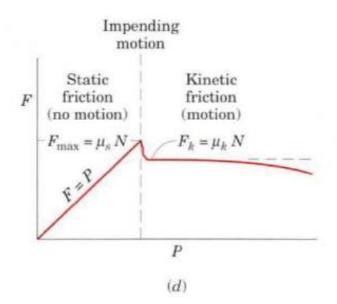
Where  $\mu_s$ , is the proportionality constant, called the coefficient of static friction.

 $F < \mu_s N$ 

#### **Kinetic Friction**

After slippage occurs, a condition of kinetic friction accompanies the ensuing motion. Kinetic friction force is usually somewhat less than the maximum static friction force. The kinetic friction force  $F_k$  is also proportional to the normal force. Thus,

$$F_k = \mu_k N$$

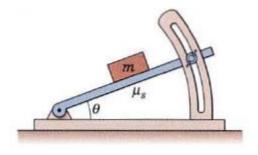




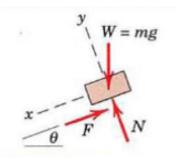


# Problem 1

Determine the maximum angle  $\theta$  which the adjustable incline may have with the horizontal before the block of mass m begins to slip. The coefficient of static friction between the block and the inclined surface is  $\mu_s$ .



Solution



Equilibrium in the x- and y-directions requires

- $\Sigma F_x=0$  mg sin $\theta$  F =0 F =mg sin  $\theta$
- $\Sigma F_y\!\!=\!\!0 \qquad \text{-} mg\,\cos\theta + N \!=\! 0 \qquad N \!=\!\! mg\,\cos\theta$

 $F/N = tan \theta$ 

 $F = F_{max} = \mu_s N$ 

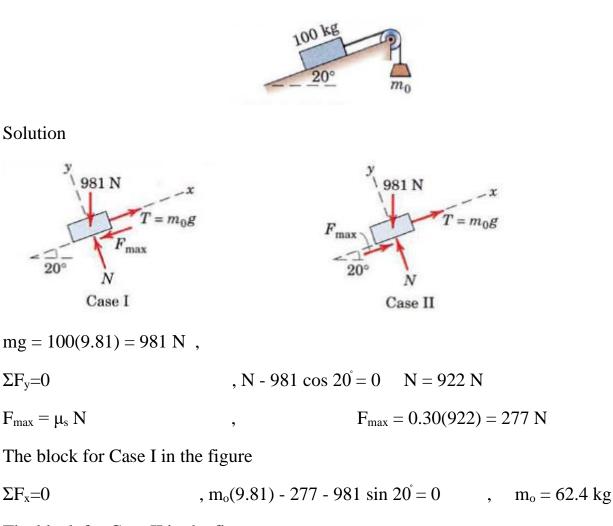
 $\mu_s = \tan \theta_{max}$  or  $\theta_{max} = \tan^{-1}\mu_s$ ,





# Problem 2

Determine the range of values which the mass  $m_o$  may have so that the 100-kg block shown in the figure will neither start moving up the plane nor slip down the plane. The coefficient of static friction for the contact surfaces is 0.30



The block for Case II in the figure

$$\Sigma F_x=0$$
  $m_o(9.81) + 277 - 981 \sin 20^\circ = 0$   $m_o = 6.01 \text{ kg}$ 

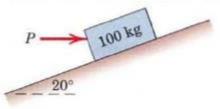
Thus,  $m_o$  may have any value from 6.01 to 62.4 kg, and the block will remain at rest.



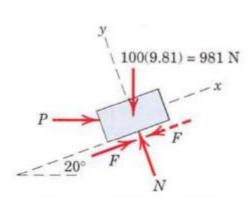


#### Problem 3

Determine the magnitude and direction of the friction force acting on the 100-kg block shown if, first, P = 500 N and, second, P = 100 N. The coefficient of static friction is 0.20, and the coefficient of kinetic friction is 0.17. The forces are applied with the block initially at rest.



Solution



$\Sigma F_x=0$	$P \cos 20^\circ + F - 981 \sin 20^\circ = 0$
$\Sigma F_y=0$	N - P sin 20° - 981 cos 20° = 0
<u>Case I</u> . $P = 500 \text{ N}$	
F = - 134.3 N	, N = 1093N
$F_{max} = \mu_s N$	$F_{max} = 0.20(1093) = 219 \text{ N}$
<u>Case II</u> . $P = 10$	00 N
F = 242 N ,	N = 956 N

 $F_{max} = \mu_s N \qquad \qquad F_{max} = 0.20(956) = 191.2 N$ 

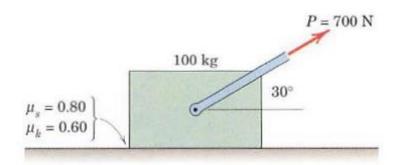
It follows that 242 N of friction cannot be supported. Therefore, equilibrium cannot exist, and we obtain the correct value of the friction force by using the kinetic coefficient of friction accompanying the motion down the plane.  $F_k = \mu_k N$   $F_k = 0.17(956) = 162.5 N$ 



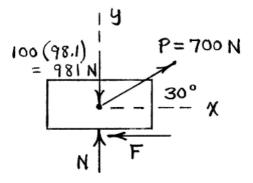


#### Problem 4

The 700-N force is applied to the 100-kg block, which is stationary before the force is applied. Determine the magnitude and direction of the friction force F exerted by the horizontal surface on the block.



Solution



$$\Sigma F_X = 0$$
: 700 cos 30° - F = 0, F = 606 N  
 $\Sigma F_Y = 0$ : N-981 + 700 sin 30° = 0, N = 631 N  
 $F_{max} = \mu_s N = 0.8 (631) = 505 N < F = 606 N$   
Assumption invalid, motion occurs.  
 $F = \mu_k N = 0.6 (631) = 379 N$