Sample problem: a force at an angle.
Example: what is the magnitude of net force on the ball along each axis, and what is the ball's acceleration along each axis? Consider the below figure.

Sol.
$\mathrm{F}_{\mathrm{x}}=\mathrm{F} \cos \theta=262 \cos 60=131 \mathrm{~N}$
$\mathrm{F}_{\mathrm{y}}=\mathrm{F} \sin \theta=262 \sin 60=227 \mathrm{~N}$
Now, we need to calculate net force along X -axis
$\Sigma \mathrm{F}_{\mathrm{X}}=131 \mathrm{~N}$
Also, we need to calculate net force along Y-axis

$$
\begin{aligned}
\Sigma \mathrm{F}_{\mathrm{y}} & =\mathrm{F} \sin \theta+(-\mathrm{mg}) \\
& =227-1.4=225.6 \mathrm{~N}
\end{aligned}
$$

Now, calculating the acceleration along the X -axis using newton's $2^{\text {nd }}$ law
$\Sigma \mathrm{F}_{\mathrm{x}}=\mathrm{ma}_{\mathrm{x}}$
$\mathrm{a}_{\mathrm{x}}=\frac{\Sigma \mathrm{Fx}}{\mathrm{m}}$



Since $\mathrm{mg}=1.4 \mathrm{~N}, \mathrm{~m} * 9.8=1.4$

$$
\begin{aligned}
\mathrm{m} & =\frac{1.4}{9.8}=0.143 \mathrm{Kg} \\
\mathrm{a}_{\mathrm{x}}=\frac{131}{0.143} & =916 \mathrm{~m} / \mathrm{s}^{2}
\end{aligned}
$$

Now, calculating $\Sigma \mathrm{F}_{\mathrm{y}}=$ ma $_{\mathrm{y}}$

$$
\mathrm{a}_{\mathrm{y}}=\frac{\Sigma \mathrm{Fy}}{\mathrm{~m}}=\frac{225.6}{0.143}=1577.6 \mathrm{~m} / \mathrm{s}^{2}
$$

Sample problem: moving down a frictionless plane.
Example: what is the toy car's acceleration for the below figure?
Assumption: In this problem, ignore any friction or air resistance.


Sol.:
Components of weight $\mathrm{w}_{\mathrm{x}} \& \mathrm{w}_{\mathrm{y}}$ equals:

$$
\begin{aligned}
& \mathrm{w}_{\mathrm{x}}=\mathrm{mg} \sin \theta=(0.1)(9.81) \sin 30=0.49 \mathrm{~N} \\
& \mathrm{w}_{\mathrm{y}}=\mathrm{mg} \cos \theta=(0.1)(9.81) \cos 30=0.85 \mathrm{~N}
\end{aligned}
$$

$$
\Sigma \mathrm{F}_{\mathrm{x}}=\text { max }_{\mathrm{x}} \text { newton's } 2^{\text {nd }} \text { law }
$$

Since

$$
\Sigma \mathrm{F}_{\mathrm{x}}=\mathrm{mg} \sin \theta=0.49 \mathrm{~N}
$$

Hence

$$
\begin{aligned}
& 0.49=\mathrm{ma} \\
& 0.49=(0.1) * \mathrm{a} \\
& \mathrm{a}=4.9 \mathrm{~m} / \mathrm{s}^{2} \text { (down the plane) }
\end{aligned}
$$

## Hooke's law and spring force:

It is law of physics that states that the force (Fs) needed to extend or compress a spring by some distance $(\mathrm{X})$ scales linearly with respect to that distance.

## Spring force:

Force exerted by spring depends on:

- How much it is stretched or compressed.
- Spring constant.

Fs = - KX Hooke's
Where
Fs: spring force. (N)


K : spring constant.
X : displacement of end from rest point. (m)
Example: what is the force exerted by the spring for the below figure?
Sol.:

Fs $=-K X$
Fs $=-(4.2)(0.36)$
$\mathrm{Fs}=-1.5 \mathrm{~N}$ (to the left)


Sample problem: spring force and tension.
Example: what is the amount of tension in rope for the below figure? What is the position of the end of the spring away from its rest position?


Sol.:

Notes:

- The forces sum to zero for each object (i.e spring or block) because there is no acceleration.
- The tension forces are equal in magnitude, so we use the same variable T for each of them.


## Since

$\Sigma \mathrm{F}=\mathrm{ma}, \quad$ apply $2^{\text {nd }}$ law on the block
$\Sigma \mathrm{F}_{\mathrm{y}}=\mathrm{ma}_{\mathrm{y}}$
$\mathrm{T}-\mathrm{w}=\mathrm{m}(0)$
$\mathrm{T}=\mathrm{w}=\mathrm{mg}=98 \mathrm{~N}$.
Fs = - KY
by apply $2^{\text {nd }}$ law on the spring


$\Sigma \mathrm{F}_{\mathrm{y}}=\mathrm{ma}_{\mathrm{y}}$
Fs $-\mathrm{T}=\mathrm{m}(0), \mathrm{Fs}=\mathrm{T}=98 \mathrm{~N}$.
$\mathrm{Fs}=-\mathrm{KY}$
$98=-535 * \mathrm{Y}, \mathrm{Y}=\frac{-98}{535}=-0.183 \mathrm{~m}$.

Air resistance: a force that opposes motion in air

- Drag force opposes motion in air.
- Drag force increases as speed increase.

The force created by air resistance is called drag force.
$\mathrm{F}_{\mathrm{D}}=\frac{1}{2} \mathrm{C} \rho \mathrm{AV}^{2}$
Where:
$F_{D}$ : drag force
C: drag coefficient for object (based on approximation of shape) $\rho:$ air density

A: cross-sectional area
V: velocity

Terminal velocity: is the maximum velocity attainable by an object as it falls through a fluid, (air is the most common
 example)

Drag force equals weight.
$V_{T}=\sqrt{\frac{2 m g}{c \rho A}}$
$\mathrm{V}_{\mathrm{T}}$ : terminal velocity
mg: weight
Example: the drag coefficient $(\mathrm{C})$ is 0.49 and the air density $(\rho)$ is $1.1 \mathrm{Kg} / \mathrm{m}^{3}$. What is the skydiver's terminal velocity as shown in figure?

Sol.:
$V_{T}=\sqrt{\frac{2 m g}{c \rho A}}$
$V_{T}=\sqrt{\frac{2(650)}{(0.49)(1.1)(0.9)}}$

$V_{T}=52 \mathrm{~m} / \mathrm{s}$

Sample problem: blocks and a pulley system.
Example: what is the acceleration of the block on the frictionless table?
Sol.:
According to the free body diagram, we noticed that the magnitudes of the tension forces exerted on each block by the rope are the same; the amount of tension does not vary within a rope. Because the rope connects the blocks, they accelerate at the same rate (but in different direction).


Block A on table

$$
\text { X-Component } \quad \text { Y- component }
$$

Tension
T
Weight
0N
-mg
Normal force
0N
FN
Acceleration
a
$0 \mathrm{~m} / \mathrm{s}^{2}$

## Falling block B

> X- Component Y-component

Tension 0N
Weight
Acceleration
$0 \mathrm{~m} / \mathrm{s}^{2}$

T
-mg
-a

Apply $2^{\text {nd }}$ law of newton on block A
$\Sigma \mathrm{F}_{\mathrm{x}}=\mathrm{m}_{\mathrm{A}} \mathrm{a}_{\mathrm{x}}$
$\mathrm{T}=\mathrm{m}_{\mathrm{A}} \mathrm{a}_{\mathrm{x}}$
$\mathrm{a}_{\mathrm{x}}=\frac{\mathrm{T}}{\mathrm{mA}} \ldots$ (1)
Apply $2^{\text {nd }}$ law of newton on block B
$\Sigma \mathrm{F}_{\mathrm{y}}=\mathrm{m}_{\mathrm{B}} \mathrm{a}_{\mathrm{y}}$
$\mathrm{T}-\mathrm{w}_{\mathrm{B}}=\mathrm{m}_{\mathrm{B}} \mathrm{a}_{\mathrm{y}}$
$T=w_{B}+m_{B} a_{Y}$
Since $a_{y}=-a_{x}$
$T=m_{B} g+m_{B}\left(-a_{x}\right)$
$T=m_{B} g-m_{B} a_{x} \quad$ sub. Into equ. 1
$\mathrm{a}_{\mathrm{x}}=\frac{\mathrm{mBg}-\mathrm{mB} \mathrm{ax}}{\mathrm{mA}}$
$\mathrm{m}_{\mathrm{A}} * \mathrm{a}_{\mathrm{x}}=\mathrm{m}_{\mathrm{B}} \mathrm{g}-\mathrm{m}_{\mathrm{B}} \mathrm{a}_{\mathrm{x}}$
$\mathrm{a}_{\mathrm{x}}\left(\mathrm{m}_{\mathrm{A}}+\mathrm{m}_{\mathrm{B}}\right)=\mathrm{m}_{\mathrm{B}} \mathrm{g} \quad \mathrm{a}_{\mathrm{x}}=\mathrm{m}_{\mathrm{B}} \mathrm{g} /\left(\mathrm{m}_{\mathrm{A}}+\mathrm{m}_{\mathrm{B}}\right)=\frac{5.7 * 9.8}{(4.2+5.7)}=5.64 \mathrm{~m} / \mathrm{s}^{2}$

Sample problem: airplane at constant velocity.
Example: The plane flies at an angle of $60^{\circ}$ and it does not accelerating. Its weight is $2.6 * 10^{5} \mathrm{~N}$ and its engine thrust is $3 * 10^{5} \mathrm{~N}$. What is the amount of lift force on its wings?


Sol.:
According to the figure on right side, one can see that the jet airplane flying through the air at an angle. It travels at a constant velocity; this means that it does not accelerating and no net force is acting on the plane along any dimension.

The forces acting on the plane are its weight, the force provided by its engine, called thrust, the drag force from air resistance, and the lift force from the wings.

The lift force acts perpendicular to the surface of wings.

Weight

$$
\begin{array}{cc}
\text { X- Component } & \text { Y- component } \\
-m g \sin \theta & -m g \cos \theta
\end{array}
$$

Thrust
$\mathrm{F}_{\mathrm{T}}$
0N
Lift
0
$\mathrm{F}_{\mathrm{L}}$
Drag Force
$\mathrm{F}_{\mathrm{R}}$
0
$\Sigma F=$ ma $\quad$ 2nd law of newton
$\Sigma \mathrm{F}_{\mathrm{y}}=0$
$\mathrm{F}_{\mathrm{L}}-\mathrm{mg} \cos \theta=0$
$\mathrm{F}_{\mathrm{L}}-2.6^{*} 10^{5} \cos 60=0$
$\mathrm{F}_{\mathrm{L}}=1.3 * 10^{5} \mathrm{~N}$

