



MATLAB

Stage2

Lec5

MATRIX

MS.c Ola Ali

MS.c Haneen Alharir

Introduction :

Matrices are the basic elements of the MATLAB environment. A matrix is a two-dimensional array consisting of m rows and n columns.

Special cases are column vectors ($n = 1$) and row vectors ($m = 1$). In this section we will illustrate how to apply different operations on matrices. The following topics are discussed: vectors and matrices in MATLAB, the inverse of a matrix, determinants, and matrix manipulation.

MATLAB supports two types of operations, known as matrix operations and array operations. Matrix operations will be discussed.

Matrix generation:

Matrices are fundamental to MATLAB. Therefore, we need to become familiar with matrix generation and manipulation. Matrices can be generated in several ways.

Entering a vector:

A vector is a special case of a matrix. The purpose of this section is to show how to create vectors and matrices in MATLAB. As discussed earlier, an array of dimension $1 \times n$ is called a row vector, whereas an array of dimension $m \times 1$ is called a column vector. The elements of vectors in MATLAB are enclosed by square brackets and are separated by spaces or by commas. For example, to enter a row vector, v , type.

```
>> v = [1 4 7 10 13]
v =
     1     4     7    10    13
```

Column vectors are created in a similar way, however, semicolon (;) must separate the components of a column vector,

```
>> w = [1;4;7;10;13]
w =
     1
     4
     7
    10
    13
```

On the other hand, a *row* vector is converted to a *column* vector using the *transpose* operator. The *transpose* operation is denoted by an apostrophe or a single quote (').

```
>> w = v'
w =
     1
     4
     7
    10
    13
```

Thus, $v(1)$ is the first element of vector v , $v(2)$ its second element, and so forth.

Furthermore, to access *blocks* of elements, we use MATLAB's colon notation (:). For example, to access the first three elements of v , we write,

```
>> v(1:3)
ans =
     1     4     7
```

Or, all elements from the third through the last elements,

```
>> v(3:end)
ans =
     7    10    13
```

where *end* signifies the *last* element in the vector. If v is a vector, writing

```
>> v(:)
```

produces a column vector, whereas writing

```
>> v(1:end)
```

produces a row vector.

Entering a matrix:

A matrix is an array of numbers. To type a matrix into MATLAB you must

- begin with a square bracket,
- separate elements in a row with spaces or commas (,)
- use a semicolon (;) to separate rows
- end the matrix with another square bracket,

Here is a typical example. To enter a matrix A , such as,

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix} \quad (2.1)$$

type,

```
>> A = [1 2 3; 4 5 6; 7 8 9]
```

MATLAB then displays the 3×3 matrix as follows,

```
A =  
 1  2  3  
 4  5  6  
 7  8  9
```

Note that the use of semicolons (;) here is different from their use mentioned earlier to suppress output or to write multiple commands in a single line.

Once we have entered the matrix, it is automatically stored and remembered in the *Workspace*. We can refer to it simply as matrix A . We can then view a particular element in a matrix by specifying its location. We write,

```
>> A(2,1)  
ans =  
 4
```

$A(2,1)$ is an element located in the second row and first column. Its value is 4.

Matrix index:

We select elements in a matrix just as we did for vectors, but now we need two indices. The element of row i and column j of the matrix A is denoted by $A(i,j)$. Thus, $A(i,j)$ in MATLAB refers to the element A_{ij} of matrix A . The *first* index is the *row* number and the *second* index is the *column* number. For example, $A(1,3)$ is an element of *first* row and *third* column. Here, $A(1,3)=3$.

Correcting any entry is easy through indexing. Here we substitute $A(3,3)=9$ by $A(3,3)=0$. The result is

```
>> A(3,3) = 0
A =
    1    2    3
    4    5    6
    7    8    0
```

Colon operator in a matrix :

The colon operator can also be used to pick out a certain row or column. For example, the statement $A(m:n,k:l)$ specifies rows m to n and column k to l . Subscript expressions refer to portions of a matrix.

For example,

```
>> A(2,:)
ans =
    4    5    6
```

is the second row elements of A .

The colon operator can also be used to extract a sub-matrix from a matrix A .

```
>> A(:,2:3)
ans =
    2    3
    5    6
    8    0
```

$A(:,2:3)$ is a sub-matrix with the last two columns of A .

A row or a column of a matrix can be deleted by setting it to a *null* vector, $[]$.

```
>> A(:,2)=[]
ans =
    1    3
    4    6
    7    0
```

To extract a *submatrix* B consisting of rows 2 and 3 and columns 1 and 2 of the matrix A, do the following

```
>> B = A([2 3],[1 2])
B =
    4    5
    7    8
```

To interchange rows 1 and 2 of A, use the vector of row indices together with the colon operator.

```
>> C = A([2 1 3], :)
C =
    4    5    6
    1    2    3
    7    8    0
```

It is important to note that the *colon operator* (:) stands for *all columns* or *all rows*. To create a vector version of matrix A, do the following