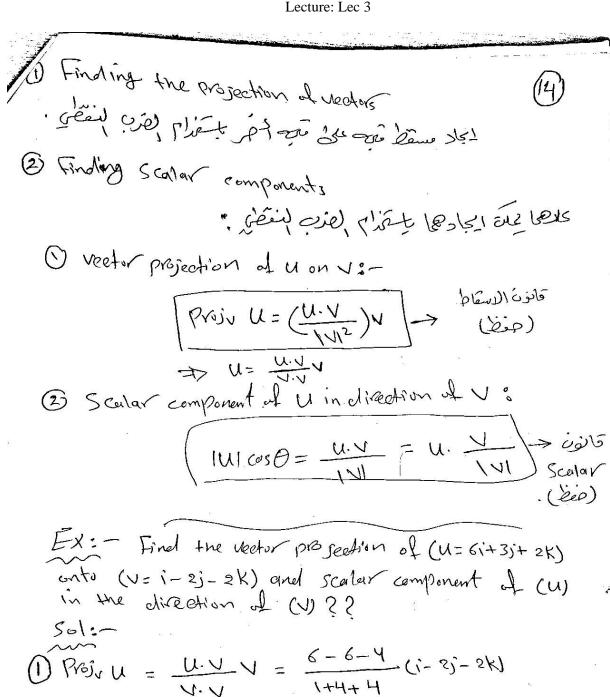


## Department of Medical Instrumentation Techniques Engineering

Class: second stage Subject: Mathematics II

Lecturer: Dr. Diyar Hussain Habbeb



 $= -\frac{4}{9} (i-2j-2k)$ 

 $= -\frac{4}{9}i + \frac{8}{9}j + \frac{8}{9}k$ 



#### Department of Medical Instrumentation Techniques Engineering

Class: second stage Subject: Mathematics II

Lecturer: Dr. Diyar Hussain Habbeb

Lecture: Lec 3



Scalar component of (U) in direction of (V):

(15)

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2} + (-2)^{2}} = 3$$

$$|V| = \sqrt{1^{2} + (-2)^{2}} = 3$$

$$|V| =$$

EX: Find the the vector projection of a force F= 5i+25 onto V=i-3; and scalar component of F on the direction of V?

(1) 
$$Proj_{v}F = \frac{(F \cdot V)V}{|V|^{2}}V$$
  

$$= \frac{5-6}{1+9}(i-3j) = -\frac{1}{10}(i-3j)$$

$$= -\frac{1}{10}i+\frac{3}{10}j$$

2) The Scalow component of F in the direction of Vis:

$$|F|\cos\theta = \frac{F \cdot V}{|V|} = \frac{5 - R}{\sqrt{1 + q}} = \frac{1}{\sqrt{10}}$$



Department of Medical Instrumentation Techniques Engineering

Class: second stage Subject: Mathematics II

Lecturer: Dr. Diyar Hussain Habbeb

Lecture: Lec 3

(1)

Cross product

IF We consider that U&V are two vactors, the cross product for them is:

UX X J = MINISINO

Mere (UXV) or thogonal to both (USV) and the

\* properties of cross product:-

1- (ru) X (SV) = (rs) (UXV)

2- UX (V+W)= UXV+UW

3- (V+W) XU = VXU + WXU

4- VXU=-(UXV)

5- U X0 = 0

 $(-(\vec{a} \times \vec{c}) \times \vec{b} \neq \vec{a} \times (\vec{b} \times \vec{c}).$ 

عِلَىٰ الْحَالَ الْمُعَالَىٰ الْمُعَلِّلِي الْمُعَلِّلِي الْمُعَلِّلِي الْمُعَلِّلِي الْمُعَلِّلِي الْمُعَلِّلِي الْمُعَلِّلِي الْمُعَلِّلِي الْمُعَلِّلِي الْمُعْلَىٰ الْمُعْلَىٰ الْمُعَلِّلِي الْمُعَلِّلِي الْمُعْلَىٰ الْمِعْلِى الْمُعْلَىٰ الْمُعْلَىٰ الْمُعْلَىٰ الْمُعْلَىٰ الْمُعْم



Department of Medical Instrumentation Techniques Engineering

Class: second stage Subject: Mathematics II

Lecturer: Dr. Diyar Hussain Habbeb

Lecture: Lec 3

= 3 da 2 185 x 2 (ا) نائج عليه إعزب الرجامي جو مقيه (vector) رئيس المحامي والمحامي والمحامي والمحامي والمحامي والمحامي والمحامي والمحامي والمحامية المحامية المحامي المائيه الناكر مد عليه لعنه لم المون عون عون على لا ملقهين ركونك عالى ملسوى الذي عتويما. € لد باد الحل طبيعة إعرب له كامي، صال طبقيني ؟-Odxb=101161 SINO ( Sing matrix ( ( ( ) EX1: - = i+3j+4K? Find the Cross product? Sol:- $\overrightarrow{a} \times \overrightarrow{b} = \begin{bmatrix}
i & j & k \\
i & j & k \\
i & 3 & 4
\end{bmatrix}$ axb = 1/3 4/-1/2 5/+K/2 3/  $\vec{a} \times \vec{b} = (3 \times \vec{5} - 4 \times 7)i - (1 \times \vec{5} - 4 \times 2)j + (1 \times 7 - 34)k$ = (-15-28)i-(-5-8)j+(7-6)k 08 a xb = -431+131+k



Department of Medical Instrumentation Techniques Engineering

Class: second stage Subject: Mathematics II

Lecturer: Dr. Diyar Hussain Habbeb

Lecture: Lec 3

Ex2: Find 
$$\overrightarrow{u} \times \overrightarrow{v}$$
 and  $\overrightarrow{v} \times \overrightarrow{u}$  when:

$$\overrightarrow{u} = 2i + j + k$$

$$\overrightarrow{v} = -4i + 3j + k$$

$$\overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 10k$$

$$\overrightarrow{v} \times \overrightarrow{v} = -2i - 6j + 1$$



Department of Medical Instrumentation Techniques Engineering

Class: second stage Subject: Mathematics II

Lecturer: Dr. Diyar Hussain Habbeb

Lecture: Lec 3

١٠٠٠ عقے تکون ماصل اعدب لاتجاهی = صفی When the cross product = Zero ا عنوا يكون طبخيان متلزيان وكاث باك B when the two nectors are parallel, i.e. (0 = 0/180) EX3:- Find the cross product for the following  $\frac{5018-}{9}$  0 between  $\frac{1}{9}$   $\frac{1}{9}$   $\frac{1}{9}$   $\frac{1}{9}$   $\frac{1}{9}$   $\frac{1}{9}$   $\frac{1}{9}$   $\frac{1}{9}$   $\frac{1}{9}$ So, ox x b = lal. 161. Since  $\frac{\partial}{\partial x} = \frac{\partial}{\partial b} = \frac{\partial}$ 

vectors and O between them = 0

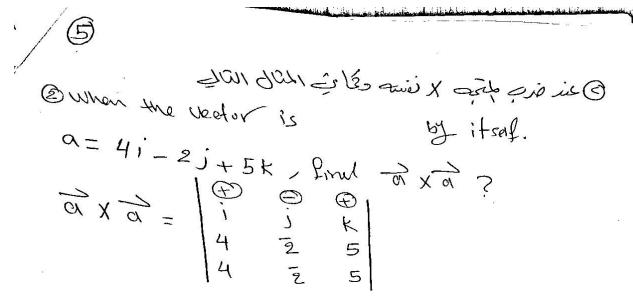


Department of Medical Instrumentation Techniques Engineering

Class: second stage Subject: Mathematics II

Lecturer: Dr. Diyar Hussain Habbeb

Lecture: Lec 3



EX5: - Find a unit vector Perpendicular to the plane constructed by P(1, 1,2), Q(2,0,1) & R(0,2,1)?

Sol: -

Sol:
$$\frac{Sol:}{PQ} = (2-1)i + (0-(-1)j + (-1+2)k)$$

$$\frac{Sol}{PQ} = (2-1)i + (0-(-1)j + (-1+2)k)$$

$$\frac{PQ}{PQ} = i + j - 3k$$

PR = (0-1)i + (2-(-1))j + (1-2)k PR = -i + 3j - k



Department of Medical Instrumentation Techniques Engineering

Class: second stage Subject: Mathematics II

Lecturer: Dr. Diyar Hussain Habbeb

Lecture: Lec 3