

### Al-Mustaqbal University College Department of Computer Engineering Techniques



# Information Theory and coding Fourth stage

# Lecture 3 Conditional Probability and Venn's Diagram

By: MSC. Ridhab Sami



# Department of Computer Engineering Techniques (Stage: 4) Information Theory and coding M.Sc. Ridhab Sami RidhabSami @mustaqbal-college.edu.iq



### **Conditional Probability:**

It is happened when there are dependent events. We have to use the symbol "|" to mean "given":

- P(B|A) means "Event B given Event A has occurred".
- P(B|A) is also called the "Conditional Probability" of B given A has occurred.
- And we write it as:

$$P(A \mid B) = \frac{number\ of\ elements\ of\ A\ and\ B}{number\ of\ elements\ of\ B}$$

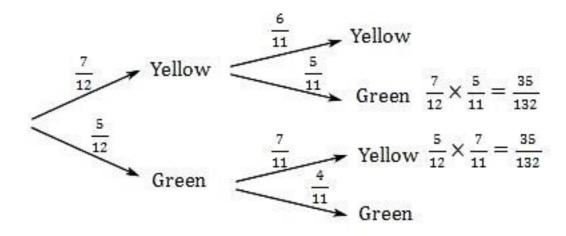
Or

$$P(A \mid B) = \frac{P(A \cap B)}{P(B)}$$

Where P(B) > 0

**Example:** A box contains 5 green pencils and 7 yellow pencils. Two pencils are chosen at random from the box without replacement. What is the probability they are different colors?

**Solution:** Using a tree diagram:







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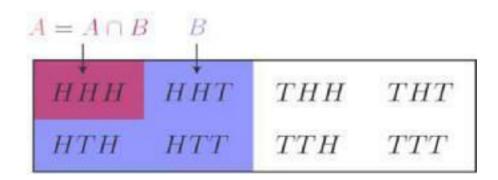
**Example:** Find the conditional prob. For Toss a fair coin 3 times :1- What is the probability of 3 heads? 2- What is the probability of head?

#### **Solution:**

 $S = \{HHH, HHT, HTH, HTT, THH, THT, TTH, TTT\}$ 

 $A = \{HHH\}$ 

 $B = \{HHH, HHT, HTH, HTT\}$ 



The conditional probability of A given B is written P(A|B) and is defined

$$P(A \mid B) = \frac{P(A \cap B)}{P(B)}$$

We have P(A)=1/8

P(B)=4/8

 $P(A \cap B) = 1/8$ 

$$P(A|B) = \frac{1/8}{4/8} = \frac{1}{4}$$





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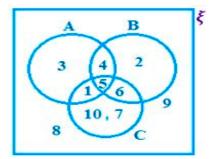
#### Venn's Diagram

A Venn diagram is a diagram that shows all possible logical relations between a finite collections of different sets. These diagrams depict elements as points in the plane, and sets as regions inside closed curves. A Venn diagram consists of multiple overlapping closed curves, usually circles, each representing a set. The points inside a curve labelled S represent elements of the set S, while points outside the boundary represent elements not in the set S. Fig. 5 shows the set  $A = \{1,2,3\}, B = \{4,5\}$  and  $U = \{1,2,3,4,5,6\}$ .

#### **Example:**

#### From the adjoining Venn diagram, find the following sets.

- (i) A
- (ii) B
- (iii) ξ
- (iv) A'
- (v) B'
- (vi) C'
- (vii) C A
- (viii) B C
- (ix) A B
- (x) A ∪ B
- (xi) B ∪ C
- (xii)  $A \cap C$
- (xiii) B ∩ C
- (xiv) (B ∪ C)'
- (xv) (A ∩ B)'
- (xvi) (A ∪ B) ∩ C









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#### Answers for examples on Venn diagram are given below:

(i) A

$$= \{1, 3, 4, 5\}$$

(ii) B

(iii) ξ

$$= \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$$

(iv) A'

all elements of universal set leaving the = {2, 6, 7, 8, 9, 10} elements of set A.

(v) B'

 $= \{1, 3, 7, 8, 9, 10\}$ all elements of universal set leaving the elements of set B.

(vi) C' = To find

$$C = \{1, 5, 6, 7, 10\}$$

Therefore, C' = {2, 3, 4, 8, 9} all elements of universal set leaving the elements of set C.

(vii) C - A

Here 
$$C = \{1, 5, 6, 7, 10\}$$

$$A = \{1, 3, 4, 5\}$$

then  $C - A = \{6, 7, 10\}$  excluding all elements of A from C.

(viii) B - C

Here 
$$B = \{4, 5, 6, 2\}$$

$$C = \{1, 5, 6, 7, 10\}$$

B - C = 
$$\{4, 2\}$$
 excluding all elements of C from B.





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#### (ix) B - A

Here 
$$B = \{4, 5, 2\}$$

$$A = \{1, 3, 4, 5\}$$

B - A = 
$$\{6, 2\}$$
 excluding all elements of A from C.

#### (x) A U B

Here 
$$A = \{1, 3, 4, 5\}$$

$$B = (4, 5, 6, 2)$$

$$A \cup B = \{1, 2, 3, 4, 5, 6\}$$

#### (xi) B U C

Here 
$$B = \{4, 5, 6, 2\}$$

$$C = \{1, 5, 6, 7, 10\}$$

$$B \cup C = \{1, 2, 4, 5, 6, 7, 10\}$$

#### (xii) (B U C)'

Since, 
$$B \cup C = \{1, 2, 4, 5, 6, 7, 10\}$$

Therefore, 
$$(B \cup C)' = \{3, 8, 9\}$$





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#### (xiii) (A ∩ B)'

$$A = \{1, 3, 4, 5\}$$

$$B = \{4, 5, 6, 2\}$$

$$(A \cap B) = \{4, 5\}$$

$$(A \cap B)' = \{1, 2, 3, 6, 7, 8, 9, 10\}$$

#### (xiv) (A ∪ B) ∩ C

$$A = \{1, 2, 3, 4\}$$

$$B = \{4, 5, 6, 2\}$$

$$C = \{1, 5, 6, 7, 10\}$$

$$A \cup B = \{1, 2, 3, 4, 5, 6\}$$

$$(A \cup B) \cap C = \{1, 5, 6\}$$

#### (xv) $A \cap (B \cap C)$

$$A = \{1, 3, 4, 5\}$$

$$B = \{4, 5, 6, 2\}$$

$$C = \{1, 5, 6, 7, 10\}$$

$$B \cap C = \{5, 6\}$$

$$A \cap (B \cap C) = \{5\}$$